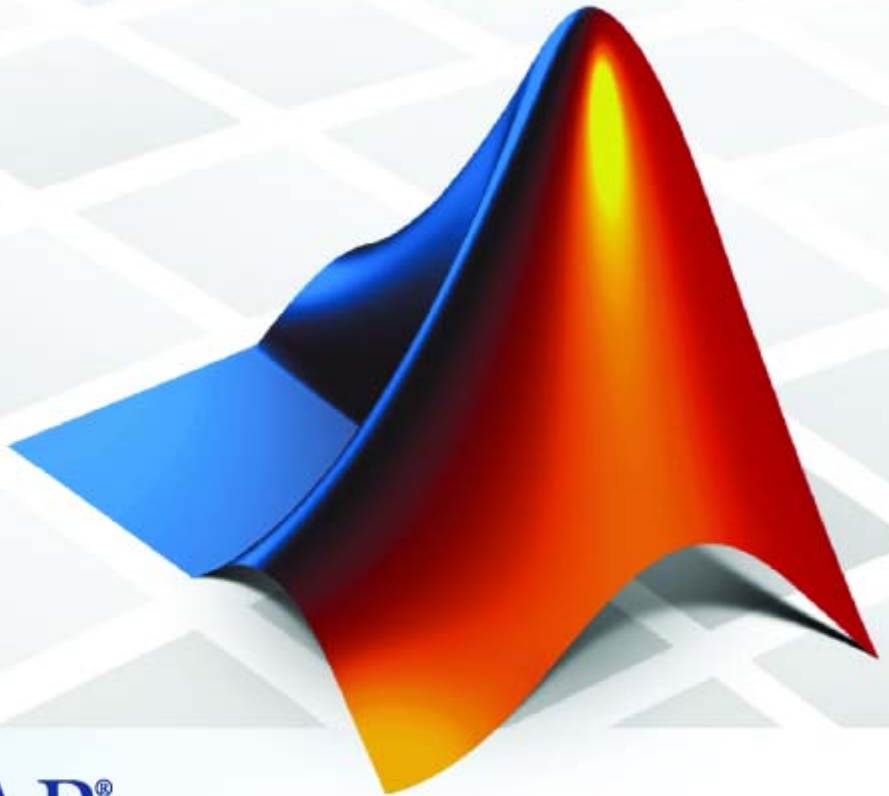


Fixed-Income Toolbox 1

User's Guide



MATLAB[®]

How to Contact The MathWorks



www.mathworks.com
comp.soft-sys.matlab
www.mathworks.com/contact_TS.html

Web
Newsgroup
Technical Support



suggest@mathworks.com
bugs@mathworks.com
doc@mathworks.com
service@mathworks.com
info@mathworks.com

Product enhancement suggestions
Bug reports
Documentation error reports
Order status, license renewals, passcodes
Sales, pricing, and general information



508-647-7000 (Phone)



508-647-7001 (Fax)



The MathWorks, Inc.
3 Apple Hill Drive
Natick, MA 01760-2098

For contact information about worldwide offices, see the MathWorks Web site.

Fixed-Income Toolbox User's Guide

© COPYRIGHT 2003–2007 by The MathWorks, Inc.

The software described in this document is furnished under a license agreement. The software may be used or copied only under the terms of the license agreement. No part of this manual may be photocopied or reproduced in any form without prior written consent from The MathWorks, Inc.

FEDERAL ACQUISITION: This provision applies to all acquisitions of the Program and Documentation by, for, or through the federal government of the United States. By accepting delivery of the Program or Documentation, the government hereby agrees that this software or documentation qualifies as commercial computer software or commercial computer software documentation as such terms are used or defined in FAR 12.212, DFARS Part 227.72, and DFARS 252.227-7014. Accordingly, the terms and conditions of this Agreement and only those rights specified in this Agreement, shall pertain to and govern the use, modification, reproduction, release, performance, display, and disclosure of the Program and Documentation by the federal government (or other entity acquiring for or through the federal government) and shall supersede any conflicting contractual terms or conditions. If this License fails to meet the government's needs or is inconsistent in any respect with federal procurement law, the government agrees to return the Program and Documentation, unused, to The MathWorks, Inc.

Trademarks

MATLAB, Simulink, Stateflow, Handle Graphics, Real-Time Workshop, and xPC TargetBox are registered trademarks, and SimBiology, SimEvents, and SimHydraulics are trademarks of The MathWorks, Inc.

Other product or brand names are trademarks or registered trademarks of their respective holders.

Patents

The MathWorks products are protected by one or more U.S. patents. Please see www.mathworks.com/patents for more information.

Revision History

May 2003	Online only	New for Version 1.0 (Release 13)
November 2003	First printing	Unchanged
June 2004	Online only	Revised for Version 1.0.1 (Release 14)
August 2004	Online only	Revised for Version 1.1 (Release 14+)
September 2005	Online only	Revised for Version 1.1.1 (Release 14SP3)
March 2006	Online only	Revised for Version 1.1.2 (Release 2006a)
September 2006	Online only	Revised for Version 1.2 (Release 2006b)
March 2007	Online only	Revised for Version 1.3 (Release 2007a)

Getting Started

1

What Is Fixed-Income Toolbox?	1-2
Using Mortgage-Backed Securities	1-2
Using Debt Instruments	1-3
Using Derivative Securities	1-3

Mortgage-Backed Securities

2

What Are Mortgage-Backed Securities?	2-2
Using Fixed-Rate Mortgage Pool Functions	2-3
Inputs to Functions	2-4
Generating Prepayment Vectors	2-4
Mortgage Prepayments	2-6
Risk Measurement	2-8
Mortgage Pool Valuation	2-9
Computing Option-Adjusted Spread (OAS)	2-10
Prepayments with Fewer Than 360 Months Remaining ..	2-13
Pools with Different Numbers of Coupons Remaining	2-15

Debt Instruments

3

Treasury Bills Defined	3-2
Computing Treasury Bill Price and Yield	3-3
Treasury Bill Repurchase Agreements	3-3
Treasury Bill Yields	3-5

Using Zero-Coupon Bonds	3-7
Measuring Zero-Coupon Bond Function Quality	3-7
Pricing Treasury Notes	3-8
Pricing Corporate Bonds	3-10
Stepped-Coupon Bonds	3-12
Cash Flows from Stepped-Coupon Bonds	3-12
Price and Yield of Stepped-Coupon Bonds	3-13
Term Structure Calculations	3-15
Computing Spot and Forward Curves	3-15
Computing Spreads	3-17

Derivative Securities

4

Pricing and Hedging	4-2
Swap Pricing Assumptions	4-2
Swap Pricing Example	4-3
Portfolio Hedging	4-8
Convertible Bond Valuation	4-10
Treasury Bond Futures	4-12
Theoretical Prices	4-12
Implied Repo	4-15
Hedge Parameters	4-16

Functions — By Category

5

Cash Flows	5-2
Certificates of Deposit	5-2

Convertible Bonds	5-3
Derivative Securities	5-3
Mortgage-Backed Securities	5-4
Option-Adjusted Spread Computations	5-5
Stepped-Coupon Bonds	5-6
Treasury Bills	5-7
Treasury Bond Futures	5-8
Zero-Coupon Instruments	5-9

Functions — Alphabetical List

6

Examples

A

Treasury Bills	A-2
Using Zero-Coupon Bonds	A-2
Stepped-Coupon Bonds	A-2
Pricing and Hedging	A-2
Treasury Bond Futures	A-2

Glossary

Index

Getting Started

What Is Fixed-Income Toolbox?
(p. 1-2)

Describes the features of
Fixed-Income Toolbox

What Is Fixed-Income Toolbox?

- “Using Mortgage-Backed Securities” on page 1-2
- “Using Debt Instruments” on page 1-3
- “Using Derivative Securities” on page 1-3

Fixed-Income Toolbox extends MATLAB® with functions for fixed-income modeling and analysis. You can use the toolbox to determine the price, yield, and cash flow for many types of fixed-income securities, including mortgage-backed securities, corporate bonds, Treasury bonds, municipal bonds, certificates of deposit, and Treasury bills. Fixed-Income Toolbox also enables you to work with derivatives, including swaps, convertible bonds, and Treasury futures. You can use built-in functions to create customized fixed-income models based on mortgage-backed securities and debt instruments. You can then use Fixed-Income Toolbox to perform the following:

- Calculate the price and yield for generic fixed-rate mortgage pools and balloon mortgages
- Determine the price, yield, discount rate, and cash-flow schedule for debt instruments, including Treasury bills, zero-coupon bonds, and stepped-coupon bonds
- Calculate swap rates and sensitivities

Using Mortgage-Backed Securities

With Fixed-Income Toolbox, you can model generic fixed-rate mortgage pools and balloon mortgages. Tools are provided for:

- Calculating the price and yield of mortgage-backed securities using prepayment options derived from uniform practices of the Public Securities Association (PSA)
- Determining the mortgage-pool price or effective duration using the option adjusted spread (OAS) method
- Calculating basic risk measurements for a mortgage-pool portfolio using convexity, duration, and average life

Using Debt Instruments

You can also use Fixed-Income Toolbox to work with a variety of debt instruments. You can calculate price, yield, discount rate, and break-even discount rate for treasury bills, as well as determine price, yield, and cash-flow schedules for corporate, treasury, and municipal bonds. The zero-coupon functions in Fixed-Income Toolbox facilitate the extraction of present value from virtually any fixed-coupon instrument for any time period. Toolbox functions also let you calculate price, yield, and cash-flow schedules for stepped-coupon bonds. The next coupon dates are computed automatically from the last entered input end dates. The payment due on settlement represents the accrued interest due on that day.

Using Derivative Securities

In addition, Fixed-Income Toolbox provides tools based on Black's option functions for working with fixed-income derivatives. These tools let you calculate swap price by computing par yields that equate the floating-rate side of a swap to the fixed-rate side. You can set the present value of the fixed side to the present value of the floating side without aligning and comparing fixed and floating periods. The duration-hedging capability in the toolbox lets you hedge a portfolio and address interest-rate risk exposure with a swap arrangement. Fixed-Income Toolbox lets you use binomial and trinomial trees to value convertible bonds. The value of the convertible bond is determined by the uncertainty of the relative stock.

Mortgage-Backed Securities

What Are Mortgage-Backed Securities? (p. 2-2)

Describes mortgages and mortgage passthrough securities

Using Fixed-Rate Mortgage Pool Functions (p. 2-3)

Illustrates the use of toolbox functions to perform common calculations involved with mortgage-backed securities

What Are Mortgage-Backed Securities?

Mortgage-backed securities (MBS) are a type of investment that represents ownership in a group of mortgages. Principal and interest from the individual mortgages are used to pay principal and interest on the MBS.

Ownership in a group of mortgages is typically represented by a *passthrough certificate* (PC). Most passthrough certificates are issued by the Government National Mortgage Agency, a branch of the United States Government, or by one of two private corporations: Fannie Mae or Freddie Mac. With these certificates, homeowners' payments pass from the originating bank through the issuing agency to holders of the certificates. These agencies also frequently guarantee that the certificate holder receives timely payment of principal and interest from the PCs.

Using Fixed-Rate Mortgage Pool Functions

- “Inputs to Functions” on page 2-4
- “Generating Prepayment Vectors” on page 2-4
- “Mortgage Prepayments” on page 2-6
- “Risk Measurement” on page 2-8
- “Mortgage Pool Valuation” on page 2-9
- “Computing Option-Adjusted Spread (OAS)” on page 2-10
- “Prepayments with Fewer Than 360 Months Remaining” on page 2-13
- “Pools with Different Numbers of Coupons Remaining” on page 2-15

Fixed-Income Toolbox supports calculations involved with generic fixed-rate mortgage pools and balloon mortgages. Passthrough certificates typically have embedded call options in the form of prepayment. Prepayment is an excess payment applied to the principal of a PC. These accelerated payments reduce the effective life of a PC.

The toolbox comes with a standard Public Securities Association (PSA) prepayment model and can generate multiples of standard prepayment speeds. The Public Securities Association provides a set of uniform practices for calculating the characteristics of mortgage-backed securities when there is an assumed prepayment function.

You can obtain more information about these uniform practices on the PSA Web site (<http://www.bondmarkets.com>).

Alternatively, aside from the standard PSA implementation in this toolbox, you can supply your own projected prepayment vectors. At this time, however, custom prepayment functionality that incorporates pool-specific information and interest rate forecasts are not available in this toolbox. If you plan to use custom prepayment vectors in your calculations, you presumably already own such a suite in MATLAB.

Inputs to Functions

Because of the generic, all-purpose nature of the toolbox passthrough functions, users can fine tune them to conform to a particular mortgage. Most functions require at least this set of inputs:

- Gross coupon rate
- Settlement date
- Issue (effective) date
- Maturity date

Typical optional inputs include standard prepayment speed (or customized vector), net coupon rate (if different from gross coupon rate), and payment delay in number of days.

All calculations are based on expected payment dates and actual cash flow to the investor. For example, when `GrossRate` and `CouponRate` differ as inputs to `mbstdurp`, the function returns a modified duration based on `CouponRate`. (A notable exception is `mbspassthrough`, which returns interest quantities based on the `GrossRate`.)

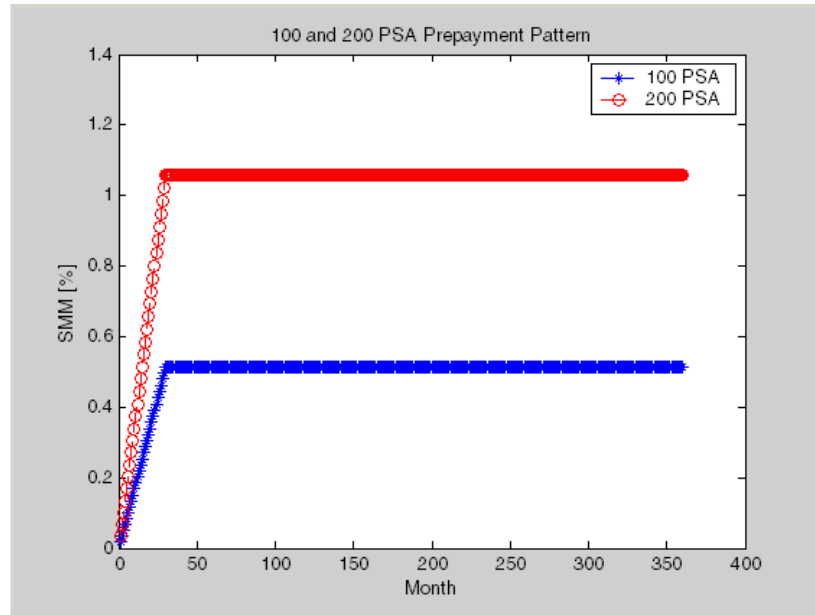
Generating Prepayment Vectors

You can generate PSA multiple prepayment vectors very quickly. To generate prepayment vectors of 100 and 200 PSA, type

```
PSASpeed = [100, 200];  
[CPR, SMM] = psaspeed2rate(PSASpeed);
```

This function computes two prepayment values: conditional prepayment rate (CPR) and single monthly mortality (SMM) rate. CPR is the percentage of outstanding principal prepaid in one year. SMM is the percentage of outstanding principal prepaid in one month. In other words, CPR is an annual version of SMM.

Since the entire 360-by-2 array is too long to show in this document, observe the SMM (100 and 200 PSA) plots, spaced one month apart, instead.



Prepayment assumptions form the basis upon which far more comprehensive MBS calculations are based. As an illustration observe the following example, which demonstrates the use of the function `mbscfamounts` to generate cash flows and timings based on a set of standard prepayments.

Consider three mortgage pools that were sold on the issue date (which starts unamortized). The first two pools "balloon out" in 60 months, and the third is regularly amortized to the end. The prepayment speeds are assumed to be 100, 200, and 200 PSA, respectively.

```
Settle      = [datenum('1-Feb-2000');
              datenum('1-Feb-2000');
              datenum('1-Feb-2000')];

Maturity    = [datenum('1-Feb-2030')];

IssueDate   = datenum('1-Feb-2000');
GrossRate   = 0.08125;
CouponRate  = 0.075;
Delay       = 14;
```

```

PSASpeed = [100, 200];
[CPR, SMM] = psaspeed2rate(PSASpeed);

PrepayMatrix = ones(360,3);
PrepayMatrix(1:60,1:2) = SMM(1:60,1:2);
PrepayMatrix(:,3) = SMM(:,2);

[CFlowAmounts, CFlowDates, TFactors, Factors] = ...
mbscfamounts(Settle, Maturity, IssueDate, GrossRate, ...
CouponRate, Delay, [], PrepayMatrix);

```

The fourth output argument, `Factors`, indicates the fraction of the balance still outstanding at the beginning of each month. A snapshot of this argument in the MATLAB array editor illustrates the 60-month life of the first two of the mortgages with balloon payments and the continuation of the third mortgage until the end (360 months).

	59	60	61	62	63	64	65
1	0.7627	0.75801	0.75334	0	0	0	0
2	0.60207	0.59509	0.58818	0	0	0	0
3	0.60207	0.59509	0.58818	0.58135	0.57459	0.56791	0.5613

You can readily see that `mbscfamounts` is the building block of most fixed rate and balloon pool cash flows.

Mortgage Prepayments

Prepayment is beneficial to the passthrough owner when a mortgage pool has been purchased at discount. The next example compares mortgage yields (compounded monthly) versus the purchase clean price with constant prepayment speed. The example illustrates that when you have purchased a pool at a discount, prepayment generates a higher yield with decreasing purchase price.

```
Price = [85; 90; 95];
Settle = datenum('15-Apr-2002');
Maturity = datenum('1 Jan 2030');
IssueDate = datenum('1-Jan-2000');
GrossRate = 0.08125;
CouponRate = 0.075;
Delay = 14;
Speed = 100;
```

Compute the mortgage and bond-equivalent yields.

```
[MYield, BEMBSYield] = mbsyield(Price, Settle, Maturity, ...
IssueDate, GrossRate, CouponRate, Delay, Speed)
```

```
MYield =
```

```
0.1018
0.0918
0.0828
```

```
BEMBSYield =
```

```
0.1040
0.0936
0.0842
```

If for this same pool of mortgages, there was no prepayment (Speed = 0), the yields would decline to

```
MYield =
```

```
0.0926
0.0861
0.0802
```

```
BEMBSYield =
```

```
0.0944
0.0877
0.0815
```

Likewise, if the rate of prepayment doubled (Speed = 200), the yields would increase to

MYield =

0.1124

0.0984

0.0858

BEMBSYield =

0.1151

0.1004

0.0873

For the same prepayment vector, deeper discount pools earn higher yields. For more information, see `mbsprice` and `mbsyield`.

Risk Measurement

Fixed-Income Toolbox provides the most basic risk measures of a pool portfolio:

- Modified duration
- Convexity
- Average life of pool

Consider the following example, which calculates the Macaulay and modified durations given the price of a mortgage pool.

```
Price = [95; 100; 105];
Settle = datenum('15-Apr-2002');
Maturity = datenum('1-Jan-2030');
IssueDate = datenum('1-Jan-2000');
GrossRate = 0.08125;
CouponRate = 0.075;
Delay = 14;
Speed = 100;
```

```
[YearDuration, ModDuration] = mbsdurp(Price, Settle, ...
Maturity, IssueDate, GrossRate, CouponRate, Delay, Speed)
```

```
YearDuration =
```

```
6.1341
6.3882
6.6339
```

```
ModDuration =
```

```
5.8863
6.1552
6.4159
```

Using Fixed-Income Toolbox functions, you can obtain modified duration and convexity from either price or yield, as long as you specify a prepayment vector or an assumed prepayment speed. The toolbox risk-measurement functions (`mbsdurp`, `mbsdury`, `mbsconvp`, `mbsconvy`, and `mbswal`) adhere to the guidelines listed in the *PSA Uniform Practices* manual.

Mortgage Pool Valuation

For accurate valuation of a mortgage pool, you must generate interest rate paths and use them in conjunction with mortgage pool characteristics to properly value the pool. A widely used methodology is the option-adjusted spread (OAS). OAS measures the yield spread that is not directly attributable to the characteristics of a fixed-income investment.

Calculating OAS

Prepayment alters the cash flows of an otherwise regularly amortizing mortgage pool. A comprehensive option-adjusted spread calculation typically begins with the generation of a set of paths of spot rates to predict prepayment. A path is collection of i spot-rate paths, with corresponding j cash flows on each of those paths.

The effect of the OAS on pool pricing is shown mathematically in the following equation, where K represents the option-adjusted spread.

$$PoolPrice = \frac{1}{NumberofPaths} \times \sum_i^{NumberofPaths} \sum_j \frac{CF_{ij}}{(1 + zerorates_{ij} + K)^{T_{ij}}}$$

Calculating Effective Duration

Alternatively, if you are more interested in the sensitivity of a mortgage pool to interest rate changes, you should use effective duration, which is a more appropriate measure. Effective duration is defined mathematically with the following equation.

$$Effective\ Duration = \frac{P(y + \Delta y) - P(y - \Delta y)}{2P(y)\Delta y}$$

Calculating Market Price

The toolbox has all the components required to calculate OAS and effective duration if you supply prepayment vectors or assumptions. For OAS, given a prepayment vector, you can generate a set of cash flows with `mbscf` amounts. Discounting these cash flows with the reference curve and then adding OAS produces the market price. See “Computing Option-Adjusted Spread (OAS)” on page 2-10 for a discussion on the computation of option-adjusted spread.

Effective duration is a more difficult issue. While modified duration changes the discounting process (by changing the yield used to discount cash flows), effective duration must account for the change in cash flow because of the change in yield. A possible solution is to recompute prices using `mbsprice` for a small change in yield, in both the upwards and downwards directions. In this case, you must recompute the prepayment input. Internally, this alters the cash flows of the mortgage pool. Assuming that the OAS stays constant in all yield environments, you can apply a set of discounting factors to the cash flows in up and down yield environments to find the effective duration.

Computing Option-Adjusted Spread (OAS)

The option-adjusted spread is an amount of extra interest added above (or below if negative) the reference zero curve. To compute the OAS, you must provide the zero curve as an extra input. You can specify the zero curve in any intervals and with any compounding method. (To minimize any error due to interpolation, keep the intervals as regular and frequent as possible.)

You must supply a prepayment vector or specify a speed corresponding to a standard PSA prepayment vector.

One way to compute the appropriate zero curve for an agency is to look at its bond yields and bootstrap them from the shortest maturity onwards. You can do this with Financial Toolbox functions `zbtprice` and `zbtyield`.

The following example demonstrates how to calculate an appropriate zero curve followed by computation of the pool's OAS. This example calculates the OAS of a 30-year fixed rate mortgage with approximately a 28-year weighted average maturity left, given an assumption of 0, 50, and 100 PSA prepayment speeds.

Create curve for zerorates.

```
Bonds = [datenum('11/21/2002') 0 100 0 2 1;
          datenum('02/20/2003') 0 100 0 2 1;
          datenum('07/31/2004') 0.03 100 2 3 1;
          datenum('08/15/2007') 0.035 100 2 3 1;
          datenum('08/15/2012') 0.04875 100 2 3 1;
          datenum('02/15/2031') 0.05375 100 2 3 1];

Yields = [0.0162;
          0.0163;
          0.0211;
          0.0328;
          0.0420;
          0.0501];
```

Since the above is Treasury data and not selected agency data, a term structure of spread is assumed. In this example, the spread declines proportionally from a maximum of 250 basis points at the shortest maturity.

```
Yields = Yields + 0.025 * (1./[1:6]');
```

Get parameters from Bonds matrix.

```
Settle = datenum('20-Aug-2002');
Maturity = Bonds(:,1);
CouponRate = Bonds(:,2);
Face = Bonds(:,3);
```

```
Period = Bonds(:,4);
Basis = Bonds(:,5);
EndMonthRule = Bonds(:,6);

[Prices, AccruedInterest] = bndprice(Yields, CouponRate, ...
Settle, Maturity, Period, Basis, EndMonthRule, [], [], [], [], ...
Face);
```

Use `zbtprice` to solve for zero rates.

```
[ZeroRatesP, CurveDatesP] = zbtprice(Bonds, Prices, Settle);
ZeroCompounding = 2*ones(size(ZeroRatesP));
ZeroMatrix = [CurveDatesP, ZeroRatesP, ZeroCompounding];
```

Use output from `zbtprice` to calculate the OAS.

```
Price = 95;
Settle = datenum('20-Aug-2002');
Maturity = datenum('2-Jan-2030');
IssueDate = datenum('2-Jan-2000');
GrossRate = 0.08125;
CouponRate = 0.075;
Delay = 14;
Interpolation = 1;
PrepaySpeed = [0; 50; 100];

OAS = mbsprice2oas(ZeroMatrix, Price, Settle, Maturity, ...
IssueDate, GrossRate, CouponRate, Delay, Interpolation, ...
PrepaySpeed)

OAS =

    26.0502
    28.6348
    31.2222
```

This example shows that one cash flow set is being discounted and solved for its OAS, as contrasted with the `NumberOfPaths` set of cash flows as shown in “Mortgage Pool Valuation” on page 2-9. Averaging the sets of cash flows resulting from all simulations into one average cash flow vector and solving

for the OAS, discounts the averaged cash flows to have a present value of today's (average) price.

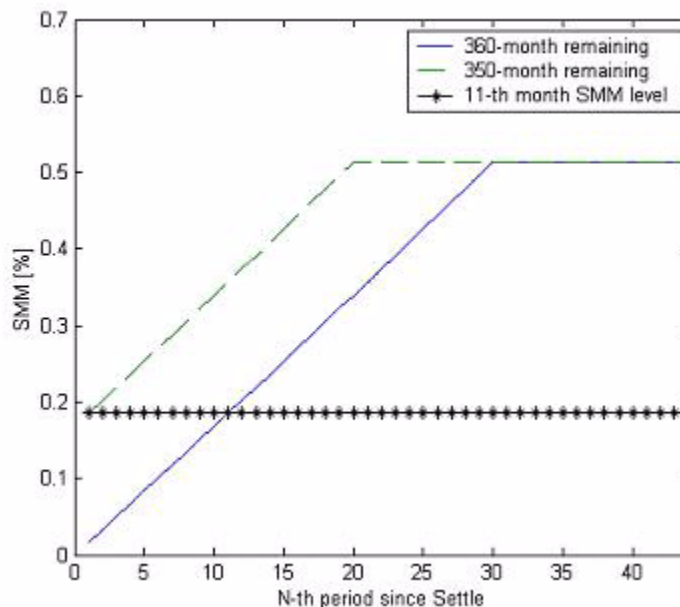
While this example uses the mortgage pool price (`mbsprice2oas`) to determine the OAS, you can also use yield to resolve it (`mbsyield2oas`). Also, there are reverse OAS functions that return prices and yields given OAS (`mbsoas2price` and `mbsoas2yield`).

The example also restates earlier examples that show discount securities benefit from higher level of prepayment, keeping everything else unchanged. The relation is reversed for premium securities.

Prepayments with Fewer Than 360 Months Remaining

When fewer than 360 months remain in the pool, the applicable PSA prepayment vector is "seasoned" by the pool's age. (Elements in the 360-element prepayment vector that represent past payments are skipped. For example, on a 30-year mortgage that is 10-months old, only the final 350 prepayments are applied.)

Assume, for example, that you have two 30-year loans, one new and another 10-months old. Both have the same PSA speed of 100 and prepay using the vectors plotted below.



Still within the scope of relative valuation, you could also solve for the percentage of the standard PSA prepayment vector given the pool's arbitrary, user-supplied prepayment vector, such that the PSA speed gives the same Macaulay duration as the user-supplied prepayment vector.

If you supply a custom prepayment vector, you must account for the number of months remaining.

```
Price = 101;
Settle = datenum('1-Jan-2001');
Maturity = datenum('1-Jan-2030');
IssueDate = datenum('1-Jan-2000');
GrossRate = 0.08125;
PrepayMatrix = 0.005*ones(348,1);
CouponRate = 0.075;
Delay = 14;
```

```
ImpliedSpeed = mbsprice2speed(Price, Settle, Maturity, ...
IssueDate, GrossRate, PrepayMatrix, CouponRate, Delay)
```

```
ImpliedSpeed =
```

```
104.2526
```

Examine the prepayment input. The remaining 29 years require 348 monthly elements in the prepayment vector. Suppose then, keeping everything the same, you change `Settle` to February 14, 2003.

```
Settle = datenum('14-Feb-2003');
```

You can use `cpncount` to count all incoming coupons received after `Settle` by invoking

```
NumCouponsRemaining = cpncount(Settle, Maturity, 12, 1, [], ...
    IssueDate)
```

```
NumCouponsRemaining =
323
```

The input 12 defines the monthly payment frequency, 1 defines the 30/360 basis, and `IssueDate` defines aging and determination-of-holder date. Thus, you must supply a 323-element vector to properly account for prepayment corresponding to each monthly payment.

Pools with Different Numbers of Coupons Remaining

Suppose one pool has two remaining coupons, and the other has three. MATLAB expects the prepayment matrix to be in the following format:

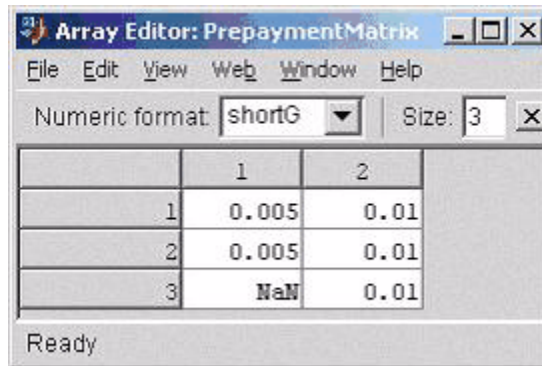
```
V11      V21
V12      V22
NaN      V23
```

V_{ij} denotes the single monthly mortality (SMM) rate for pool i during the j th coupon period since `Settle`.

The use of NaN to pad the prepayment matrix is necessary because MATLAB cannot concatenate vectors of different lengths into a matrix. Also, it can

serve as an error check against any unintended operation (any MATLAB operation that would return NaN).

For example, assume that the two-month pool has a constant SMM of 0.5% and the three-month has a constant SMM of 1% in every period. The prepayment matrix you would create is depicted below.



The screenshot shows the MATLAB Array Editor window titled "Array Editor: PrepaymentMatrix". The window has a menu bar with "File", "Edit", "View", "Web", "Window", and "Help". Below the menu bar, there is a "Numeric format" dropdown set to "shortG" and a "Size" field set to "3". The main area displays a 3x2 matrix with the following values:

	1	2
1	0.005	0.01
2	0.005	0.01
3	NaN	0.01

The status bar at the bottom of the window shows "Ready".

Create this input in whatever manner is best for you.

Summary of Prepayment Data Vector Representation

- When you specify a PSA prepayment speed, MATLAB "seasons" the pool according to its age.
- When you specify your own prepayment matrix, identify the maximum number of coupons remaining using `cpncount`. Then supply the matrix elements up to the point when cash flow ceases to exist.
- When different length pools must exist in the same matrix, pad the shorter one(s) with NaN. Each column of the prepayment matrix corresponds to a specific pool.

Debt Instruments

Treasury Bills Defined (p. 3-2)	Defines Treasury bills and distinguishes them from Treasury notes and bonds
Computing Treasury Bill Price and Yield (p. 3-3)	Describes the functions included in this toolbox for computing prices and yields on Treasury bills
Using Zero-Coupon Bonds (p. 3-7)	Shows the use of zero-coupon bonds as a method to price Treasury notes and corporate bonds
Stepped-Coupon Bonds (p. 3-12)	Discusses cash flow, prices, and yields on bonds whose coupons change over time
Term Structure Calculations (p. 3-15)	Describes the construction of Treasury spot, par-yield, and forward curves and their application in computing rate spreads

Treasury Bills Defined

Treasury bills are short-term securities (issued with maturities of one year or less) sold by the United States Treasury. Sales of these securities are frequent, usually weekly. From time to time, the Treasury also offers longer duration securities called Treasury notes and Treasury bonds.

A Treasury bill is a discount security. The holder of the Treasury bill does not receive periodic interest payments. Instead, at the time of sale, a percentage discount is applied to the face value. At maturity, the holder redeems the bill for full face value.

The basis for Treasury bill interest calculation is actual/360. Under this system, interest accrues on the actual number of elapsed days between purchase and maturity, and each year contains 360 days.

Computing Treasury Bill Price and Yield

- “Treasury Bill Repurchase Agreements” on page 3-3
- “Treasury Bill Yields” on page 3-5

Fixed-Income Toolbox provides the following suite of functions for computing price and yield on Treasury bills.

Treasury Bill Functions

Function	Purpose
tbilldisc2yield	Convert discount rate to yield.
tbillprice	Price Treasury bill given its yield or discount rate.
tbillrepo	Break-even discount of repurchase agreement.
tbillyield	Yield and discount of Treasury bill given its price.
tbillyield2disc	Convert yield to discount rate.
tbillval01	The value of one basis point given the characteristics of the Treasury bill, as represented by its settlement and maturity dates. You can relate the basis point to discount, money-market, or bond-equivalent yield.

For all functions with yield in the computation, you can specify yield as money-market or bond-equivalent yield. The functions all assume a face value of \$100 for each Treasury bill.

Treasury Bill Repurchase Agreements

The following example shows how to compute the break-even discount rate. This is the rate that correctly prices the Treasury bill such that the profit from selling the bill equals 0.

```
Maturity = '26-Dec-2002';
InitialDiscount = 0.0161;
PurchaseDate = '26-Sep-2002';
SaleDate = '26-Oct-2002';
```

```
RepoRate = 0.0149;
```

```
BreakevenDiscount = tbillrepo(RepoRate, InitialDiscount, ...  
PurchaseDate, SaleDate, Maturity)
```

```
BreakevenDiscount =
```

```
0.0167
```

You can check the result of this computation by examining the cash flows in and out from the repurchase transaction. First compute the price of the Treasury bill on the purchase date (September 26).

```
PriceOnPurchaseDate = tbillprice(InitialDiscount, ...  
PurchaseDate, Maturity, 3)
```

```
PriceOnPurchaseDate =
```

```
99.5930
```

Next compute the interest due on the repurchase agreement.

```
RepoInterest = ...
```

```
RepoRate*PriceOnPurchaseDate*days360(PurchaseDate, SaleDate) / 360
```

```
RepoInterest =
```

```
0.1237
```

RepoInterest for a 1.49% 30-day term repurchase agreement (30/360 basis) is 0.1237.

Finally, compute the price of the Treasury bill on the sale date (October 26).

```
PriceOnSaleDate = tbillprice(BreakevenDiscount, SaleDate, ...  
Maturity, 3)
```

```
PriceOnSaleDate =
```

```
99.7167
```


Examining the cash flows, observe that the break-even discount causes the sum of the price on the purchase date plus the accrued 30-day interest to be equal to the price on sale date. The next table shows the cash flows.

Cash Flows from Repurchase Agreement

Date	Cash Out Flow		Cash In Flow	
9/26/2002	Purchase T-bill	99.593	Repo money	99.593
10/26/2002	Payment of repo	99.593	Sell T-bill	99.7168
	Repo interest	0.1238		
	Total	199.3098		199.3098

Treasury Bill Yields

Using the same data as before, you can examine the money-market and bond-equivalent yields of the Treasury bill at the time of purchase and sale. The function `tbilldisc2yield` can perform both computations at one time.

```
Maturity = '26-Dec-2002';
InitialDiscount = 0.0161;
PurchaseDate = '26-Sep-2002';
SaleDate = '26-Oct-2002';
RepoRate = 0.0149;
BreakevenDiscount = tbillrepo(RepoRate, InitialDiscount, ...
PurchaseDate, SaleDate, Maturity)
```

```
[BEYield, MMYield] = ...
tbilldisc2yield([InitialDiscount; BreakevenDiscount], ...
[PurchaseDate; SaleDate], Maturity)
```

```
BEYield =
```

```
0.01639
0.01700
```

```
MMYield =
```

0.01617

0.01677

For the short Treasury bill (fewer than 182 days to maturity), the money-market yield is $360/365$ of the bond-equivalent yield, as this example shows.

Using Zero-Coupon Bonds

- “Measuring Zero-Coupon Bond Function Quality” on page 3-7
- “Pricing Treasury Notes” on page 3-8
- “Pricing Corporate Bonds” on page 3-10

A zero-coupon bond is a corporate, Treasury, or municipal debt instrument that pays no periodic interest. Typically, the bond is redeemed at maturity for its full face value. It will be a security issued at a discount from its face value, or it may be a coupon bond stripped of its coupons and repackaged as a zero-coupon bond.

Fixed-Income Toolbox provides functions for valuing zero-coupon debt instruments. These functions supplement existing coupon bond functions such as `bndprice` and `bndyield` that are available in Financial Toolbox.

Measuring Zero-Coupon Bond Function Quality

Zero-coupon function quality is measured by how consistent the results are with coupon-bearing bonds. Because the zero's yield is essentially bond-equivalent, comparisons with coupon-bearing bonds are possible.

In the textbook case, where time (t) is measured continuously and the rate (r) is continuously compounded, the value of a zero bond is simply the principal multiplied by $e^{-r \cdot t}$. In reality, the rate quoted is rarely continuous and the basis can be variable, requiring a more consistent approach to meet the stricter demands of accurate pricing.

The following two examples

- “Pricing Treasury Notes” on page 3-8
- “Pricing Corporate Bonds” on page 3-10

show how the zero functions are consistent with supported coupon bond functions.

Pricing Treasury Notes

A Treasury note can be considered to be a package of zeros. The toolbox functions that price zeros require a coupon bond equivalent yield. That yield can originate from any type of coupon paying bond, with any periodic payment, or any accrual basis. The next example shows the use of the toolbox to price a Treasury note and compares the calculated price with the actual price quotation for that day.

```
Settle = datenum('02-03-2003');
MaturityCpn = datenum('05-15-2009');
Period = 2;
Basis = 0;
```

```
% Quoted yield.
QYield = 0.03342;
```

```
% Quoted price.
QPriceACT = 112.127;
```

```
CouponRate = 0.055;
```

Extract the cash flow and compute price from the sum of zeros discounted.

```
[CFlows, CDates] = cfamounts(CouponRate, Settle, MaturityCpn, ...
Period, Basis);
MaturityofZeros = CDates;
```

Compute the price of the coupon bond identically as a collection of zeros by multiplying the discount factors to the corresponding cash flows.

```
PriceofZeros = CFlows * zeroprice(QYield, Settle, ...
MaturityofZeros, Period, Basis)/100;
```

The following table shows the intermediate calculations.

Cash Flows	Discount Factors	Discounted Cash Flows
-1.2155	1.0000	-1.2155
2.7500	0.9908	2.7246
2.7500	0.9745	2.6799
2.7500	0.9585	2.6359
2.7500	0.9427	2.5925
2.7500	0.9272	2.5499
2.7500	0.9120	2.5080
2.7500	0.8970	2.4668
2.7500	0.8823	2.4263
2.7500	0.8678	2.3864
2.7500	0.8535	2.3472
2.7500	0.8395	2.3086
2.7500	0.8257	2.2706
102.7500	0.8121	83.4451
	Total	112.1263

Compare the quoted price and the calculated price based on zeros.

[QPriceACT PriceofZeros]

ans =

112.1270 112.1263

This example shows that zeroprice can satisfactorily price a Treasury note, a semiannual actual/actual basis bond, as if it were a composed of a series of zero-coupon bonds.

Pricing Corporate Bonds

You can similarly price a corporate bond, for which there is no corresponding zero-coupon bond, as opposed to a Treasury note, for which corresponding zeros exist. You can create a synthetic zero-coupon bond and arrive at the quoted coupon-bond price when you later sum the zeros.

```
Settle = datenum('02-05-2003');
MaturityCpn = datenum('01-14-2009');
Period = 2;
Basis = 1;
% Quoted yield.
QYield = 0.05974;
% Quoted price.
QPrice30 = 99.382;
CouponRate = 0.05850;
```

Extract cash flow and compute price from the sum of zeros.

```
[CFlows, CDates] = cfamounts(CouponRate, Settle, MaturityCpn, ...
    Period, Basis);

Maturity = CDates;
```

Compute the price of the coupon bond identically as a collection of zeros by multiplying the discount factors to the corresponding cash flows.

```
Price30 = CFlows * zeroprice(QYield, Settle, Maturity, Period, ...
    Basis)/100;
```

Compare quoted price and calculated price based on zeros.

```
[QPrice30 Price30]

ans =

    99.3820    99.3828
```

As a test of fidelity, intentionally giving the wrong basis, say actual/actual (Basis = 0) instead of 30/360, gives a price of 99.3972. Such a systematic

error, if recurring in a more complex pricing routine, quickly adds up to large inaccuracies.

In summary, the zero functions in MATLAB facilitate extraction of present value from virtually any fixed-coupon instrument, up to any period in time.

Stepped-Coupon Bonds

- “Cash Flows from Stepped-Coupon Bonds” on page 3-12
- “Price and Yield of Stepped-Coupon Bonds” on page 3-13

A stepped-coupon bond has a fixed schedule of changing coupon amounts. Like fixed coupon bonds, stepped-coupon bonds could have different periodic payments and accrual bases.

The functions `stepcpnprice` and `stepcpnyield` compute prices and yields of such bonds. An accompanying function `stepcpncfamounts` produces the cash flow schedules pertaining to these bonds.

Cash Flows from Stepped-Coupon Bonds

Consider a bond that has a schedule of two coupons. Suppose the bond starts out with a 2% coupon that steps up to 4% in two years and onwards to maturity. Assume that the issue and settlement dates are both March 15, 2003. The bond has a five-year maturity. Use `stepcpncfamounts` to generate the cash flow schedule and times.

```
Settle      = datenum('15-Mar-2003');
Maturity    = datenum('15-Mar-2008');
ConvDates   = [datenum('15-Mar-2005')];
CouponRates = [0.02, 0.04];

[CFlows, CDates, CTimes] = stepcpncfamounts(Settle, Maturity, ...
ConvDates, CouponRates)
```

Notably, `ConvDates` has one less element than `CouponRates` because MATLAB assumes that the first element of `CouponRates` indicates the coupon schedule between `Settle` (March 15, 2003) and the first element of `ConvDates` (March 15, 2005), shown diagrammatically below.

	Pay 2% from March 15, 2003		Pay 4% from March 15, 2003
Effective 2% on March 15, 2003		Effective 4% on March 15, 2005	

Coupon Dates	Semiannual Coupon Payment
15-Mar-03	0
15-Sep-03	1
15-Mar-04	1
15-Sep-04	1
15-Mar-05	1
15-Sep-05	2
15-Mar-06	2
15-Sep-06	2
15-Mar-07	2
15-Sep-07	2
15-Mar-08	102

The payment on March 15, 2005 is still a 2% coupon. Payment of the 4% coupon starts with the next payment, September 15, 2005. March 15, 2005 is the end of first coupon schedule, not to be confused with the beginning of the second.

In summary, MATLAB takes user input as the end dates of coupon schedules and computes the next coupon dates automatically.

The payment due on settlement (zero in this case) represents the accrued interest due on that day. It is negative if such amount is nonzero. Comparison with `cfamounts` in Financial Toolbox shows that the two functions operate identically.

Price and Yield of Stepped-Coupon Bonds

The toolbox provides two basic analytical functions to compute price and yield for stepped-coupon bonds. Using the above bond as an example, you can compute the price when the yield is known.

You can estimate the yield to maturity as a number-of-year weighted average of coupon rates. For this bond, the estimated yield is

$$\frac{(2 \times 2) + (4 \times 3)}{5}$$

or 3.33%. While definitely not exact (due to nonlinear relation of price and yield), this estimate suggests close to par valuation and serves as a quick first check on the function.

Yield = 0.0333;

```
[Price, AccruedInterest] = stepcpnprice(Yield, Settle, ...  
Maturity, ConvDates, CouponRates)
```

The price returned is 99.2237 (per \$100 notional), and the accrued interest is zero, consistent with our earlier assertions.

To validate that there is consistency among the stepped-coupon functions, you can use the above price and see if indeed it implies a 3.33% yield by using `stepcpnyield`.

```
YTM = stepcpnyield(Price, Settle, Maturity, ConvDates, ...  
CouponRates)
```

YTM =

0.0333

Term Structure Calculations

- “Computing Spot and Forward Curves” on page 3-15
- “Computing Spreads” on page 3-17

So far we have avoided a more formal definition of "yield" and its application. In many situations when cash flow is available, discounting factors to the cash flows may not be immediately apparent. In other cases, what is relevant is often a *spread*, the difference between curves (also known as the term structure of spread).

All these calculations require one main ingredient, the Treasury spot, par-yield, or forward curve. Typically, the generation of these curves starts with a series of on-the-run and selected off-the-run issues as inputs.

MATLAB uses these bonds to find spot rates one at a time, from the shortest maturity onwards, using bootstrap techniques. All cash flows are used to construct the spot curve, and rates between maturities (for these coupons) are interpolated linearly.

Computing Spot and Forward Curves

For an illustration of how this works, observe the use of `zbtyield` (or equivalently `zbtprice`) on a portfolio of six Treasury bills and bonds.

Bills	Maturity Date	Current Yield
3 month	4/17/03	1.15
6 month	7/17/03	1.18

Notes/Bonds	Coupon	Maturity Date	Current Yield
2 year	1.750	12/31/04	1.68
5 year	3.000	11/15/07	2.97
10 year	4.000	11/15/12	4.01
30 year	5.375	2/15/31	4.92

You can specify prices or yields to the bonds above to infer the spot curve. The function `zbyield` accepts yields (bond-equivalent yield, to be exact).

To proceed, first assemble the above table into a variable called `Bonds`. The first column contains maturities, the second contains coupons, and the third contains notionals or face values of the bonds. (Note that bills have zero coupons.)

```
Bonds = [datenum('04/17/2003')    0        100;
         datenum('07/17/2003')    0        100;
         datenum('12/31/2004')    0.0175   100;
         datenum('11/15/2007')    0.03     100;
         datenum('11/15/2012')    0.04     100;
         datenum('02/15/2031')    0.05375  100];
```

Then specify the corresponding yields.

```
Yields = [0.0115;
          0.0118;
          0.0168;
          0.0297;
          0.0401;
          0.0492];
```

You are now ready to compute the spot curve for each of these six maturities. The spot curve is based upon a settlement date of January 17, 2003.

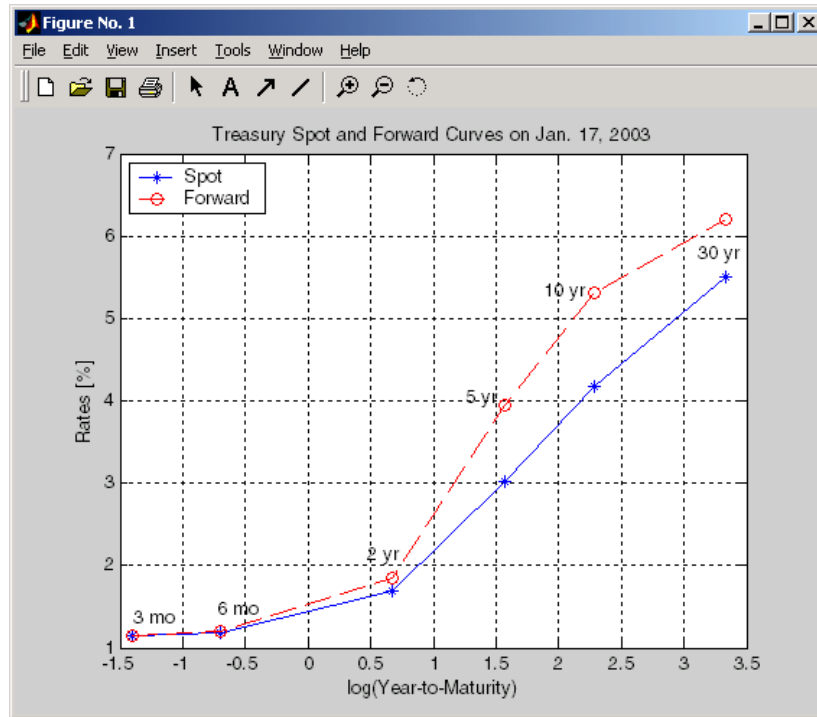
```
Settle = datenum('17-Jan-2003');
[ZeroRates, CurveDates] = zbyield(Bonds, Yields, Settle)
```

This gets you the Treasury spot curve for the day.

You can compute the forward curve from this spot curve with `zero2fwd`.

```
[ForwardRates, CurveDates] = zero2fwd(ZeroRates, CurveDates, ...
Settle)
```

Here the notion of forward rates refers to rates between the maturity dates shown above, not to a certain period (forward three-month rates, for example).



Computing Spreads

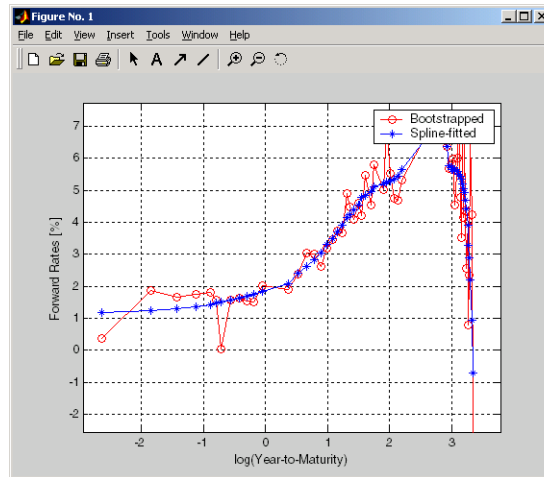
Calculating the spread between specific, fixed forward periods (such as the Treasury-Eurodollar spread) requires an extra step. Interpolate the zero rates (or zero prices, instead) for the corresponding maturities on the interval dates. Then use the interpolated zero rates to deduce the forward rates, and thus the spread of Eurodollar forward curve segments versus the relevant forward segments from Treasury bills.

Additionally, the variety of curve functions (including zero2fwd) helps to standardize such calculations. For instance, by making both rates quoted with quarterly compounding and on an actual/360 basis, the resulting spread structure is fully comparable. This avoids the small inconsistency that occurs when directly comparing the bond-equivalent yield of a Treasury bill to the quarterly forward rates implied by Eurodollar futures.

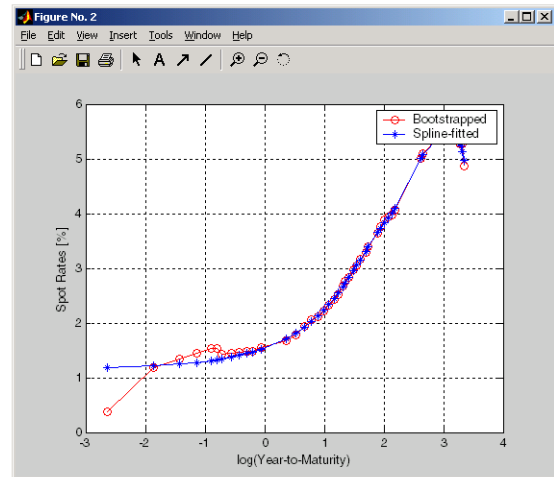
Noise in Curve Computations

When introducing more bonds in constructing curves, noise may become a factor and may need some "smoothing" (with splines, for example); this helps obtain a smoother forward curve.

The following spot and forward curves are constructed from 67 Treasury bonds. The fitted and bootstrapped spot curve (bottom right figure) displays comparable stability. The forward curve (upper left figure) contains significant noise and shows an improbable forward rate structure. The noise is not necessarily bad; it could uncover trading opportunities for a relative-value approach. Yet, a more balanced approach is desired when the bootstrapped forward curve oscillates this much and contains a negative rate as large as -10% (not shown in the plot because it is outside the limits).



Implied Forward Curves.
The jagged curve comes from direct bootstrapping.
The smooth curve shows the effect of smoothing with splines.



Implied Spot Rate Curves.
These curves correspond to the forward curve above.

This example uses `termfit`, a demonstration function from Financial Toolbox that also requires the use of Spline Toolbox.

Derivative Securities

Pricing and Hedging (p. 4-2)	Describes the pricing of Eurodollar-based swaps and portfolio hedging
Convertible Bond Valuation (p. 4-10)	Illustrates a binomial or trinomial tree approach to value convertible bonds
Treasury Bond Futures (p. 4-12)	Describes the computation of Treasury futures conversion factors and theoretical Treasury futures prices

Pricing and Hedging

- “Swap Pricing Assumptions” on page 4-2
- “Swap Pricing Example” on page 4-3
- “Portfolio Hedging” on page 4-8

Swap Pricing Assumptions

Fixed-Income Toolbox contains the function `liborfloat2fixed`, which computes a fixed-rate par yield that equates the floating-rate side of a swap to the fixed-rate side. The solver sets the present value of the fixed side to the present value of the floating side without having to line up and compare fixed and floating periods.

Assumptions on Floating-Rate Input

- Rates are quarterly, for example, that of Eurodollar futures.
- Effective date is the first third Wednesday after the settlement date.
- All delivery dates are spaced three months apart.
- All periods start on the third Wednesday of delivery months.
- All periods end on the same dates of delivery months, three months after the start dates.
- Accrual basis of floating rates is actual/360.
- Applicable forward rates are estimated by interpolation in months when forward-rate data is not available.

Assumptions on Fixed-Rate Output

- Design allows you to create a bond of any coupon, basis, or frequency, based upon the floating-rate input.
- The start date is a valuation date, that is, a date when an agreement to enter into a contract by the settlement date is made.
- Settlement can be on or after the start date. If it is after, a forward fixed-rate contract results.

- Effective date is assumed to be the first third Wednesday after settlement, the same date as that of the floating rate.
- The end date of the bond is a designated number of years away, on the same day and month as the effective date.
- Coupon payments occur on anniversary dates. The frequency is determined by the period of the bond.
- Fixed rates are not interpolated. A fixed-rate bond of the same present value as that of the floating-rate payments is created.

Swap Pricing Example

This example demonstrates the use of the functions in computing the fixed rate applicable to a series of 2-, 5-, and 10-year swaps based on Eurodollar market data. According to the Chicago Mercantile Exchange (<http://www.cme.com>), Eurodollar data on Friday, October 11, 2002, was as shown in the following table.

Note This example illustrates swap calculations in MATLAB. Timing of the data set used was not rigorously examined and was assumed to be the proxy for the swap rate reported on October 11, 2002.

Eurodollar Data on Friday, October 11, 2002

Month	Year	Settle
10	2002	98.21
11	2002	98.26
12	2002	98.3
1	2003	98.3
2	2003	98.31
3	2003	98.275
6	2003	98.12
9	2003	97.87
12	2003	97.575

Eurodollar Data on Friday, October 11, 2002 (Continued)

Month	Year	Settle
3	2004	97.26
6	2004	96.98
9	2004	96.745
12	2004	96.515
3	2005	96.33
6	2005	96.135
9	2005	95.955
12	2005	95.78
3	2006	95.63
6	2006	95.465
9	2006	95.315
12	2006	95.16
3	2007	95.025
6	2007	94.88
9	2007	94.74
12	2007	94.595
3	2008	94.48
6	2008	94.375
9	2008	94.28
12	2008	94.185
3	2009	94.1
6	2009	94.005
9	2009	93.925
12	2009	93.865
3	2010	93.82

Eurodollar Data on Friday, October 11, 2002 (Continued)

Month	Year	Settle
6	2010	93.755
9	2010	93.7
12	2010	93.645
3	2011	93.61
6	2011	93.56
9	2011	93.515
12	2011	93.47
3	2012	93.445
6	2012	93.41
9	2012	93.39

Using this data, you can compute 1-, 2-, 3-, 4-, 5-, 7-, and 10-year swap rates with the toolbox function `liborfloat2fixed`. The function requires you to input only Eurodollar data, the settlement date, and tenor of the swap. MATLAB then performs the required computations.

To illustrate how this function works, first load the data contained in the supplied Excel worksheet `EDdata.xls`.

```
[EDRawData, textdata] = xlsread('EDdata.xls');
```

Extract the month from the first column and the year from the second column. The rate used as proxy is the arithmetic average of rates on opening and closing.

```
Month = EDRawData(:,1);
Year = EDRawData(:,2);
IMMData = (EDRawData(:,4)+EDRawData(:,6))/2;
EDFutData = [Month, Year, IMMData];
```

Next, input the current date.

```
Settle = datenum('11-Oct-2002');
```

To compute for the two-year swap rate, set the tenor to 2.

```
Tenor = 2;
```

Finally, compute the swap rate with `liborfloat2fixed`.

```
[FixedSpec, ForwardDates, ForwardRates] = ...  
liborfloat2fixed(EDFutData, Settle, Tenor)
```

MATLAB returns a par-swap rate of 2.23% using the default setting (quarterly compounding and 30/360 accrual), and forward dates and rates data (quarterly compounded), comparable to 2.17% of Friday's average broker data in Table H15 of *Federal Reserve Statistical Release* (<http://www.federalreserve.gov/releases/h15/update/>).

```
FixedSpec =  
  
    Coupon: 0.0223  
    Settle: '16-Oct-2002'  
    Maturity: '16-Oct-2004'  
    Period: 4  
    Basis: 1
```

```
ForwardDates =  
  
    731505  
    731596  
    731687  
    731778  
    731869  
    731967  
    732058  
    732149
```

```
ForwardRates =  
  
    0.0178  
    0.0168  
    0.0171
```

```

0.0189
0.0216
0.0250
0.0280
0.0306

```

In the `FixedSpec` output, note that the swap rate actually goes forward from the third Wednesday of October 2002 (October 16, 2002), five days after the original `Settle` input (October 11, 2002). This, however, is still the best proxy for the swap rate on `Settle`, as the assumption merely starts the swap's effective period and does not affect its valuation method or its length.

The correction suggested by Hull and White improves the result by turning on convexity adjustment as part of the input to `liborfloat2fixed`. (See Hull, J., *Options, Futures, and Other Derivatives*, 4th Edition, Prentice-Hall, 2000.) For a long swap, for example, five years or more, this correction could prove to be substantial.

The adjustment requires additional parameters:

- `StartDate`, which you make the same as `Settle` (the default) by providing an empty matrix `[]` as input.
- `ConvexAdj` to tell `liborfloat2fixed` to perform the adjustment.
- `RateParam`, which provides the parameters `a` and `S` as input to the Hull-White short rate process.
- Optional parameters `InArrears` and `Sigma`, for which you can use empty matrices `[]` to accept the MATLAB defaults.
- `FixedCompound`, with which you can facilitate comparison with values cited in Table H15 of *Federal Reserve Statistical Release* by turning the default quarterly compounding into semiannual compounding, with the (default) basis of 30/360.

```

StartDate = [];
Interpolation = [];
ConvexAdj = 1;
RateParam = [0.03; 0.017];
FixedCompound = 2;
[FixedSpec, ForwardDaates, ForwardRates] = ...

```

```
liborfloat2fixed(EDFutData, Settle, Tenor, StartDate, ...
Interpolation, ConvexAdj, RateParam, [], [], FixedCompound)
```

This returns 2.21% as the two-year swap rate, quite close to the reported swap rate for that date.

Analogously, the following table summarizes the solutions for 1-, 3-, 5-, 7-, and 10-year swap rates (convexity-adjusted and unadjusted).

Calculated and Market Average Data of Swap Rates on Friday, October 11, 2002

Swap Length (Years)	Unadjusted	Adjusted	Table H15	Adjusted Error (Basis Points)
1	1.80%	1.79%	1.80%	-1
2	2.24%	2.21%	2.22%	-1
3	2.70%	2.66%	2.66%	0
4	3.12%	3.03%	3.04%	-1
5	3.50%	3.37%	3.36%	+1
7	4.16%	3.92%	3.89%	+3
10	4.87%	4.42%	4.39%	+3

Portfolio Hedging

You can use these results further, such as for hedging a portfolio. The `liborduration` function provides a duration-hedging capability. You can isolate assets (or liabilities) from interest-rate risk exposure with a swap arrangement.

Suppose you own a bond with these characteristics:

- \$100 million face value
- 7% coupon paid semiannually

- 5% yield to maturity
- Settlement on October 11, 2002
- Maturity on January 15, 2010
- Interest accruing on an actual/365 basis

Use of the `bnddury` function from Financial Toolbox shows a modified duration of 5.6806 years.

To immunize this asset, you can enter into a pay-fixed swap, specifically a swap in the amount of notional principal (Ns) such that $Ns * SwapDuration + \$100M * 5.6806 = 0$ (or $Ns = -100 * 5.6806 / SwapDuration$).

Suppose again, you choose to employ a 5-, 7-, or 10-year swap (3.37%, 3.92%, and 4.42% from the previous table) as your hedging tool.

```
SwapFixRate = [0.0337; 0.0392; 0.0442];
Tenor = [5; 7; 10];
Settle = '11-Oct-2002';
PayFixDuration = liborduration(SwapFixRate, Tenor, Settle)
```

This gives a duration of -3.6835, -4.7307, and -6.0661 years for 5-, 7-, and 10-year swaps. The corresponding notional amount is computed by

```
Ns = -100*5.6806./PayFixDuration
```

```
Ns =
```

```
154.2163
120.0786
93.6443
```

The notional amount entered in pay-fixed side of the swap instantaneously immunizes the portfolio.

Convertible Bond Valuation

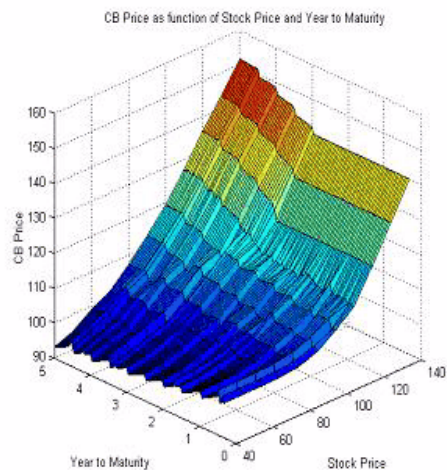
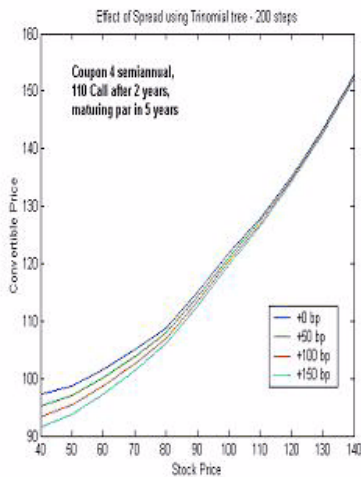
A convertible bond (CB) is a debt instrument that can be converted into a predetermined amount of a company's equity at certain times before the bond's maturity.

Fixed-Income Toolbox uses a binomial and trinomial tree approach (cbprice) to value convertible bonds. The value of a convertible bond is determined by the uncertainty of the related stock. Once the stock evolution is modeled, backward discounting is computed.

The last column of such trees provides the data to decide which is more profitable: the debt notional (plus interest, if any) or the equivalent number of shares per the notional.

Where debt prevails, the toolbox discounts backward with the risk-free rate plus the spread reflecting the credit risk of the issuer. Where stock prevails, the toolbox discounts with the risk-free rate. The intrinsic value of a convertible bond is the sum of the (probability-adjusted) debt and stock portions from the last node. This is compared with current stock price, to see if voluntary or forced conversion may take place. Otherwise, its value is the intrinsic value. From here, the same discounting process is repeated after adjusting debt portion to be equal to 0 if any conversion takes place. Dividends and coupons are handled discretely, at the date they occur.

The approach is equivalent to solving a one-dimensional partial differential equation such as one described by Tsiveriotis and Fernandes. (See Tsiveriotis, K. and C. Fernandes (1998), "Valuing Convertible Bonds with Credit Risk," *The Journal of Fixed Income*, 8 (3), 95-102.) Using the same example of bond specifications that they use (4% annual coupon, payable twice a year, callable after two years at 110, and redeemable at par in five years), the toolbox gives results like theirs.



The figure on the left shows the bond "floor" of the convertible (a 5% yield, given a 4% coupon at about 97% par) when share prices are low.

The change of curvature located at the end of the second year is due to the activation of the embedded (soft) call feature (visible on the surface plot in the right figure).

Finally, there is the flat section when time is nearing expiration and share prices are high, indicating a delta of unity, a characteristic of in-the-money equity options embedded in a bond.

Treasury Bond Futures

Fixed-Income Toolbox also provides new functions that compute Treasury futures conversion factors and theoretical Treasury futures prices.

- “Theoretical Prices” on page 4-12
- “Implied Repo” on page 4-15
- “Hedge Parameters” on page 4-16

Theoretical Prices

This example shows how you can provide an input of eligible bonds and obtain its conversion factor to a 6% coupon rate (or against any other desired coupon rate). The example assumes no knowledge of the repo rate and instead uses the spot curve as the funding rate (`tfutbyprice` and `tfutbyyield`).

```
RefDate = [datenum('1-Dec-2002');
           datenum('1-Mar-2003');
           datenum('1-Jun-2003');
           datenum('1-Sep-2003');
           datenum('1-Dec-2003');
           datenum('1-Sep-2003');
           datenum('1-Dec-2002');
           datenum('1-Jun-2003')];

Maturity = [datenum('15-Nov-2012');
            datenum('15-Aug-2012');
            datenum('15-Feb-2012');
            datenum('15-Feb-2011');
            datenum('15-Aug-2011');
            datenum('15-Aug-2010');
            datenum('15-Aug-2009');
            datenum('15-Feb-2010')];

CouponRate = [0.04; 0.04375; 0.04875; 0.05;
              0.05; 0.0575; 0.06; 0.065];

CF = convfactor(RefDate, Maturity, CouponRate)
```

CF =

0.8539
 0.8858
 0.9259
 0.9418
 0.9403
 0.9862
 1.0000
 1.0266

The results can be checked against the Chicago Board of Trade
 (<http://www.cbot.com>) 10-year futures contract table.

Coupon	Issue Date	Maturity Date	6% Conversion Factors						
			Jun-03	Sep-03	Dec-03	Mar-04			
	Dec-02	Mar-03							
4.00	11/15/02	11/15/12	0.8539	0.8568	0.8595	0.8625	0.8653	0.8683	
4 3/8	08/15/02	08/15/12	0.8836	0.8858	0.8883	0.8905	0.893	0.8954	
4 7/8	02/15/02	02/15/12	0.9226	0.9242	0.9259	0.9275	0.9293	0.931	
5	02/15/01	02/15/11	0.9372	0.9386	0.9403	0.9418	0.9435	0.9451	
5	08/15/01	08/15/11	0.9342	0.9356	0.9372	0.9386	0.9403	0.9418	
5 1/2	05/17/99	05/15/09	---	---	---	---	---	---	
5 3/4	08/15/00	08/15/10	0.9851	0.9854	0.9859	0.9862	0.9867	---	
6	08/16/99	08/15/09	1	---	---	---	---	---	
6 1/2	02/15/00	02/15/10	1.0282	1.0273	1.0266	---	---	---	

This computation can be incorporated into other functions that use conversion factors, such as routines to find the cheapest-to-deliver bonds. This is also equivalent to calculating the theoretical price of a particular set of bond futures prices.

A Treasury spot curve is necessary to discount the issue properly. MATLAB takes into account the actual/actual accrual basis and any intermittent

coupons between the settlement and delivery dates. You can generate the spot curve using any set of Treasury bonds as long as the bonds cover the entire life of the futures in question.

```
% Computing the reference spot curve.
Bonds = [datenum('02/13/2003'), 0;
         datenum('05/15/2003'), 0;
         datenum('10/31/2004'), 0.02125;
         datenum('11/15/2007'), 0.03;
         datenum('11/15/2012'), 0.04;
         datenum('02/15/2031'), 0.05375];

Yields = [1.20; 1.25; 1.86; 2.99; 4.02; 4.93] / 100;

Settle = datenum('11/15/2002');

[ZeroRates, CurveDates] = ...
    zbyield(Bonds, Yields, Settle);

% Computing theoretical futures T-bonds price.
SpotCurve = [CurveDates, ZeroRates];
RefDate = [datenum('1-Dec-2002'); datenum('1-Mar-2003')];
MatFut = [datenum('15-Dec-2002'); datenum('15-Mar-2003')];
Maturity = [datenum('15-Aug-2009'); datenum('15-Aug-2010')];
CouponRate = [0.06; 0.0575];
CF = convfactor(RefDate, Maturity, CouponRate);
Price = [114.416; 113.171];
Interpolation = 1;

QtdFutPrice = tfutbyprice(SpotCurve, Price, Settle, ...
    MatFut, CF, CouponRate, Maturity, Interpolation)

QtdFutPrice =

    113.8129
    112.4986
```

These quoted prices for December 2002 and March 2003 are comparable with futures prices of 113.93 and 112.68 traded that same hour at the Chicago Board of Trade. Without a live data feed, the data timings are asynchronous,

but the results compare favorably for illustration purposes. These methods are well documented (such as in Hull 2000) and require some assumptions about the intended delivery date. Because of the short-term maturities on most bond futures, no convexity adjustment is usually needed.

When you know the repo rate, you can calculate theoretical prices with `tfutpricebyrepo` or `tfutyieldbyrepo`. Effectively, the known repo rate substitutes for the segment of the spot curve between the settlement and delivery dates.

Implied Repo

Alternatively, you can calculate the cheapest-to-deliver (CTD) bonds by comparing the repo rates implied by bond current and future prices. A higher-cost bond, obviously, is not a candidate for the CTD bond, and vice versa.

Within a low-yield environment, you would like to compare implied repos on two bonds on the extremes of a deliverable three-month contract for 10-year Treasury bonds. You expect that the CTD bond has a higher coupon and shorter maturity, and that this bond implies lower funding cost.

For example, two bonds on the extremes are a 6.5% coupon maturing February 15, 2010, and a 3.875% coupon maturing February 15, 2013. You would expect the 6.5% to be significantly cheaper to deliver as implied by its lower funding rate. The price of the 6.5% is 118.439, and price of the 3.875% is 99.601.

Quoted futures price for June 2003 is 113.9219 (113-295). Today is March 27, 2003, and you intend to deliver on June 27, 2003 (92 days repo). There are no coupons to reinvest during this period.

The code that provides this information to the toolbox `tfutimrepo` function is

```
ReinvestData = [0.025  3];
Price = [118.300;
        99.601];
QtdFutPrice = [113.9219;
              113.9219];
Settle = datenum('03/27/2003');
MatFut = [datenum('27-Jun-2003');
```

```
        datenum('27-Jun-2003')]);  
CF = [1.0266;  
      0.8478];  
CouponRate = [0.06500;  
              0.03875];  
Maturity = [datenum('15-Feb-2010');  
            datenum('15-Feb-2013')];  
ImpliedRepo = tfutimprepo(ReinvestData, Price, QtdFutPrice, ...  
                          Settle, MatFut, CF, CouponRate, Maturity)  
  
ImpliedRepo =  
  
        0.0100  
       -0.0795
```

This result confirms that the CTD bond is indeed the 6.5% February 2010 bond, as it has the higher implied repo (ignoring transaction cost) before arbitrage can occur. The implied repo in MATLAB is always returned on an actual/360 accrual basis.

Remember that this data is likely to be asynchronous and is useful for illustration purpose only.

Hedge Parameters

Treasury futures hedge parameters are frequently measured with DV01, the dollar value when there is a one-basis-point shift. This is easily calculated by computing the duration of the underlying bond for the contract (the CTD bond), dividing it by its conversion factor, and multiplying it by its cash price. Use `bnddurp` and `bnddury` from Financial Toolbox to compute modified durations of fixed-coupon bonds. Again, the facility provided by the Treasury bond futures functions easily leverages such tasks and lets you focus on more qualitative assessment of your routines.

Functions — By Category

Cash Flows (p. 5-2)	Work with cash flows for bond portfolios
Certificates of Deposit (p. 5-2)	Work with certificates of deposit
Convertible Bonds (p. 5-3)	Work with convertible bonds
Derivative Securities (p. 5-3)	Work with derivative securities
Mortgage-Backed Securities (p. 5-4)	Work with mortgage-backed securities
Option-Adjusted Spread Computations (p. 5-5)	Work with option-adjusted spread computations
Stepped-Coupon Bonds (p. 5-6)	Work with stepped-coupon bonds
Treasury Bills (p. 5-7)	Work with Treasury bills
Treasury Bond Futures (p. 5-8)	Work with treasury bond futures
Zero-Coupon Instruments (p. 5-9)	Work with zero-coupon instruments

Cash Flows

cfamounts

Cash flow and time mapping for
bond portfolio

Certificates of Deposit

cdai

Accrued interest on certificate of
deposit (CD)

cdprice

Price certificate of deposit (CD)

cdyield

Yield on certificate of deposit (CD)

Convertible Bonds

cbprice	Price convertible bond
---------	------------------------

Derivative Securities

bkcall	Price European call option on bonds using Black's model
bkcaplet	Price interest rate caplet using Black's model
bkfloorlet	Price interest rate floorlet using Black's model
bkput	Price European put option on bonds using Black's model
liborduration	Duration of LIBOR-based interest rate swap
liborfloat2fixed	Compute par fixed-rate of swap given 3-month LIBOR data
liborprice	Price swap given swap rate

Mortgage-Backed Securities

mbscfamounts	Cash flow and time mapping for mortgage pool
mbsconvp	Convexity of mortgage pool given price
mbsconvy	Convexity of mortgage pool given yield
mbsdurp	Duration of mortgage pool given price
mbsdury	Duration of mortgage pool given yield
mbsnoprepay	End-of-month mortgage cash flows and balances without prepayment
mbspassthrough	Mortgage pool cash flows and balances with prepayment
mbsprice	Mortgage-backed security price given yield
mbsprice2speed	Implied PSA prepayment speeds given price
mbswal	Weighted average life of mortgage pool
mbsyield	Mortgage-backed security yield given price
mbsyield2speed	Implied PSA prepayment speeds given yield
psaspeed2default	Benchmark default
psaspeed2rate	Single monthly mortality rate given PSA speed

Option-Adjusted Spread Computations

mbssoas2price

Price given option-adjusted spread

mbssoas2yield

Yield given option-adjusted spread

mbsprice2oas

Option-adjusted spread given price

mbsyield2oas

Option-adjusted spread given yield

Stepped-Coupon Bonds

stepcpncfamounts

Cash flow amounts and times for
bonds and stepped coupons

stepcpnprice

Price bond with stepped coupons

stepcpnyield

Yield to maturity of bond with
stepped coupons

Treasury Bills

tbilldisc2yield	Convert Treasury bill discount to equivalent yield
tbillprice	Price Treasury bill
tbillrepo	Break-even discount of repurchase agreement
tbillval01	Value of one basis point
tbillyield	Yield on Treasury bill
tbillyield2disc	Convert Treasury bill yield to equivalent discount

Treasury Bond Futures

convfactor	Treasury bond conversion factors
tfutbyprice	Future prices of Treasury bonds given spot price
tfutbyyield	Future prices of Treasury bonds given current yield
tfutimprepo	Implied simple annual repurchase rate to prevent arbitrage
tfutpricebyrepo	Theoretical futures bond price
tfutyieldbyrepo	Theoretical futures bond yield

Zero-Coupon Instruments

zeroprice

Price zero-coupon instruments given
yield

zeroyield

Yield of zero-coupon instruments
given price

Functions — Alphabetical List

bkcall

Purpose Price European call option on bonds using Black's model

Syntax `CallPrice = bkcall(Strike, ZeroData, Sigma, BondData, Settle, Expiry, Period, Basis, EndMonthRule, InterpMethod, StrikeConvention)`

Arguments

Strike	Scalar or number of options (NOPT) by 1 vector of strike prices.
ZeroData	Two-column (optionally three-column) matrix containing zero (spot) rate information used to discount future cash flows. First column: Serial maturity date associated with the zero rate in the second column. Second column: Annualized zero rates, in decimal form, appropriate for discounting cash flows occurring on the date specified in the first column. All dates must occur after <code>Settle</code> (dates must correspond to future investment horizons) and must be in ascending order. Third column (optional): Annual compounding frequency. Values are 1 (annual), 2 (semiannual, default), 3 (three times per year), 4 (quarterly), 6 (bimonthly), 12 (monthly), and -1 (continuous).
Sigma	Scalar or NOPT- by-1 vector of annualized price volatilities required by Black's model.

BondData	<p data-bbox="756 260 1335 390">Row vector with three (optionally four) columns or NOPT-by-3 (optionally NOPT-by-4) matrix specifying characteristics of underlying bonds in the form:</p> <pre data-bbox="756 425 1305 460">[CleanPrice CouponRate Maturity Face]</pre> <p data-bbox="756 486 1305 546">CleanPrice is the price excluding accrued interest.</p> <p data-bbox="756 581 1246 616">CouponRate is the decimal coupon rate.</p> <p data-bbox="756 651 1246 711">Maturity is the bond maturity date in serial date number format.</p> <p data-bbox="756 746 1276 841">Face is the face value of the bond. If unspecified, the face value is assumed to be 100.</p>
Settle	<p data-bbox="756 859 1335 980">Settlement date of the options. May be a serial date number or date string. Settle also represents the starting reference date for the input zero curve.</p>
Expiry	<p data-bbox="756 998 1335 1093">Scalar or NOPT-by-1 vector of option maturity dates. May be a serial date number or date string.</p>
Period	<p data-bbox="756 1111 1335 1206">(Optional) Number of coupons per year for the underlying bond. Default = 2 (semiannual). Supported values are 0, 1, 2, 3, 4, 6, and 12.</p>

Basis	<p>(Optional) Day-count basis of the bond. A vector of integers.</p> <ul style="list-style-type: none">• 0 = actual/actual (default)• 1 = 30/360 (SIA)• 2 = actual/360• 3 = actual/365• 4 = 30/360 (PSA)• 5 = 30/360 (ISDA)• 6 = 30/360 (European)• 7 = actual/365 (Japanese)• 8 = actual/actual (ISMA)• 9 = actual/360 (ISMA)• 10 = actual/365 (ISMA)
EndMonthRule	<p>(Optional) End-of-month rule. This rule applies only when Maturity is an end-of-month date for a month having 30 or fewer days. 0 = ignore rule, meaning that a bond's coupon payment date is always the same numerical day of the month. 1 = set rule on (default), meaning that a bond's coupon payment date is always the last actual day of the month.</p>

InterpMethod	(Optional) Scalar integer zero curve interpolation method. For cash flows that do not fall on a date found in the ZeroData spot curve, indicates the method used to interpolate the appropriate zero discount rate. Available methods are (0) nearest, (1) linear, and (2) cubic. Default = 1. See interp1 for more information.
StrikeConvention	<p>(Optional) Scalar or NOPT-by-1 vector of option contract strike price conventions.</p> <p>StrikeConvention = 0 (default) defines the strike price as the cash (dirty) price paid for the underlying bond.</p> <p>StrikeConvention = 1 defines the strike price as the quoted (clean) price paid for the underlying bond. The accrued interest of the bond at option expiration is added to the input strike price when evaluating Black's model.</p>

Description

CallPrice = bkcall(Strike, ZeroData, Sigma, BondData, Settle, Expiry, Period, Basis, EndMonthRule, InterpMethod, StrikeConvention) using Black's model, derives an NOPT-by-1 vector of prices of European call options on bonds.

If cash flows occur beyond the dates spanned by ZeroData, the input zero curve, the appropriate zero rate for discounting such cash flows is obtained by extrapolating the nearest rate on the curve (that is, if a cash flow occurs before the first or after the last date on the input zero curve, a flat curve is assumed).

Examples

This example is based on example 22.1, page 512, of Hull. (See References below.)

Consider a European call option on a bond maturing in 9.75 years. The underlying bond has a clean price of \$935, a face value of \$1000, and

pays 10% semiannual coupons. Since the bond matures in 9.75 years, a \$50 coupon will be paid in three months and again in nine months. Also, assume that the annualized volatility of the forward bond price is 9%. Furthermore, suppose the option expires in 10 months and has a strike price of \$1000, and that the annualized continuously compounded risk-free discount rates for maturities of 3, 9, and 10 months are 9%, 9.5%, and 10%, respectively.

```
% Specify the option information.
Settle      = '15-Mar-2004';
Expiry      = '15-Jan-2005'; % 10 months from settlement
Strike      = 1000;
Sigma       = 0.09;
Convention  = [0 1]';

% Specify the interest rate environment.
ZeroData    = [datenum('15-Jun-2004') 0.09 -1; % 3 months
               datenum('15-Dec-2004') 0.095 -1; % 9 months
               datenum(Expiry)        0.10 -1]; % 10 months

% Specify the bond information.
CleanPrice  = 935;
CouponRate  = 0.1;
Maturity    = '15-Dec-2013'; % 9.75 years from settlement
Face        = 1000;
BondData    = [CleanPrice CouponRate datenum(Maturity) Face];
Period      = 2;
Basis       = 1;

% Call Black's model.
CallPrices = bkcall(Strike, ZeroData, Sigma, BondData, Settle,...
Expiry, Period, Basis, [], [], Convention)

CallPrices =

    9.4873
    7.9686
```


When the strike price is the dirty price (Convention = 0), the call option value is \$9.49. When the strike price is the clean price (Convention = 1), the call option value is \$7.97.

References

[1] Hull, John C., *Options, Futures, and Other Derivatives*, Prentice Hall, 5th edition, 2003, pp. 287-288, 508-515.

See Also

bkput

bkcaplet

Purpose Price interest rate caplet using Black's model

Syntax `CapPrices = bkcaplet(CapData, FwdRates, ZeroPrice, Settle, StartDate, EndDate, Sigma)`

Arguments

CapData	Number of caps (NCAP) by 2 matrix containing cap rates and bases: [CapRates Basis] Values for bases may be: <ul style="list-style-type: none">• 0 = actual/actual (default)• 1 = 30/360 (SIA)• 2 = actual/360• 3 = actual/365• 4 = 30/360 (PSA)• 5 = 30/360 (ISDA)• 6 = 30/360 (European)• 7 = actual/365 (Japanese)• 8 = actual/actual (ISMA)• 9 = actual/360 (ISMA)• 10 = actual/365 (ISMA)
FwdRates	Scalar or NCAP-by-1 vector containing forward rates in decimal. FwdRates accrue on the same basis as CapRates.
ZeroPrice	Scalar or NCAP-by-1 vector containing zero coupon prices with maturities corresponding to those of each cap in CapData, per \$100 nominal value.

Settle	Scalar or NCAP-by-1 vector of identical elements containing settlement date of caplets.
StartDate	Scalar or NCAP-by-1 vector containing start dates of the caplets.
EndDate	Scalar or NCAP-by-1 vector containing maturity dates of caplets.
Sigma	Scalar or NCAP-by-1 vector containing volatility of forward rates in decimal, corresponding to each caplet.

Description

CapPrices = bkcaplet(CapData, FwdRates, ZeroPrice, Settle, StartDate, EndDate, Sigma) computes the prices of interest rate caplets for every \$100 face value of principal.

Examples

Given a notional amount of \$1,000,000, compute the value of a caplet on October 15, 2002 that starts on October 15, 2003 and ends on January 15, 2004.

```
CapData = [0.08, 1];
FwdRates = 0.07;
ZeroPrice = 100*exp(-0.065*1.25);
Settle = datenum('15-Oct-2002');
BeginDates = datenum('15-Oct-2003');
EndDates = datenum('15-Jan-2004');
Sigma = 0.20;
```

Because the caplet is \$100 notional, divide \$1,000,000 by \$100.

```
Notional = 1000000/100;

CapPrice = Notional*bkcaplet(CapData, FwdRates, ZeroPrice, ...
Settle, BeginDates, EndDates, Sigma)

CapPrice =

    519.0046
```

bkcaplet

See Also

[bkfloorlet](#)

Purpose

Price interest rate floorlet using Black's model

Syntax

FloorPrices = bkfloorlet(FloorData, FwdRates, ZeroPrice, Settle, StartDate, EndDate, Sigma)

Arguments

- FloorData Number of floors (NFLR) by 2 matrix containing floor rates and bases:
[FloorRate Basis]
Values for bases may be:
- 0 = actual/actual (default)
 - 1 = 30/360 (SIA)
 - 2 = actual/360
 - 3 = actual/365
 - 4 = 30/360 (PSA)
 - 5 = 30/360 (ISDA)
 - 6 = 30/360 (European)
 - 7 = actual/365 (Japanese)
 - 8 = actual/actual (ISMA)
 - 9 = actual/360 (ISMA)
 - 10 = actual/365 (ISMA)
- FwdRates Scalar or NFLR-by-1 vector containing forward rates in decimal. FwdRates accrue on the same basis as FloorRates.
- ZeroPrice Scalar or NFLR-by-1 vector containing zero coupon prices with maturities corresponding to those of each floor in FloorData, per \$100 nominal value.

Settle	Scalar or NFLR-by-1 vector of identical elements containing settlement date of floorlets.
StartDate	Scalar or NFLR-by-1 vector containing start dates of the floorlets.
EndDate	Scalar or NFLR-by-1 vector containing maturity dates of floorlets.
Sigma	Scalar or NFLR-by-1 vector containing volatility of forward rates in decimal, corresponding to each floorlet.

Description

FloorPrices = bkfloorlet(FloorData, FwdRates, ZeroPrice, Settle, StartDate, EndDate, Sigma) computes the prices of interest rate floorlets for every \$100 of notional value.

Examples

Given a notional amount of \$1,000,000, compute the value of a floorlet on October 15, 2002 that starts on October 15, 2003 and ends on January 15, 2004.

```
FloorData = [0.08, 1];
FwdRates = 0.07;
ZeroPrice = 100*exp(-0.065*1.25);
Settle = datenum('15-Oct-2002');
BeginDates = datenum('15-Oct-2003');
EndDates = datenum('15-Jan-2004');
Sigma = 0.20;

% Because floorlet is $100 notional, divide $1,000,000 by $100.
Notional = 1000000/100;

FloorPrice = Notional*bkfloorlet(FloorData, FwdRates, ...
ZeroPrice, Settle, BeginDates, EndDates, Sigma)

FloorPrice =

    2823.91
```

See Also

bkcaplet

bkput

Purpose Price European put option on bonds using Black's model

Syntax PutPrice = bkput(Strike, ZeroData, Sigma, BondData, Settle, Expiry, Period, Basis, EndMonthRule, InterpMethod, StrikeConvention)

Arguments

Strike	Scalar or number of options (NOPT) by 1 vector of strike prices.
ZeroData	Two-column (optionally three-column) matrix containing zero (spot) rate information used to discount future cash flows. First column: Serial maturity date associated with the zero rate in the second column. Second column: Annualized zero rates, in decimal form, appropriate for discounting cash flows occurring on the date specified in the first column. All dates must occur after Settle (dates must correspond to future investment horizons) and must be in ascending order. Third column (optional): Annual compounding frequency. Values are 1 (annual), 2 (semiannual, default), 3 (three times per year), 4 (quarterly), 6 (bimonthly), 12 (monthly), and -1 (continuous).
Sigma	Scalar or NOPT- by-1 vector of annualized price volatilities required by Black's model.

BondData	<p>Row vector with three (optionally four) columns or NOPT-by-3 (optionally NOPT-by-4) matrix specifying characteristics of underlying bonds in the form:</p> <pre>[CleanPrice CouponRate Maturity Face]</pre> <p>CleanPrice is the price excluding accrued interest. CouponRate is the decimal coupon rate. Maturity is the bond maturity date in serial date number format. Face is the face value of the bond. If unspecified, the face value is assumed to be 100.</p>
Settle	<p>Settlement date of the options. May be a serial date number or date string. Settle also represents the starting reference date for the input zero curve.</p>
Expiry	<p>Scalar or NOPT-by-1 vector of option maturity dates. May be a serial date number or date string.</p>
Period	<p>(Optional) Number of coupons per year for the underlying bond. Default = 2 (semiannual). Supported values are 0, 1, 2, 3, 4, 6, and 12.</p>
Basis	<p>(Optional) Day-count basis of the bond. A vector of integers.</p> <ul style="list-style-type: none">• 0 = actual/actual (default)• 1 = 30/360 (SIA)• 2 = actual/360• 3 = actual/365• 4 = 30/360 (PSA)• 5 = 30/360 (ISDA)• 6 = 30/360 (European)

- 7 = actual/365 (Japanese)
- 8 = actual/actual (ISMA)
- 9 = actual/360 (ISMA)
- 10 = actual/365 (ISMA)

EndMonthRule (Optional) End-of-month rule. This rule applies only when **Maturity** is an end-of-month date for a month having 30 or fewer days. 0 = ignore rule, meaning that a bond's coupon payment date is always the same numerical day of the month. 1 = set rule on (default), meaning that a bond's coupon payment date is always the last actual day of the month.

InterpMethod (Optional) Scalar integer zero curve interpolation method. For cash flows that do not fall on a date found in the **ZeroData** spot curve, indicates the method used to interpolate the appropriate zero discount rate. Available methods are (0) nearest, (1) linear, and (2) cubic. Default = 1. See **interp1** for more information.

StrikeConvention (Optional) Scalar or NOPT-by-1 vector of option contract strike price conventions.

StrikeConvention = 0 (default) defines the strike price as the cash (dirty) price paid for the underlying bond.

StrikeConvention = 1 defines the strike price as the quoted (clean) price paid for the underlying bond. The accrued interest of the bond at option expiration is added to the input strike price when evaluating Black's model.

Description

PutPrice = bkput(Strike, ZeroData, Sigma, BondData, Settle, Expiry, Period, Basis, EndMonthRule, InterpMethod, StrikeConvention) using Black's model, derives an NOPT-by-1 vector of prices of European put options on bonds.

If cash flows occur beyond the dates spanned by ZeroData, the input zero curve, the appropriate zero rate for discounting such cash flows is obtained by extrapolating the nearest rate on the curve (that is, if a cash flow occurs before the first or after the last date on the input zero curve, a flat curve is assumed).

Examples

This example is based on example 22.2, page 514, of Hull. (See References below.)

Consider a European put option on a bond maturing in 10 years. The underlying bond has a clean price of \$122.82, a face value of \$100, and pays 8% semi-annual coupons. Also, assume that the annualized volatility of the forward bond yield is 20%. Furthermore, suppose the option expires in 2.25 years and has a strike price of \$115, and that the annualized continuously compounded risk free zero (spot) curve is flat at 5%. For a hypothetical settlement date of March 15, 2004, the following code illustrates the use of Black's model to duplicate the put prices in Example 22.2 of the Hull reference. In particular, it illustrates how to convert a broker's yield volatility to a price volatility suitable for Black's model.

```
% Specify the option information.
Settle      = '15-Mar-2004';
Expiry      = '15-Jun-2006'; % 2.25 years from settlement
Strike      = 115;
YieldSigma  = 0.2;
Convention  = [0; 1];

% Specify the interest rate environment. Since the
% zero curve is flat, interpolation into the curve always returns
% 0.05. Thus, the following curve is not unique to the solution.
ZeroData    = [datenum('15-Jun-2004') 0.05  -1;
               datenum('15-Dec-2004') 0.05  -1;
```

```
        datenum(Expiry)      0.05  -1];

% Specify the bond information.
CleanPrice = 122.82;
CouponRate = 0.08;
Maturity   = '15-Mar-2014'; % 10 years from settlement
Face       = 100;
BondData   = [CleanPrice CouponRate datenum(Maturity) Face];
Period     = 2; % semiannual coupons
Basis      = 1; % 30/360 day-count basis

% Convert a broker's yield volatility quote to a price volatility
% required by Black's model. To duplicate Example 22.2 in Hull,
% first compute the periodic (semiannual) yield to maturity from
% the clean bond price.
Yield = bndyield(CleanPrice, CouponRate, Settle, Maturity,...
Period, Basis);

% Compute the duration of the bond at option expiration. Most
% fixed-income sensitivity analyses use the modified duration
% statistic to examine the impact of small changes in periodic
% yields on bond prices. However, Hull's example operates in
% continuous time (annualized instantaneous volatilities and
% continuously compounded zero yields for discounting coupons).
% To duplicate Hull's results, use the second output of BNDDURY,
% the Macaulay duration.
[Modified, Macaulay] = bnddury(Yield, CouponRate, Expiry,...
Maturity, Period, Basis);

% Convert the yield-to-maturity from a periodic to a
% continuous yield.
Yield = Period .* log(1 + Yield./Period);

% Finally, convert the yield volatility to a price volatility via
% Hull's Equation 22.6 (page 514).
PriceSigma = Macaulay .* Yield .* YieldSigma;
```

```
% Finally, call Black's model.  
PutPrices = bkput(Strike, ZeroData, PriceSigma, BondData,...  
Settle, Expiry, Period, Basis, [], [], Convention)  
PutPrices =  
  
1.7838  
2.4071
```

When the strike price is the dirty price (`Convention = 0`), the call option value is \$1.78. When the strike price is the clean price (`Convention = 1`), the call option value is \$2.41.

References

[1] Hull, John C., *Options, Futures, and Other Derivatives*, Prentice Hall, 5th edition, 2003, pp. 287-288, 508-515.

See Also

bkcall

cbprice

Purpose Price convertible bond

Syntax [CBMatrix, UndMatrix, DebtMatrix, EqtyMatrix] =
cbprice(RiskFreeRate, StaticSpread, Sigma, Price, ConvRatio,
NumSteps, IssueDate, Settle, Maturity, CouponRate, Period, Basis,
EndMonthRule, DividendType, DividendInfo, CallType, CallInfo,
TreeType)

Arguments

RiskFreeRate	Annual yield of risk-free bond with the same maturity as the convertible, compounded continuously. (Recommended value is the yield of a risk-free bond with the same maturity as the convertible.)
StaticSpread	Value of constant spread to the risk free rate. Adding this to the RiskFreeRate produces the issuer's yield, which reflects its credit risk.
Sigma	Annual volatility in decimal.
Price	Price of asset at settlement or valuation date.
ConvRatio	Scalar. Number of assets convertible to a single bond.
NumSteps	Number of steps in binomial tree.
IssueDate	Issue date of bond.
Settle	Settlement date of bond.
Maturity	Maturity date of bond.
CouponRate	Coupon rate payable per unit of face value.
Period	(Optional) Coupons per year of the bond. A vector of integers. Allowed values are 0, 1, 2, 3, 4, 6, and 12. Default = 2.

Basis	<p>(Optional) Scalar value for day-count basis of the instrument.</p> <ul style="list-style-type: none"> • 0 = actual/actual (default) • 1 = 30/360 (SIA) • 2 = actual/360 • 3 = actual/365 • 4 = 30/360 (PSA) • 5 = 30/360 (ISDA) • 6 = 30/360 (European) • 7 = actual/365 (Japanese) • 8 = actual/actual (ISMA) • 9 = actual/360 (ISMA) • 10 = actual/365 (ISMA)
EndMonthRule	<p>(Optional) End-of-month rule. This rule applies only when Maturity is an end-of-month date for a month having 30 or fewer days. 0 = ignore rule, meaning that a bond's coupon payment date is always the same numerical day of the month. 1 = set rule on (default), meaning that a bond's coupon payment date is always the last actual day of the month.</p>
DividendType	<p>(Optional). 0 = dollar dividend (default). 1 = dividend yield.</p>
DividendInfo	<p>(Optional) Two-column matrix of dividend information. First column contains the ex-dividend date corresponding to the amount in the second column. Default = no dividend.</p>

CallType	0 = call on cash price (default). 1 = call on clean price.
CallInfo	(Optional) Two-column matrix of call information. First column contains the call dates. Second column contains call prices for every \$100 face of bond. A call in the amount of call prices is activated <i>after</i> the corresponding call date. Default = no call feature.
TreeType	(Optional) 0 = binomial tree (default). 1 = trinomial tree.

All inputs are scalars except for DividendInfo and CallInfo.

Description

[CBMatrix, UndMatrix, DebtMatrix, EqtyMatrix] = cbprice(RiskFreeRate, StaticSpread, Sigma, Price, ConvRatio, NumSteps, IssueDate, Settle, Maturity, CouponRate, Period, Basis, EndMonthRule, DividendType, DividendInfo, CallType, CallInfo, TreeType) computes the price of a convertible bond using a Cox-Ross-Rubinstein binomial tree or, optionally, a trinomial tree.

CBMatrix is a matrix of convertible bond prices.

UndMatrix is a matrix of stock prices in binomial format.

DebtMatrix is a matrix of the debt portion of the convertible bond.

EqtyMatrix is a matrix of the equity portion of the convertible bond.

Examples

Perform a spread effect analysis of a 4%-coupon convertible bond callable at 110 at end of second year, maturing at par in five years, with yield to maturity of 5% and spread (of YTM versus 5-year treasury) of 0, 50, 100, and 150 basis points. The underlying stock pays no dividend.

```
RiskFreeRate = 0.05;  
Sigma        = 0.3;  
ConvRatio    = 1;  
NumSteps     = 200;
```



```

IssueDate    = datenum('2-Jan-2002');
Settle       = datenum('2-Jan-2002');
Maturity     = datenum('2-Jan-2007');
CouponRate   = 0.04;
Period       = 2;
Basis        = 1;
EndMonthRule = 1;
DividendType = 0;
DividendInfo = [];
CallInfo     = [datenum('2-Jan-2004'), 110];
CallType     = 1;
TreeType     = 1;

% Nested loop accross prices and static spread dimensions
% to compute convertible prices.

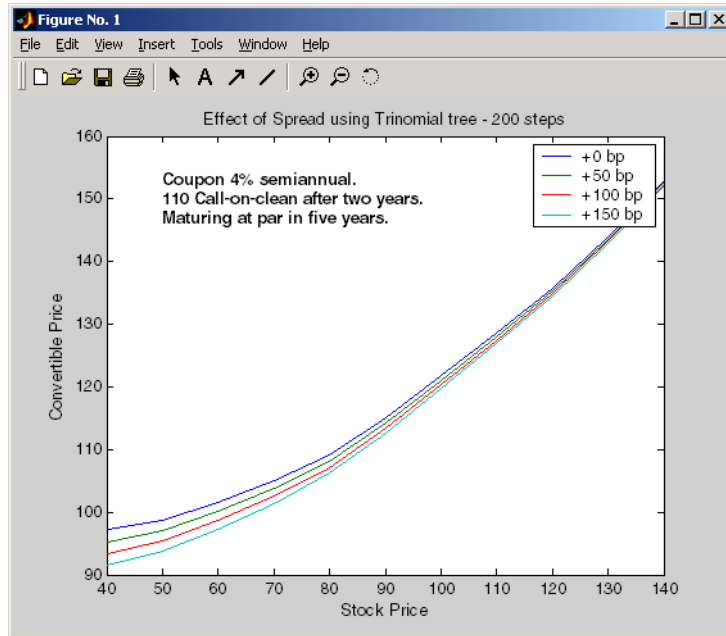
for j = 0:0.005:0.015;
    StaticSpread = j;
    for i = 0:10:100
        Price = 40+i;
        [CbMatrix, UndMatrix, DebtMatrix, EqtyMatrix] = ...
            cbprice(RiskFreeRate, StaticSpread, Sigma, Price, ...
                ConvRatio, NumSteps, IssueDate, Settle, ...
                Maturity, CouponRate, Period, Basis, EndMonthRule, ...
                DividendType, DividendInfo, CallType, CallInfo, ...
                TreeType);

        convprice(i/10+1, j*200+1) = CbMatrix(1,1);
        stock(i/10+1, j*200+1)     = Price;
    end
end

plot(stock, convprice);
legend({'+0 bp'; '+50 bp'; '+100 bp'; '+150 bp'});
title ('Effect of Spread using Trinomial tree - 200 steps')
xlabel('Stock Price');
ylabel('Convertible Price');

```

```
text(50, 150, ['Coupon 4% semiannual.', sprintf('\n'), ...  
             '110 Call-on-clean after two years.' sprintf('\n'), ...  
             'Maturing at par in five years.'],'fontweight','Bold')
```



Purpose Accrued interest on certificate of deposit (CD)

Syntax `AccrInt = cdai(CouponRate, Settle, Maturity, IssueDate, Basis)`

Arguments

CouponRate	Annual interest rate in decimal.
Settle	Settlement date. Settle must be earlier than or equal to Maturity.
Maturity	Maturity date.
IssueDate	Issue date.
Basis	(Optional) Day-count basis of the instrument.

- 0 = actual/actual (default)
- 1 = 30/360 (SIA)
- 2 = actual/360
- 3 = actual/365
- 4 = 30/360 (PSA)
- 5 = 30/360 (ISDA)
- 6 = 30/360 (European)
- 7 = actual/365 (Japanese)
- 8 = actual/actual (ISMA)
- 9 = actual/360 (ISMA)
- 10 = actual/365 (ISMA)

Each required input must be some certificates of deposit (NCDS) by 1 or 1-by-NCDS conforming vector or scalar. The optional Basis argument may be either a NCDS-by-1 or a 1-by-NCDS vector, a scalar, or the empty matrix ([]).

Description

`AccrInt = cdai(CouponRate, Settle, Maturity, IssueDate, Basis)` computes the accrued interest on a certificate of deposit.

`AccrInt` represents the accrued interest per \$100 of face value.

This function assumes that the certificates of deposit pay interest at maturity. Because of the simple interest treatment of these securities, the function is best used for short term maturities (less than one year). The default simple interest calculation is the actual/360 convention (SIA).

Examples

Given a certificate of deposit (CD) with these characteristics, compute the accrued interest due on the CD.

```
CouponRate    = 0.05;
Settle         = '02-Jan-02';
Maturity       = '31-Mar-02';
IssueDate      = '1-Oct-01';
```

```
AccrInt = cdai(CouponRate, Settle, Maturity, IssueDate)
```

```
AccrInt =
    1.2917
```

See Also

`accfrac`, `bdyield`, `stepcpnyield`, `tbillyield`, `zeroyield`

Purpose Price certificate of deposit (CD)

Syntax [Price, AccrInt] = cdprice(Yield, CouponRate, Settle, Maturity, IssueDate, Basis)

Arguments

Yield	Simple yield to maturity over the basis denominator.
CouponRate	Coupon interest rate in decimal.
Settle	Settlement date. Settle must be earlier than or equal to Maturity.
Maturity	Maturity date.
IssueDate	Issue date.
Basis	(Optional) Day-count basis of the instrument. <ul style="list-style-type: none">• 0 = actual/actual (default)• 1 = 30/360 (SIA)• 2 = actual/360• 3 = actual/365• 4 = 30/360 (PSA)• 5 = 30/360 (ISDA)• 6 = 30/360 (European)• 7 = actual/365 (Japanese)• 8 = actual/actual (ISMA)• 9 = actual/360 (ISMA)• 10 = actual/365 (ISMA)

Each required input must be some certificates of deposit (NCDS) by 1 or 1-by-NCDS conforming vector or scalar. The optional Basis argument

cdprice

may be either a NCDS-by-1 or a 1-by-NCDS vector, a scalar, or the empty matrix ([]).

Description

[Price, AccrInt] = cdprice(Yield, CouponRate, Settle, Maturity, IssueDate, Basis) computes the price of a certificate of deposit given its yield.

Price is the clean price of the CD per \$100 of face value.

AccruedInt is the accrued interest payable at settlement per unit of face value.

This function assumes that the certificates of deposit pay interest at maturity. Because of the simple interest treatment of these securities, the function is best used for short term maturities (less than one year). The default simple interest calculation is the actual/360 convention.

Examples

Given a certificate of deposit (CD) with these characteristics, compute the price of the CD and the accrued interest due on the settlement date.

```
Yield          = 0.0525;
CouponRate     = 0.05;
Settle         = '02-Jan-02';
Maturity       = '31-Mar-02';
IssueDate      = '1-Oct-01';
```

```
[Price, AccruedInt] = cdprice(Yield, CouponRate, Settle, ...
Maturity, IssueDate)
```

```
Price =
```

```
99.9233
```

```
AccruedInt =
```

```
1.2917
```

See Also

bndprice, cdai, cdyield, stepcpnprice, tbillprice

Purpose

Yield on certificate of deposit (CD)

Syntax

Yield = cdyield(Price, CouponRate, Settle, Maturity, IssueDate, Basis)

Arguments

Price	Clean price of the certificate of deposit per \$100 face. If you have a vector of dirty or cash prices of CDs, compute the accrued interest portion using <code>cdai</code> .
CouponRate	Annual interest rate in decimal.
Settle	Settlement date. <code>Settle</code> must be earlier than or equal to <code>Maturity</code> .
Maturity	Maturity date.
IssueDate	Issue date.
Basis	(Optional) Day-count basis of the instrument. <ul style="list-style-type: none"> • 0 = actual/actual (default) • 1 = 30/360 (SIA) • 2 = actual/360 • 3 = actual/365 • 4 = 30/360 (PSA) • 5 = 30/360 (ISDA) • 6 = 30/360 (European) • 7 = actual/365 (Japanese) • 8 = actual/actual (ISMA) • 9 = actual/360 (ISMA) • 10 = actual/365 (ISMA)

cdyield

Each required input must be some certificates of deposit (NCDS) by 1 or 1-by-NCDS conforming vector or scalar. The optional Basis argument may be either a NCDS-by-1 or a 1-by-NCDS vector, a scalar, or the empty matrix ([]).

Description

Yield = cdyield(Price, CouponRate, Settle, Maturity, IssueDate, Basis) computes the yield to maturity of a certificate of deposit given its clean price.

This function assumes that the certificates of deposit pay interest at maturity. Because of the simple interest treatment of these securities, the function is best used for short term maturities (less than one year). The default simple interest calculation is the actual/360 convention.

Examples

Given a certificate of deposit (CD) with these characteristics, compute the yield on the CD.

```
Price      = 101.125;
CouponRate = 0.05;
Settle     = '02-Jan-02';
Maturity   = '31-Mar-02';
IssueDate  = '1-Oct-01';

Yield = cdyield(Price, CouponRate, Settle, Maturity, IssueDate)

Yield =

    0.0039
```

See Also

bndprice, cdai, cdprice, stepcpnprice, tbillprice

Purpose

Cash flow and time mapping for bond portfolio

Syntax

```
[CFlowAmounts, CFlowDates, TFactors, CFlowFlags] =  
cfamounts(CouponRate, Settle, Maturity, Period, Basis,  
EndMonthRule, IssueDate, FirstCouponDate, LastCouponDate,  
StartDate, Face)
```

Arguments

CouponRate	Decimal number indicating the annual percentage rate used to determine the coupons payable on a bond.
Settle	Settlement date. A vector of serial date numbers or date strings. Settle must be earlier than or equal to Maturity.
Maturity	Maturity date. A vector of serial date numbers or date strings.
Period	(Optional) Coupons per year of the bond. A vector of integers. Allowed values are 0, 1, 2, 3, 4, 6, and 12. Default = 2.
Basis	(Optional) Day-count basis of the bond. A vector of integers. A scalar. <ul style="list-style-type: none">• 0 = actual/actual (default)• 1 = 30/360 (SIA)• 2 = actual/360• 3 = actual/365• 4 = 30/360 (PSA)• 5 = 30/360 (ISDA)• 6 = 30/360 (European)• 7 = actual/365 (Japanese)

- 8 = actual/actual (ISMA)
- 9 = actual/360 (ISMA)
- 10 = actual/365 (ISMA)

EndMonthRule	(Optional) End-of-month rule. A vector. This rule applies only when Maturity is an end-of-month date for a month having 30 or fewer days. 0 = ignore rule, meaning that a bond's coupon payment date is always the same numerical day of the month. 1 = set rule on (default), meaning that a bond's coupon payment date is always the last actual day of the month.
IssueDate	(Optional) Date when a bond was issued.
FirstCouponDate	(Optional) Date when a bond makes its first coupon payment. When FirstCouponDate and LastCouponDate are both specified, FirstCouponDate takes precedence in determining the coupon payment structure.
LastCouponDate	(Optional) Last coupon date of a bond prior to the maturity date. In the absence of a specified FirstCouponDate, a specified LastCouponDate determines the coupon structure of the bond. The coupon structure of a bond is truncated at the LastCouponDate regardless of where it falls and will be followed only by the bond's maturity cash flow date.

StartDate	(Reserved input argument, currently unused; optional) Date when a bond actually starts (the date from which a bond's cash flows can be considered). To make an instrument forward starting, specify this date as a future date. If StartDate is not explicitly specified, the effective start date is the settlement date.
Face	(Optional) Face or par value. Default = 100.

Required arguments must be number of bonds (NUMBONDS) by 1 or 1-by-NUMBONDS conforming vectors or scalars. Optional arguments must be either NUMBONDS-by-1 or 1-by-NUMBONDS conforming vectors, scalars, or empty matrices.

Description

`[CFlowAmounts, CFlowDates, TFactors, CFlowFlags] = cfamounts(CouponRate, Settle, Maturity, Period, Basis, EndMonthRule, IssueDate, FirstCouponDate, LastCouponDate, StartDate, Face)` returns matrices of cash flow amounts, cash flow dates, time factors, and cash flow flags for a portfolio of NUMBONDS fixed income securities. The elements contained in the cash flow matrix, time factor matrix, and cash flow flag matrix correspond to the cash flow dates for each security. The first element of each row in the cash flow matrix is the accrued interest payable on each bond. This is zero in the case of all zero coupon bonds. This function determines all cash flows and time mappings for a bond whether the coupon structure contains odd first or last periods. All output matrices are padded with NaNs as necessary to ensure that all rows have the same number of elements.

`CFlowAmounts` is the cash flow matrix of a portfolio of bonds. Each row represents the cash flow vector of a single bond. Each element in a column represents a specific cash flow for that bond.

`CFlowDates` is the cash flow date matrix of a portfolio of bonds. Each row represents a single bond in the portfolio. Each element in a column represents a cash flow date of that bond.

TFactors is the matrix of time factors for a portfolio of bonds. Each row corresponds to the vector of time factors for each bond. Each element in a column corresponds to the specific time factor associated with each cash flow of a bond. Time factors are useful in determining the present value of a stream of cash flows. The term "time factor" refers to the exponent TF in the discounting equation

$$PV = CF / (1 + z/2)^{TF}$$

where:

- PV = Present value of a cash flow
- CF = The cash flow amount
- z = The risk-adjusted annualized rate or yield corresponding to given cash flow. The yield is quoted on a semiannual basis.
- TF = Time factor for a given cash flow. Time is measured in semiannual periods from the settlement date to the cash flow date. In computing time factors, we use SIA actual/actual day count conventions for all time factor calculations.

CFlowFlags is the matrix of cash flow flags for a portfolio of bonds. Each row corresponds to the vector of cash flow flags for each bond. Each element in a column corresponds to the specific flag associated with each cash flow of a bond. Flags identify the type of each cash flow (for example, nominal coupon cash flow, front or end partial or "stub" coupon, maturity cash flow). Possible values are shown in the table.

Flag	Cash Flow Type
0	Accrued interest due on a bond at settlement.
1	Initial cash flow amount smaller than normal due to "stub" coupon period. A stub period is created when the time from issue date to first coupon is shorter than normal.

Flag	Cash Flow Type
2	Larger than normal initial cash flow amount because first coupon period is longer than normal.
3	Nominal coupon cash flow amount.
4	Normal maturity cash flow amount (face value plus the nominal coupon amount).
5	End "stub" coupon amount (last coupon period abnormally short and actual maturity cash flow is smaller than normal).
6	Larger than normal maturity cash flow because last coupon period longer than normal.
7	Maturity cash flow on a coupon bond when the bond has less than one coupon period to maturity.
8	Smaller than normal maturity cash flow when bond has less than one coupon period to maturity.
9	Larger than normal maturity cash flow when bond has less than one coupon period to maturity.
10	Maturity cash flow on a zero coupon bond.

Examples

Consider a portfolio containing a corporate bond paying interest quarterly and a treasury bond paying interest semiannually. Compute the cash flow structure and the time factors for each bond.

```
Settle = '01-Nov-1993';
Maturity = ['15-Dec-1994'; '15-Jun-1995'];
CouponRate = [0.06; 0.05];
Period = [4; 2];
Basis = [1; 0];
[CFlowAmounts, CFlowDates, TFactors, CFlowFlags] = ...
cfamounts(CouponRate, Settle, Maturity, Period, Basis)

CFlowAmounts =
```

cfamounts

```
-0.7667  1.5000  1.5000  1.5000  1.5000 101.5000  
-1.8989  2.5000  2.5000  2.5000 102.5000      NaN
```

CFlowDates =

```
728234  728278  728368  728460  728552  728643  
728234  728278  728460  728643  728825      NaN
```

TFactors =

```
0  0.2404  0.7403  1.2404  1.7403  2.2404  
0  0.2404  1.2404  2.2404  3.2404      NaN
```

CFlowFlags =

```
0  3  3  3  3  4  
0  3  3  3  4  NaN
```

See Also

accrfrac, cfdates, cpncount, cpndaten, cpndatenq, cpndatep,
cpndatepq, cpndaysn, cpndaysp, cnpersz

Purpose Treasury bond conversion factors

Syntax ConvFactor = convfactor(RefDate, Maturity, CouponRate, RefYield, Convention)

Arguments

RefDate	Reference dates, for which conversion factor is computed (usually the first day of delivery months).
Maturity	Maturity date of underlying bond.
CouponRate	Annual coupon rate of underlying bond in decimal.
RefYield	(Optional) Reference semiannual yield. Default = 0.06 (6%).
Convention	(Optional) Conversion factor convention. Scalar. Valid values are: 1 = U. S. Treasury bond (20-year) and Treasury note (10-year) futures contract (default). 2 = U. S. 2-year and 5-year Treasury note futures contract.

Description ConvFactor = convfactor(RefDate, Maturity, CouponRate, RefYield, Convention) computes conversion factors based upon a reference 6% semiannual yield.

Note You can verify the output of this function by comparing the output against the quotations provided by the Chicago Board of Trade (<http://www.cbot.com>).

Examples

```
RefDate = [datenum('1-Dec-2002');  
           datenum('1-Mar-2003');
```

convfactor

```
        datenum('1-Jun-2003');
        datenum('1-Sep-2003');
        datenum('1-Dec-2003');
        datenum('1-Sep-2003');
        datenum('1-Dec-2002');
        datenum('1-Jun-2003')];

Maturity = [datenum('15-Nov-2012');
            datenum('15-Aug-2012');
            datenum('15-Feb-2012');
            datenum('15-Feb-2011');
            datenum('15-Aug-2011');
            datenum('15-Aug-2010');
            datenum('15-Aug-2009');
            datenum('15-Feb-2010')];

CouponRate = [0.04; 0.04375; 0.04875; 0.05;
              0.05; 0.0575; 0.06; 0.065];

ConvFactor = convfactor(RefDate, Maturity, CouponRate)

ConvFactor =

    0.8539
    0.8858
    0.9259
    0.9418
    0.9403
    0.9862
    1.0000
    1.0266
```

See Also

tfutbyprice, tfutbyyield

Purpose Duration of LIBOR-based interest rate swap

Syntax `[PayFixDuration GetFixDuration] = liborduration(SwapFixRate, Tenor, Settle)`

Arguments

<code>SwapFixRate</code>	Scalar or column vector of swap fixed rates in decimal.
<code>Tenor</code>	Scalar or column vector indicating life of the swap in years. Fractional numbers are rounded upward.
<code>Settle</code>	Scalar or column vector of settlement dates.

Description `[PayFixDuration GetFixDuration] = liborduration(SwapFixRate, Tenor, Settle)` computes the duration of LIBOR-based interest rate swaps.

`PayFixDuration` is the modified duration, in years, realized when entering pay-fix side of the swap.

`GetFixDuration` is the modified duration, in years, realized when entering receive-fix side of the swap.

Examples Given the data

```
SwapFixRate = 0.0383;  
Tenor = 7;  
Settle = datenum('11-Oct-2002');
```

compute the swap durations.

```
[PayFixDuration GetFixDuration] = liborduration(SwapFixRate,...  
Tenor, Settle)
```

```
PayFixDuration =
```

liborduration

-4.7567

GetFixDuration =

4.7567

See Also

liborfloat2fixed, liborprice

Purpose

Compute par fixed-rate of swap given 3-month LIBOR data

Syntax

```
[FixedSpec, ForwardDates, ForwardRates] =  
liborfloat2fixed(ThreeMonthRates, Settle, Tenor, StartDate,  
Interpolation, ConvexAdj, RateParam, InArrears, Sigma,  
FixedCompound, FixedBasis)
```

Arguments

ThreeMonthRates	Three-month Eurodollar futures data or forward rate agreement data. (A forward rate agreement stipulates that a certain interest rate applies to a certain principal amount for a given future time period.) An n-by-3 matrix in the form of [month year IMMQuote]. The floating rate is assumed to compound quarterly and to accrue on an actual/360 basis.
Settle	Settlement date of swap. Scalar.
Tenor	Life of the swap. Scalar.
StartDate	(Optional) Scalar value to denote reference date for valuation of (forward) swap. This in effect allows forward swap valuation. Default = Settle.
Interpolation	(Optional) Interpolation method to determine applicable forward rate for months when no Eurodollar data is available. Default is 'linear' or 1. Other possible values are 'Nearest' or 0, and 'Cubic' or 2.
ConvexAdj	(Optional) Default = 0 (off). 1 = on. Denotes whether futures/forward convexity adjustment is required. Pertains to forward rate adjustments when those rates are taken from Eurodollar futures data.

liborfloat2fixed

RateParam	(Optional) Short-rate model's parameters (Hull-White) [a S], where the short-rate process is $dr = [\theta(t) - ar]dt + Sdz$ Default = [0.05 0.015].
InArrears	(Optional) Default = 0 (off). Set to 1 for on. If on, the routine does an automatic a convexity adjustment to forward rates.
Sigma	(Optional) Overall annual volatility of caplets.
FixedCompound	(Optional) Scalar value. Compounding or frequency of payment on the fixed side. Also, the reset frequency. Default = 4 (quarterly). Other values are 1, 2, and 12.
FixedBasis	(Optional). Scalar value. Basis of the fixed side. 0 = actual/actual, 1 = 30/360 (SIA, default), 2 = actual/360, 3 = actual/365, 4 = 30/360 (PSA), 5 = 30/360 (ISDA), 6 = 30/360 (European), 7 = act/365 (Japanese).

Description

[FixedSpec, ForwardDates, ForwardRates] =
liborfloat2fixed(ThreeMonthRates, Settle, Tenor, StartDate,
Interpolation, ConvexAdj, RateParam, InArrears, Sigma,
FixedCompound, FixedBasis computes forward rates, dates, and
the swap fixed rate.

FixedSpec specifies the structure of the fixed-rate side of the swap:

- Coupon: Par-swap rate
- Settle: Start date
- Maturity: End date
- Period: Frequency of payment
- Basis: Accrual basis

ForwardDates are dates corresponding to ForwardRates (all third Wednesdays of the month, spread three months apart). The first element is the third Wednesday immediately after Settle.

ForwardRates are forward rates corresponding to the forward dates, quarterly compounded, and on the actual/360 basis.

Note To preserve input integrity, Tenor is rounded upward to the closest integer. Currently traded tenors are 2, 5, and 10 years.

The function assumes that floating-rate observations occur quarterly on the third Wednesday of a delivery month. The first delivery month is the month of the first third Wednesday after Settle. Floating-side payments occur on the third-month anniversaries of observation dates.

Examples

Use the supplied EDdata.xls file as input to a liborfloat2fixed computation.

```
[EDFutData, textdata] = xlsread('EDdata.xls');
Settle                 = datenum('15-Oct-2002');
Tenor                  = 2;
```

```
[FixedSpec, ForwardDates, ForwardRates] = ...
liborfloat2fixed(EDFutData, Settle, Tenor)
```

```
FixedSpec =
```

```
    Coupon: 0.0222
    Settle: '16-Oct-2002'
    Maturity: '16-Oct-2004'
    Period: 4
    Basis: 1
```

```
ForwardDates =
```

liborfloat2fixed

731505
731596
731687
731778
731869
731967
732058
732149

ForwardRates =

0.0177
0.0166
0.0170
0.0188
0.0214
0.0248
0.0279
0.0305

See Also `liborduration`, `liborprice`

Purpose Price swap given swap rate

Syntax `Price = liborprice(ThreeMonthRates, Settle, Tenor, SwapRate, StartDate, Interpolation, ConvexAdj, RateParam, InArrears, Sigma, FixedCompound, FixedBasis)`

Arguments

ThreeMonthRates	Three-month Eurodollar futures data or forward rate agreement data. (A forward rate agreement stipulates that a certain interest rate applies to a certain principal amount for a given future time period.) An n-by-3 matrix in the form of [month year IMMQuote]. The floating rate is assumed to compound quarterly and to accrue on an actual/360 basis.
Settle	Settlement date of swap. Scalar.
Tenor	Life of the swap. Scalar.
SwapRate	Swap rate in decimal.
StartDate	(Optional) Scalar value to denote reference date for valuation of (forward) swap. This in effect allows forward swap valuation. Default = Settle.
Interpolation	(Optional) Interpolation method to determine applicable forward rate for months when no Eurodollar data is available. Default is 'linear' or 1. Other possible values are 'Nearest' or 0, and 'Cubic' or 2.
ConvexAdj	(Optional) Default = 0 (off). 1 = on. Denotes whether futures/forward convexity adjustment is required. Pertains to forward rate adjustments when those rates are taken from Eurodollar futures data.

liborprice

RateParam	(Optional) Short-rate model's parameters (Hull-White) [a S], where the short-rate process is $dr = [\theta(t) - ar]dt + Sdz$ Default = [0.05 0.015].
InArrears	(Optional) Default = 0 (off). Set to 1 for on. If on, the routine does an automatic convexity adjustment to forward rates.
Sigma	(Optional) Overall annual volatility of caplets.
FixedCompound	(Optional) Scalar value. Compounding or frequency of payment on the fixed side. Also, the reset frequency. Default = 4 (quarterly). Other values are 1, 2, and 12.
FixedBasis	(Optional). Scalar value. Basis of the fixed side. 0 = actual/actual, 1 = 30/360 (SIA, default), 2 = actual/360, 3 = actual/365, 4 = 30/360 (PSA), 5 = 30/360 (ISDA), 6 = 30/360 (European), 7 = act/365 (Japanese).

Description

Price = liborprice(ThreeMonthRates, Settle, Tenor, SwapRate, StartDate, Interpolation, ConvexAdj, RateParam, InArrears, Sigma, FixedCompound, FixedBasis) computes the price per \$100 notional value of a swap given the swap rate. A positive result indicates that fixed side is more valuable than the floating side.

Price is the present value of the difference between floating and fixed-rate sides of the swap per \$100 notional.

Examples

This example shows that a swap paying the par swap rate has a value of 0.

Load the input data.

```
[EDFutData, textdata] = xlsread('EDdata.xls');  
Settle = datenum('15-Oct-2002');
```



```
Tenor = 2;
```

Compute the fixed rate from the Eurodollar data.

```
FixedSpec = liborfloat2fixed(EDFutData, Settle, Tenor);
```

Compute the price of a par swap.

```
Price = liborprice(EDFutData, Settle, Tenor, FixedSpec.Coupon)
```

```
Price =
```

```
4.1633e-015
```

MATLAB computes a value for Price that is effectively equal to 0.

See Also

`liborduration`, `liborfloat2fixed`

mbscfamounts

Purpose Cash flow and time mapping for mortgage pool

Syntax [CFlowAmounts, CFlowDates, TFactors, Factors] =
mbscfamounts(Settle, Maturity, IssueDate, GrossRate, CouponRate,
Delay, PrepaySpeed, PrepayMatrix)

Arguments

Settle	Settlement date. A serial date number or date string. Settle must be earlier than or equal to Maturity.
Maturity	Maturity date. A serial date number or date string.
IssueDate	Issue date. A serial date number or date string.
GrossRate	Gross coupon rate (including fees), in decimal.
CouponRate	Net coupon rate, in decimal. Default = GrossRate.
Delay	Delay in days.
PrepaySpeed	(Optional) Relation of the conditional payment rate (CPR) to the benchmark model. Default = 0. If you input a customized prepayment matrix, set PrepaySpeed to [] .
PrepayMatrix	(Optional) Used only when PrepayModel and PrepaySpeed are unspecified.) Customized prepayment vector. A NaN-padded matrix of size max(TermRemaining)-by-NMBS. Each column corresponds to each mortgage-backed security, and each row corresponds to each month after settlement.

All inputs (except PrepayMatrix) are number of mortgage-backed securities (NMBS) by 1 vectors.

Description

[CFlowAmounts, CFlowDates, TFactors, Factors] = mbscfamounts(Settle, Maturity, IssueDate, GrossRate, CouponRate, Delay, PrepaySpeed, PrepayMatrix) computes cash flows between settle and maturity dates, the corresponding time factors in months from settle, and the mortgage factor (the fraction of loan principal outstanding).

CFlowAmounts is a vector of cash flows starting from Settle through end of the last month (Maturity).

CFlowDates indicates when cash flows occur, including at Settle. A negative number at Settle indicates accrued interest is due.

TFactors is a vector of times in months from Settle, corresponding to each cash flow.

Factors is a vector of mortgage factors (the fraction of the balance still outstanding at the end of each month).

Examples

Example 1. Given a mortgage with the following characteristics, compute the cash flow amounts and dates, the time factors, and the mortgage factors.

```
Settle      = datenum('17-April-2002');
Maturity    = datenum('1-Jan-2030');
IssueDate   = datenum('1-Jan-2000');
GrossRate   = 0.08125;
CouponRate  = 0.075;
Delay       = 14;
PrepaySpeed = 100;
```

```
[CFlowAmounts, CFlowDates, TFactors, Factors] = ...
mbscfamounts(Settle, Maturity, IssueDate, GrossRate, ...
CouponRate, Delay, PrepaySpeed)
```

The result is contained in four 334-element row vectors.

mbscfamounts

Example 2. Given a portfolio of mortgage-backed securities, use `mbscfamounts` to compute the cash flows and other factors from the portfolio.

```
Settle    = datenum(['13-Jan-2000'; '17-Apr-2002'; '17-May-2002']);
Maturity  = datenum('1-Jan-2030');
IssueDate = datenum('1-Jan-2000');
GrossRate = 0.08125;
CouponRate = [0.075; 0.07875; 0.0775];
Delay     = 14;
PrepaySpeed = 100;

[CFlowAmounts, CFlowDates, TFactors, Factors] = ...
mbscfamounts(Settle, Maturity, IssueDate, GrossRate, ...
CouponRate, Delay, PrepaySpeed)
```

Each output is a 3-by-361 element matrix padded with NaNs wherever elements are missing.

References

[1] *PSA Uniform Practices*, SF-4

Purpose Convexity of mortgage pool given price

Syntax Convexity = mbsconvp(Price, Settle, Maturity, IssueDate, GrossRate, CouponRate, Delay, PrepaySpeed, PrepayMatrix)

Arguments

Price	Clean price for every \$100 face value.
Settle	Settlement date. A serial date number or date string. Settle must be earlier than or equal to Maturity.
Maturity	Maturity date. A serial date number or date string.
IssueDate	Issue date. A serial date number or date string.
GrossRate	Gross coupon rate (including fees), in decimal.
CouponRate	Net coupon rate, in decimal. Default = GrossRate.
Delay	Delay in days.
PrepaySpeed	(Optional) Relation of the conditional payment rate (CPR) to the benchmark model. Default = 0. Set PrepaySpeed to [] if you input a customized prepayment matrix.
PrepayMatrix	(Optional) Used only when PrepayModel and PrepaySpeed are unspecified.) Customized prepayment vector. A NaN-padded matrix of size max(TermRemaining)-by-NMBS. Each column corresponds to each mortgage-backed security, and each row corresponds to each month after settlement.

All inputs (except PrepayMatrix) are number of mortgage-backed securities (NMBS) by 1 vectors.

mbsconvp

Description

Convexity = mbsconvp(Price, Settle, Maturity, IssueDate, GrossRate, CouponRate, Delay, PrepaySpeed, PrepayMatrix) computes mortgage-backed security convexity, given time information, price at settlement, and optionally, a prepayment model.

Note If you specify the PSA or FHA model, it will be seasoned with how long the debt has been outstanding (the loan's age).

Examples

Given a mortgage-backed security with the following characteristics, compute the convexity of the security.

```
Price      = 101;
Settle     = '15-Apr-2002';
Maturity   = '1 Jan 2030';
IssueDate  = '1-Jan-2000';
GrossRate  = 0.08125;
CouponRate = 0.075;
Delay      = 14;
Speed      = 100;

Convexity = mbsconvp(Price, Settle, Maturity, IssueDate,...
GrossRate, CouponRate, Delay, Speed)

Convexity =

    71.6299
```

References

[1] *PSA Uniform Practices*, SF-49

See Also

mbsconvy, mbsdurp, mbsdury

Purpose Convexity of mortgage pool given yield

Syntax Convexity = mbsconvy(Yield, Settle, Maturity, IssueDate, GrossRate, CouponRate, Delay, PrepaySpeed, PrepayMatrix)

Arguments

Yield	Mortgage yield, compounded monthly (in decimal).
Settle	Settlement date. A serial date number or date string. Settle must be earlier than or equal to Maturity.
Maturity	Maturity date. A serial date number or date string.
IssueDate	Issue date. A serial date number or date string.
GrossRate	Gross coupon rate (including fees), in decimal.
CouponRate	Net coupon rate, in decimal. Default = GrossRate.
Delay	Delay in days.
PrepaySpeed	(Optional) Relation of the conditional payment rate (CPR) to the benchmark model. Default = 0. Set PrepaySpeed to [] if you input a customized prepayment matrix.
PrepayMatrix	(Optional) Used only when PrepayModel and PrepaySpeed are unspecified.) Customized prepayment vector. A NaN-padded matrix of size max(TermRemaining)-by-NMBS. Each column corresponds to each mortgage-backed security, and each row corresponds to each month after settlement.

All inputs (except PrepayMatrix) are number of mortgage-backed securities (NMBS) by 1 vectors.

Description Convexity = mbsconvy(Yield, Settle, Maturity, IssueDate, GrossRate, CouponRate, Delay, PrepaySpeed, PrepayMatrix)

computes mortgage-backed security convexity, given time information, semiannual mortgage yield, and optionally, a prepayment model.

Note If you specify the PSA or FHA model, it will be seasoned with how long the debt has been outstanding (the loan's age).

Examples

Given a mortgage-backed security with the following characteristics, compute the convexity of the security.

```
Yield      = 0.07125;
Settle     = '15-Apr-2002';
Maturity   = '1 Jan 2030';
IssueDate  = '1-Jan-2000';
GrossRate  = 0.08125;
Speed      = 100;
CouponRate = 0.075;
Delay      = 14;
```

```
Convexity = mbsconvy(Yield, Settle, Maturity, IssueDate, ...
GrossRate, CouponRate, Delay, Speed)
```

```
Convexity =
```

```
72.8263
```

References

[1] *PSA Uniform Practices*, SF-49

See Also

mbsconvp, mbsdurp, mbsdury

Purpose Duration of mortgage pool given price

Syntax [YearDuration, ModDuration] = mbsdurp(Price, Settle, Maturity, IssueDate, GrossRate, CouponRate, Delay, PrepaySpeed, PrepayMatrix)

Arguments

Price	Clean price for every \$100 face value.
Settle	Settlement date. A serial date number or date string. Settle must be earlier than or equal to Maturity.
Maturity	Maturity date. A serial date number or date string.
IssueDate	Issue date. A serial date number or date string.
GrossRate	Gross coupon rate (including fees), in decimal.
CouponRate	Net coupon rate, in decimal. Default = GrossRate.
Delay	Delay in days.
PrepaySpeed	(Optional) Relation of the conditional payment rate (CPR) to the benchmark model. Default = 0. Set PrepaySpeed to [] if you input a customized prepayment matrix.
PrepayMatrix	(Optional) Used only when PrepayModel and PrepaySpeed are unspecified.) Customized prepayment vector. A NaN-padded matrix of size max(TermRemaining)-by-NMBS. Each column corresponds to each mortgage-backed security, and each row corresponds to each month after settlement.

All inputs (except PrepayMatrix) are number of mortgage-backed securities (NMBS) by 1 vectors.

Description

[YearDuration, ModDuration] = mbsdurp(Price, Settle, Maturity, IssueDate, GrossRate, CouponRate, Delay, PrepaySpeed, PrepayMatrix) computes the mortgage-backed security Macaulay (YearDuration) and modified (ModDuration) durations, given time information, price at settlement, and optionally, a prepayment model.

Note If you specify the PSA or FHA model, it will be seasoned with how long the debt has been outstanding (the loan's age).

Examples

Given a mortgage-backed security with the following characteristics, compute the Macaulay and modified durations of the security.

```
Price = 101;
Settle = datenum('15-Apr-2002');
Maturity = datenum('1 Jan 2030');
IssueDate = datenum('1-Jan-2000');
GrossRate = 0.08125;
CouponRate = 0.075;;
Delay = 14;
Speed = 100;

[YearDuration, ModDuration] = mbsdurp(Price, Settle, Maturity,...
IssueDate, GrossRate, CouponRate, Delay, Speed)

YearDuration =

    6.4380

ModDuration =

    6.2080
```

References

[1] *PSA Uniform Practices*, SF-49

See Also

mbsconvp, mbsconvy, mbsdury

mbsdury

Purpose Duration of mortgage pool given yield

Syntax [YearDuration, ModDuration] = mbsdury(Yield, Settle, Maturity, IssueDate, GrossRate, CouponRate, Delay, PrepaySpeed, PrepayMatrix)

Arguments	Yield	Mortgage yield, compounded monthly, in decimal.
	Settle	Settlement date. A serial date number or date string. Settle must be earlier than or equal to Maturity.
	Maturity	Maturity date. A serial date number or date string.
	IssueDate	Issue date. A serial date number or date string.
	GrossRate	Gross coupon rate (including fees), in decimal.
	CouponRate	Net coupon rate, in decimal. Default = GrossRate.
	Delay	Delay in days.
	PrepaySpeed	(Optional) Relation of the conditional payment rate (CPR) to the benchmark model. Default = 0. Set PrepaySpeed to [] if you input a customized prepayment matrix.
	PrepayMatrix	(Optional) Used only when PrepayModel and PrepaySpeed are unspecified.) Customized prepayment vector. A NaN-padded matrix of size max(TermRemaining)-by-NMBS. Each column corresponds to each mortgage-backed security, and each row corresponds to each month after settlement.

All inputs (except PrepayMatrix) are number of mortgage-backed securities (NMBS) by 1 vectors.

Description

[YearDuration, ModDuration] = mbsdury(Yield, Settle, Maturity, IssueDate, GrossRate, CouponRate, Delay, PrepayModel, PrepaySpeed, PrepayMatrix) computes the mortgage-backed security Macaulay (YearDuration) and Modified (ModDuration) durations, given time information, yield to maturity, and optionally, a prepayment model.

Note If you specify the PSA or FHA model, it will be seasoned with how long the debt has been outstanding (the loan's age).

Examples

Given a mortgage-backed security with the following characteristics, compute the Macaulay and Modified durations of the security.

```
Yield = 0.07298413;
Settle = '15-Apr-2002';
Maturity = '1 Jan 2030';
IssueDate = '1-Jan-2000';
GrossRate = 0.08125;
Speed = 100;
CouponRate = 0.075;
Delay = 14;
```

```
[YearDuration, ModDuration] = mbsdury(Yield, Settle, Maturity,...
IssueDate, GrossRate, CouponRate, Delay, Speed)
```

```
YearDuration =
```

```
6.4380
```

```
ModDuration =
```

```
6.2080
```

mbsdury

References [1] *PSA Uniform Practices*, SF-49

See Also mbsconvp, mbsconvy, mbsdurp

Purpose End-of-month mortgage cash flows and balances without prepayment

Syntax [Balance, Interest, Payment, Principal] =
mbsnoprepay(OriginalBalance, GrossRate, Term)

Arguments

OriginalBalance	Original face value in dollars.
GrossRate	Gross coupon rate (including fees), in decimal.
Term	Term of the mortgage in months.

All inputs are number of mortgage-backed securities (NMBS) by 1 vectors.

Description [Balance, Interest, Payment, Principal] =
mbsnoprepay(OriginalBalance, GrossRate, Term) computes
end-of-month mortgage balance, interest payments, principal payments,
and cash flow payments with zero prepayment rate.

The function returns amortizing cash flows and balances over a specified term with no prepayment. When the lengths of passthroughs are not the same, MATLAB pads the shorter ones with NaN.

Balance lists the end-of-month balances over the life of the passthrough.

Interest lists all end-of-month interest payments over the life of the passthrough.

Payment lists all end-of-month payments over the life of the passthrough.

Principal lists all scheduled end-of-month principal payments over the life of the passthrough.

All outputs are Term-by-1 vectors.

Examples Given mortgage pools with the following characteristics, compute an amortization schedule.

```
OriginalBalance = 400000000;
```

mbsnoprepay

```
CouponRate = 0.08125;  
Term = [357; 355]; % Three- and five-month old mortgage pools.  
  
[Balance, Interest, Payment, Principal] = ...  
mbsnoprepay(OriginalBalance, CouponRate, Term);
```


Purpose	Price given option-adjusted spread	
Syntax	Price = mbsoas2price(ZeroCurve, OAS, Settle, Maturity, IssueDate, GrossRate, CouponRate, Delay, Interpolation, PrepaySpeed, PrepayMatrix)	
Arguments	ZeroCurve	A matrix of three columns: Column 1: Serial date numbers. Column 2: Spot rates with maturities corresponding to the dates in Column 1, in decimal (for example, 0.075). Column 3: Compounding of the rates in Column 2. (This is the agency spot rate on the settlement date.)
	OAS	Option-adjusted spreads in basis points.
	Settle	Settlement date (scalar only). A serial date number or date string. Date when option-adjusted spread is calculated.
	Maturity	Maturity date. Scalar or vector in serial date number or date string format.
	IssueDate	Issue date. A serial date number or date string.
	GrossRate	Gross coupon rate (including fees), in decimal.
	CouponRate	(Optional) Net coupon rate, in decimal. Default = GrossRate.
	Delay	(Optional) Delay (in days) between payment from homeowner and receipt by bondholder. Default = 0 (no delay between payment and receipt).

mbsoas2price

- Interpolation** Interpolation method. Computes the corresponding spot rates for the bond's cash flow. Available methods are (0) nearest, (1) linear, and (2) cubic spline. Default = 1. See `interp1` for more information.
- PrepaySpeed** (Optional) Relation of the conditional payment rate (CPR) to the benchmark model. Default = end of month's CPR. Set `PrepaySpeed` to [] if you input a customized prepayment matrix.
- PrepayMatrix** (Optional) Customized prepayment matrix. A matrix of size `max(TermRemaining)`-by-NMBS. Missing values are padded with NaNs. Each column corresponds to a mortgage-backed security, and each row corresponds to each month after settlement.

All inputs (except `PrepayMatrix`) are number of mortgage-backed securities (NMBS) by 1 vectors.

Description

`Price = mbsoas2price(ZeroCurve, OAS, Settle, Maturity, IssueDate, GrossRate, CouponRate, Delay, Interpolation, PrepaySpeed, PrepayMatrix)` computes the clean price of a passthrough security for each \$100 face value of outstanding principal.

Examples

Given an option-adjusted spread, a spot curve, and a prepayment assumption, compute theoretical price of a mortgage pool.

Create the bonds matrix.

```
Bonds = [datenum('11/21/2002') 0      100 0 2 1;  
         datenum('02/20/2003') 0      100 0 2 1;  
         datenum('07/31/2004') 0.03   100 2 3 1;  
         datenum('08/15/2007') 0.035  100 2 3 1;  
         datenum('08/15/2012') 0.04875 100 2 3 1;  
         datenum('02/15/2031') 0.05375 100 2 3 1];
```

Choose a settlement date.

```
Settle = datenum('20-Aug-2002');
```

Assume these clean prices for the bonds.

```
Prices = [ 98.97467;  
          98.58044;  
          100.10534;  
          98.18054;  
          101.38136;  
          99.25411];
```

Use this formula to compute spot compounding for the bonds.

```
SpotCompounding = 2*ones(size(Prices));
```

Use compute the zero curve.

```
[ZeroRatesP, CurveDatesP] = zbtprice(Bonds, Prices, Settle);  
ZeroCurve = [CurveDatesP, ZeroRatesP, SpotCompounding];
```

Assign parameters.

```
OAS           = [26.0502; 28.6348; 31.2222];  
Maturity      = datenum('02-Jan-2030');  
IssueDate     = datenum('02-Jan-2000');  
GrossRate     = 0.08125;  
CouponRate    = 0.075;  
Delay         = 14;  
Interpolation = 1;  
PrepaySpeed   = [0 50 100];
```

Calculate the price from the option-adjusted spread.

```
Price = mbsoas2price(ZeroCurve, OAS, Settle, Maturity, ...  
IssueDate, GrossRate, CouponRate, Delay, Interpolation, ...  
PrepaySpeed)
```

```
Price =
```

mbsoas2price

95.0000

95.0000

95.0000

See Also

mbsprice2oas, mbsyield2oas, mbsoas2yield

Purpose

Yield given option-adjusted spread

Syntax

```
[MYield, BEMBSYield] = mbsoas2yield(ZeroCurve, OAS, Settle, Maturity, IssueDate, GrossRate, CouponRate, Delay, Interpolation, PrepaySpeed, PrepayMatrix)
```

Arguments

ZeroCurve	A matrix of three columns: <ul style="list-style-type: none">• Column 1: Serial date numbers.• Column 2: Spot rates with maturities corresponding to the dates in Column 1, in decimal (for example, 0.075).• Column 3: Compounding of the rates in Column 2. (This is the agency spot rate on the settlement date.)
OAS	Option-adjusted spreads in basis points.
Settle	Settlement date (scalar only). A serial date number or date string. Date when option-adjusted spread is calculated.
Maturity	Maturity date. Scalar or vector in serial date number or date string format.
IssueDate	Issue date. A serial date number or date string.
GrossRate	Gross coupon rate (including fees), in decimal.
CouponRate	(Optional) Net coupon rate, in decimal. Default = GrossRate.
Delay	(Optional) Delay (in days) between payment from homeowner and receipt by bondholder. Default = 0 (no delay between payment and receipt).

mbsoas2yield

Interpolation	Interpolation method. Computes the corresponding spot rates for the bond's cash flow. Available methods are (0) nearest, (1) linear, and (2) cubic spline. Default = 1. See <code>interp1</code> for more information.
PrepaySpeed	(Optional) Relation of the conditional payment rate (CPR) to the benchmark model. Default = end of month's CPR. Set <code>PrepaySpeed</code> to <code>[]</code> if you input a customized prepayment matrix.
PrepayMatrix	(Optional) Customized prepayment matrix. A matrix of size <code>max(TermRemaining)</code> -by-NMBS. Missing values are padded with NaNs. Each column corresponds to a mortgage-backed security, and each row corresponds to each month after settlement.

All inputs (except `PrepayMatrix`) are number of mortgage-backed securities (NMBS) by 1 vectors.

Description

`[MYield, BEMBSYield] = mbsoas2yield(ZeroCurve, OAS, Settle, Maturity, IssueDate, GrossRate, CouponRate, Delay, Interpolation, PrepaySpeed, PrepayMatrix)` computes the mortgage and bond-equivalent yields of a passthrough security.

`MYield` is the yield to maturity of the mortgage-backed security (the mortgage yield). This yield is compounded monthly (12 times per year).

Example: 0.075 (7.5%)

`BEMBSYield` is the corresponding bond equivalent yield of the mortgage-backed security. This yield is compounded semiannually (two times per year).

Example: 0.0761 (7.61%)

Examples

Given an option-adjusted spread, a spot curve, and a prepayment assumption, compute the theoretical yield to maturity of a mortgage pool.

Create the bonds matrix.

```
Bonds = [datenum('11/21/2002') 0 100 0 2 1;
          datenum('02/20/2003') 0 100 0 2 1;
          datenum('07/31/2004') 0.03 100 2 3 1;
          datenum('08/15/2007') 0.035 100 2 3 1;
          datenum('08/15/2012') 0.04875 100 2 3 1;
          datenum('02/15/2031') 0.05375 100 2 3 1];
```

Choose a settlement date.

```
Settle = datenum('08/20/2002');
```

Assume these clean prices for the bonds.

```
Prices = [ 98.97467;
           98.58044;
           100.10534;
           98.18054;
           101.38136;
           99.25411];
```

Use this formula to compute spot compounding for the bonds.

```
SpotCompounding = 2*ones(size(Prices));
```

Compute the zero curve.

```
[ZeroRatesP, CurveDatesP] = zbtprice(Bonds, Prices, Settle);
ZeroCurve = [CurveDatesP, ZeroRatesP, SpotCompounding];
```

Assign parameters.

```
OAS = [26.0502; 28.6348; 31.2222];
Maturity = datenum('02-Jan-2030');
```

mbsoas2yield

```
IssueDate      = datenum('02-Jan-2000');
GrossRate      = 0.08125;
CouponRate     = 0.075;
Delay          = 14;
Interpolation  = 1;
PrepaySpeed    = [0 50 100];
```

Compute the mortgage yield and bond equivalent mortgage yield.

```
[MYield BEMBSYield] = mbsoas2yield(ZeroCurve, OAS, Settle, ...
Maturity, IssueDate, GrossRate, CouponRate, Delay, ...
Interpolation, PrepaySpeed)
```

```
MYield =
```

```
0.0802
0.0814
0.0828
```

```
BEMBSYield =
```

```
0.0816
0.0828
0.0842
```

See Also

`mbsprice2oas`, `mbsyield2oas`, `mbsoas2price`

Purpose Mortgage pool cash flows and balances with prepayment

Syntax [Balance, Payment, Principal, Interest, Prepayment] = mbspassthrough(OriginalBalance, GrossRate, OriginalTerm, TermRemaining, PrepaySpeed, PrepayMatrix)

Arguments

OriginalBalance	Original balance value in dollars (balance at the beginning of each TermRemaining).
GrossRate	Gross coupon rate (including fees), in decimal.
OriginalTerm	Term of the mortgage in months.
TermRemaining	(Optional) Number of full months between settlement and maturity.
PrepaySpeed	(Optional) Relation of the conditional payment rate (CPR) to the benchmark model. Default = 0 (no prepayment). Set PrepaySpeed to [] if you input a customized prepayment matrix.
PrepayMatrix	(Optional) Used only when PrepaySpeed is unspecified. Customized prepayment vector. A NaN-padded matrix of size max(TermRemaining)-by-NMBS. Each column corresponds to each mortgage-backed security, and each row corresponds to each month after settlement.

All inputs (except PrepayMatrix) are number of mortgage-backed securities (NMBS) by 1 vectors.

Description [Balance, Payment, Principal, Interest, Prepayment] = passthrough(OriginalBalance, GrossRate, OriginalTerm, TermRemaining, PrepaySpeed, PrepayMatrix) computes the cash flow of principal, interest, and prepayment of passthrough securities. All outputs are TermRemaining-by-1 vectors of end-of-month values.

mbspassthrough

Balance is the principal balance at end of month.

Payment is the total monthly payment.

Principal is the principal portion of the payment.

Interest is the interest portion of the payment.

Prepayment indicates any unscheduled principal payment.

By default, the securities are seasoned. The applicable CPR depends upon TermRemaining based upon a 30-year prepayment model (PSA or FHA). You may supply a different CPR vector of size TermRemaining-by-1.

Examples

Compute the cash flows and balances of a three-month old mortgage pool with original term of 360 months, assuming a prepayment speed of 100.

```
OriginalBalance = 100000;  
GrossRate = 0.08125;  
OriginalTerm = 360;  
TermRemaining = 357;  
PrepaySpeed = 100;
```

```
[Balance, Payment, Principal, Interest, Prepayment] =...  
mbspassthrough(OriginalBalance, GrossRate, OriginalTerm,...  
TermRemaining, PrepaySpeed);
```

See Also

mbswal

Purpose Mortgage-backed security price given yield

Syntax [Price, AccrInt] = mbsprice(Yield, Settle, Maturity, IssueDate, GrossRate, CouponRate, Delay, PrepaySpeed, PrepayMatrix)

Arguments

Yield	Mortgage yield, compounded monthly (in decimal).
Settle	Settlement date. A serial date number or date string. Settle must be earlier than or equal to Maturity.
Maturity	Maturity date. A serial date number or date string.
IssueDate	Issue date. A serial date number or date string.
GrossRate	Gross coupon rate (including fees), in decimal.
CouponRate	(Optional) Net coupon rate, in decimal. Default = GrossRate.
Delay	(Optional) Delay (in days) between payment from homeowner and receipt by bondholder. Default = 0 (no delay between payment and receipt).
PrepaySpeed	(Optional) Relation of the conditional payment rate (CPR) to the benchmark model. Default = 0 (no prepayment). Set PrepaySpeed to [] if you input a customized prepayment matrix.
PrepayMatrix	(Optional) Customized prepayment matrix. A matrix of size max(TermRemaining)-by-NMBS. Missing values are padded with NaNs. Each column corresponds to a mortgage-backed security, and each row corresponds to each month after settlement.

All inputs (except PrepayMatrix) are number of mortgage-backed securities (NMBS) by 1 vectors.

mbsprice

Description

[Price, AccrInt] = mbsprice(Yield, Settle, Maturity, IssueDate, GrossRate, CouponRate, Delay, PrepaySpeed, PrepayMatrix) computes a mortgage-backed security price, given time information, mortgage yield at settlement, and optionally, a prepayment model.

All outputs are scalar values.

Price is the clean price for every \$100 face value of the securities.

AccrInt is the accrued interest of the mortgage-backed securities.

Examples

Example 1. Given a mortgage-backed security with the following characteristics, compute the price and the accrued interest due on the security.

```
Yield = 0.0725;
Settle = datenum('15-Apr-2002');
Maturity = datenum('1 Jan 2030');
IssueDate = datenum('1-Jan-2000');
GrossRate = 0.08125;
CouponRate = 0.075;
Delay = 14;
Speed = 100;

[Price AccrInt] = mbsprice(Yield, Settle, Maturity, IssueDate,...
    GrossRate, CouponRate, Delay, Speed)

Price =

    101.3147

AccrInt =

    0.2917
```

Example 2. Given a portfolio of mortgage-backed securities, compute the clean prices and accrued interest.

```

Yield = 0.075;
Settle = datenum(['13-Feb-2000'; '17-Apr-2002'; '17-May-2002'; ...
'13-Jan-2000']);
Maturity = datenum('1-Jan-2030');
IssueDate = datenum('1-Jan-2000');
GrossRate = 0.08125;
CouponRate = [0.075; 0.07875; 0.0775; 0.08125];
Delay = 14;
Speed = 100;

[Price AccrInt] = mbsprice(Yield, Settle, Maturity, IssueDate, ...
GrossRate, CouponRate, Delay, Speed)

Price =

    99.7085
   102.0678
   101.2792
   104.0175

AccrInt =

    0.2500
    0.3500
    0.3444
    0.2708

```

References

[1] *PSA Uniform Practices*, SF-49

See Also

mbsyield

mbsprice2oas

Purpose Option-adjusted spread given price

Syntax OAS = mbsprice2oas(ZeroCurve, Price, Settle, Maturity, IssueDate, GrossRate, CouponRate, Delay, Interpolation PrepaySpeed, PrepayMatrix)

Arguments

ZeroCurve	A matrix of three columns: <ul style="list-style-type: none">• Column 1: Serial date numbers.• Column 2: Spot rates with maturities corresponding to the dates in Column 1, in decimal (for example, 0.075).• Column 3: Compounding of the rates in Column 2. Values are 1 (annual), 2 (semiannual, 3 (three times per year), 4 (quarterly), 6 (bimonthly), 12 (monthly), and -1 (continuous).
Price	Clean price for every \$100 face value of bond issue.
Settle	Settlement date (scalar only). A serial date number or date string. Date when option-adjusted spread is calculated.
Maturity	Maturity date. Scalar or vector in serial date number or date string format.
IssueDate	Issue date. A serial date number or date string.
GrossRate	Gross coupon rate (including fees), in decimal.
CouponRate	(Optional) Net coupon rate, in decimal. Default = GrossRate.

Delay	(Optional) Delay (in days) between payment from homeowner and receipt by bondholder. Default = 0 (no delay between payment and receipt).
Interpolation	Interpolation method. Computes the corresponding spot rates for the bond's cash flow. Available methods are (0) nearest, (1) linear, and (2) cubic spline. Default = 1. See <code>interp1</code> for more information.
PrepaySpeed	(Optional) Relation of the conditional payment rate (CPR) to the benchmark model. Default = end of month's CPR. Set <code>PrepaySpeed</code> to [] if you input a customized prepayment matrix.
PrepayMatrix	(Optional) Customized prepayment matrix. A matrix of size <code>max(TermRemaining)</code> -by-NMBS. Missing values are padded with NaNs. Each column corresponds to a mortgage-backed security, and each row corresponds to each month after settlement.

All inputs (except `PrepayMatrix`) are number of mortgage-backed securities (NMBS) by 1 vectors.

Description

`OAS = mbsprice2oas(ZeroCurve, Price, Settle, Maturity, IssueDate, GrossRate, CouponRate, Delay, Interpolation, PrepaySpeed, PrepayMatrix)` computes the option-adjusted spread in basis points.

Examples

Calculate the option-adjusted spread of a 30-year fixed-rate mortgage with about a 28-year weighted average maturity remaining, given assumptions of 0, 50, and 100 PSA prepayments.

Create the bonds matrix.

```
Bonds = [datenum('11/21/2002') 0      100 0 2 1;
          datenum('02/20/2003') 0      100 0 2 1;
```

```
datenum('07/31/2004') 0.03 100 2 3 1;  
datenum('08/15/2007') 0.035 100 2 3 1;  
datenum('08/15/2012') 0.04875 100 2 3 1;  
datenum('02/15/2031') 0.05375 100 2 3 1];
```

Choose a settlement date.

```
Settle= datenum('20-Aug-2002');
```

Assume these clean prices for the bonds.

```
Prices = [ 98.97467;  
          98.58044;  
          100.10534;  
          98.18054;  
          101.38136;  
          99.25411];
```

Use this formula to compute spot compounding for the bonds.

```
SpotCompounding = 2*ones(size(Prices));
```

Compute the zero curve.

```
[ZeroRatesP, CurveDatesP] = zbtprice(Bonds, Prices, Settle);  
ZeroCurve = [CurveDatesP, ZeroRatesP, SpotCompounding];
```

Assign parameters.

```
Price          = 95;  
Maturity       = datenum('02-Jan-2030');  
IssueDate      = datenum('02-Jan-2000');  
GrossRate      = 0.08125;  
CouponRate     = 0.075;  
Delay          = 14;  
Interpolation  = 1;  
PrepaySpeed    = [0; 50; 100];  
Interpolation  = 1;
```



```
PrepaySpeed = [0; 50; 100];
```

Compute the option adjusted spread.

```
OAS = mbsprice2oas(ZeroCurve, Price, Settle, Maturity, ...  
IssueDate, GrossRate, CouponRate, Delay, Interpolation, ...  
PrepaySpeed)
```

```
OAS =
```

```
26.0502
```

```
28.6348
```

```
31.2222
```

See Also

[mbssoas2price](#), [mbssoas2yield](#), [mbsyield2oas](#)

mbsprice2speed

Purpose Implied PSA prepayment speeds given price

Syntax [ImpSpdOnPrc, ImpSpdOnDur, ImpSpdOnCnv] = mbsprice2speed(Price, Settle, Maturity, IssueDate, GrossRate, PrepayMatrix, CouponRate, Delay)

Arguments

Price	Clean price for every \$100 face value.
Settle	Settlement date. A serial date number or date string. Settle must be earlier than or equal to Maturity.
Maturity	Maturity date. A serial date number or date string.
IssueDate	Issue date. A serial date number or date string.
GrossRate	Gross coupon rate (including fees), in decimal.
PrepayMatrix	Customized prepayment matrix. A matrix of size max(TermRemaining)-by-NMBS. Missing values are padded with NaNs. Each column corresponds to a mortgage-backed security, and each row corresponds to each month after settlement.
CouponRate	(Optional) Net coupon rate, in decimal. Default = GrossRate.
Delay	(Optional) Delay (in days) between payment from homeowner and receipt by bondholder. Default = 0 (no delay between payment and receipt).

All inputs (except PrepayMatrix) are number of mortgage-backed securities (NMBS) by 1 vectors.

Description

[ImpSpdOnPrc, ImpSpdOnDur, ImpSpdOnCnv] = mbsprice2speed(Price, Settle, Maturity, IssueDate, GrossRate, PrepayMatrix, CouponRate, Delay) computes PSA prepayment speeds implied by pool prices and projected (user-defined)

prepayment vectors. The calculated PSA speed produces the same price, modified duration, or modified convexity, depending upon the output requested.

ImpSpdOnPrc calculates the equivalent PSA benchmark prepayment speed for the passthrough to carry the same price.

ImpSpdOnDur calculates the equivalent PSA benchmark prepayment speed for the passthrough to carry the same modified duration.

ImpSpdOnCnv calculates the equivalent PSA benchmark prepayment speed for the passthrough to carry the same modified convexity.

All outputs are NMBS-by-1 vectors.

Examples

Calculate the equivalent PSA benchmark prepayment speeds for a mortgage pool with these characteristics and prepayment matrix.

```

Price           = 101;
Settle          = datenum('1-Jan-2000');
Maturity        = datenum('1-Jan-2030');
IssueDate       = datenum('1-Jan-2000');
GrossRate       = 0.08125;
PrepayMatrix    = 0.005*ones(360,1);
CouponRate      = 0.075;
Delay           = 14;

[ImpSpdOnPrc, ImpSpdOnDur, ImpSpdOnCnv] = ...
mbsprice2speed(Price,Settle, Maturity, IssueDate, ...
GrossRate, PrepayMatrix, CouponRate, Delay)

ImpSpdOnPrc =

    118.5980

ImpSpdOnDur =

    118.3946

```

mbsprice2speed

ImpSpdOnCnv =

109.5115

References [1] *PSA Uniform Practices*, SF-49

See Also mbsprice, mbsyield2speed

Purpose Weighted average life of mortgage pool

Compatibility PSA

Syntax `WAL = mbswal(Settle, Maturity, IssueDate, GrossRate, CouponRate, Delay, PrepaySpeed, PrepayMatrix)`

Arguments	Settle	Settlement date. A serial date number or date string. Settle must be earlier than or equal to Maturity .
	Maturity	Maturity date. A serial date number or date string.
	IssueDate	Issue date. A serial date number or date string.
	GrossRate	Gross coupon rate (including fees), in decimal.
	CouponRate	(Optional) Net coupon rate, in decimal. Default = GrossRate .
	Delay	(Optional) Delay (in days) between payment from homeowner and receipt by bondholder. Default = 0 (no delay between payment and receipt).
	PrepaySpeed	(Optional) Relation of the conditional payment rate (CPR) to the benchmark model. Default = end of month's CPR. Set PrepaySpeed to [] if you input a customized prepayment matrix.
	PrepayMatrix	(Optional) Customized prepayment matrix. A matrix of size <code>max(TermRemaining)-by-NMBS</code> . Missing values are padded with NaNs. Each column corresponds to a mortgage-backed security, and each row corresponds to each month after settlement.

All inputs (except **PrepayMatrix**) are number of mortgage-backed securities (NMBS) by 1 vectors.

mbswal

Description

WAL = mbswal(Settle, Maturity, IssueDate, GrossRate, CouponRate, Delay, PrepaySpeed, PrepayMatrix) computes the weighted average life, in number of years, of a mortgage pool, as measured from the settlement date.

Examples

Given a passthrough security with the following characteristics, compute the weighted average life of the security.

```
Settle = datenum('15-Apr-2002');
Maturity = datenum('1 Jan 2030');
IssueDate = datenum('1-Jan-2000');
GrossRate = 0.08125;
CouponRate = 0.075;
Delay = 14;
Speed = 100;
```

```
WAL = mbswal(Settle, Maturity, IssueDate, GrossRate, ...
CouponRate, Delay, Speed)
```

```
WAL =
    10.5477
```

References

[1] *PSA Uniform Practices*, SF-49

See Also

mbspassthrough

Purpose Mortgage-backed security yield given price

Syntax [MYield, BEMBSYield] = mbsyield(Price, Settle, Maturity, IssueDate, GrossRate, CouponRate, Delay, PrepaySpeed, PrepayMatrix)

Arguments

- Price Clean price for every \$100 face value.
- Settle Settlement date. A serial date number or date string. Settle must be earlier than or equal to Maturity.
- Maturity Maturity date. A serial date number or date string.
- IssueDate Issue date. A serial date number or date string.
- GrossRate Gross coupon rate (including fees), in decimal.
- CouponRate (Optional) Net coupon rate, in decimal. Default = GrossRate.
- Delay (Optional) Delay (in days) between payment from homeowner and receipt by bondholder. Default = 0 (no delay between payment and receipt).
- PrepaySpeed (Optional) Relation of the conditional payment rate (CPR) to the benchmark model. Default = 0 (no prepayment). Set PrepaySpeed to [] if you input a customized prepayment matrix.
- PrepayMatrix (Optional) Customized prepayment matrix. A matrix of size max(TermRemaining)-by-NMBS. Missing values are padded with NaNs. Each column corresponds to a mortgage-backed security, and each row corresponds to each month after settlement.

All inputs (except PrepayMatrix) are number of mortgage-backed securities (NMBS) by 1 vectors.

Description

[MYield, BEMBSYield] = mbsyield(Price, Settle, Maturity, IssueDate, GrossRate, CouponRate, Delay, PrepaySpeed,

PrepayMatrix) computes a mortgage-backed security yield to maturity and the bond equivalent yield, given time information, price at settlement, and optionally, a prepayment model.

MYield is the yield to maturity of the mortgage-backed security (the mortgage yield). This yield is compounded monthly (12 times a year).

BEMBSYield is the corresponding bond equivalent yield of the mortgage-backed security. This yield is compounded semiannually (two times a year).

Examples

Example 1. Given a mortgage-backed security with the following characteristics, compute the mortgage yield and the bond equivalent yield of the security.

```
Price = 102;
Settle = '15-Apr-2002';
Maturity = '1 Jan 2030';
IssueDate = '1-Jan-2000';
GrossRate = 0.08125;
CouponRate = 0.075;
Delay = 14;
Speed = 100;

[MYield, BEMBSYield] = mbsyield(Price, Settle, Maturity, ...
IssueDate, GrossRate, CouponRate, Delay, Speed)

MYield =

    0.0715

BEMBSYield =

    0.0725
```

Example 2. Given a portfolio of mortgage-backed securities, compute the mortgage yields and the bond equivalent yields.


```

Price = 102;
Settle = datenum(['13-Feb-2000'; '17-Apr-2002'; '17-May-2002'; ...
'13-Jan-2000']);
Maturity = datenum('1-Jan-2030');
IssueDate = datenum('1-Jan-2000');
GrossRate = 0.08125;
CouponRate = [0.075; 0.07875; 0.0775; 0.08125];
Delay = 14;
Speed = 100;

[MYield, BEMBSYield] = mbsyield(Price, Settle, Maturity, ...
IssueDate, GrossRate, CouponRate, Delay, Speed)

MYield =

    0.0717
    0.0751
    0.0739
    0.0779

BEMBSYield =

    0.0728
    0.0763
    0.0750
    0.0791

```

References

[1] PSA Uniform Practices, SF-49

See Also

mbsprice

mbsyield2oas

Purpose Option-adjusted spread given yield

Syntax OAS = mbsyield2oas(ZeroCurve, Yield, Settle, Maturity, IssueDate, GrossRate, CouponRate, Delay, Interpolation PrepaySpeed, PrepayMatrix)

Arguments

ZeroCurve	A matrix of three columns: Column 1: serial date numbers Column 2: spot rates with maturities corresponding to the dates in Column 1, in decimal (for example, 0.075) Column 3: Compounding of the rates in Column 2. Values are 1 (annual), 2 (semiannual), 3 (three times per year), 4 (quarterly), 6 (bimonthly), 12 (monthly), and -1 (continuous).
Yield	Mortgage yield, compounded monthly (in decimal).
Settle	Settlement date (scalar only). A serial date number or date string. Date when option-adjusted spread is calculated.
Maturity	Maturity date. Scalar or vector in serial date number or date string format.
IssueDate	Issue date. A serial date number or date string.
GrossRate	Gross coupon rate (including fees), in decimal.
CouponRate	(Optional) Net coupon rate, in decimal. Default = GrossRate.
Delay	(Optional) Delay (in days) between payment from homeowner and receipt by bondholder. Default = 0 (no delay between payment and receipt).

- Interpolation** Interpolation method. Computes the corresponding spot rates for the bond's cash flow. Available methods are (0) nearest, (1) linear, and (2) cubic spline. Default = 1. See `interp1` for more information.
- PrepaySpeed** (Optional) Relation of the conditional payment rate (CPR) to the benchmark model. Default = end of month's CPR. Set `PrepaySpeed` to [] if you input a customized prepayment matrix.
- PrepayMatrix** (Optional) Customized prepayment matrix. A matrix of size `max(TermRemaining)`-by-NMBS. Missing values are padded with NaNs. Each column corresponds to a mortgage-backed security, and each row corresponds to each month after settlement.

All inputs (except `PrepayMatrix`) are number of mortgage-backed securities (NMBS) by 1 vectors.

Description

`OAS = mbsyield2oas(ZeroCurve, Yield, Settle, Maturity, IssueDate, GrossRate, CouponRate, Delay, Interpolation, PrepaySpeed, PrepayMatrix)` computes the option-adjusted spread in basis points.

Examples

Calculate the option-adjusted spread of a 30-year fixed-rate mortgage pool with about 28-year weighted average maturity left, given assumptions of 0, 50, and 100 PSA prepayments.

Create bonds matrix.

```
Bonds = [datenum('11/21/2002') 0      100 0 2 1;
          datenum('02/20/2003') 0      100 0 2 1;
          datenum('07/31/2004') 0.03   100 2 3 1;
          datenum('08/15/2007') 0.035  100 2 3 1;
          datenum('08/15/2012') 0.04875 100 2 3 1;
          datenum('02/15/2031') 0.05375 100 2 3 1];
```

Choose a settlement date.

```
Settle = datenum('08/20/2002');
```

Assume these clean prices for the bonds.

```
Prices = [ 98.97467;  
          98.58044;  
          100.10534;  
          98.18054;  
          101.38136;  
          99.25411];
```

Use this formula to compute spot compounding for the bonds.

```
SpotCompounding = 2*ones(size(Prices));
```

Compute the zero curve.

```
[ZeroRatesP, CurveDatesP] = zbtprice(Bonds, Prices, Settle);  
ZeroCurve = [CurveDatesP, ZeroRatesP, SpotCompounding];
```

Assign parameters.

```
Price          = 95;  
Maturity       = datenum('02-Jan-2030');  
IssueDate      = datenum('02-Jan-2000');  
GrossRate      = 0.08125;  
CouponRate     = 0.075;  
Delay          = 14;  
Interpolation  = 1;  
PrepaySpeed    = [0 50 100];
```

Compute the yield and from the yield compute the option-adjusted spread.

```
[mbsyld, beyld] = mbsyield(Price, Settle, ...  
Maturity, IssueDate, GrossRate, CouponRate, Delay, PrepaySpeed);
```

```
OAS = mbsyield2oas(ZeroCurve, mbsyld, Settle, ...  
Maturity, IssueDate, GrossRate, CouponRate, Delay, ...  
Interpolation, PrepaySpeed)
```

OAS =

26.0502

28.6348

31.2222

See Also

[mboas2price](#), [mboas2yield](#), [mbsprice2oas](#)

mbsyield2speed

Purpose Implied PSA prepayment speeds given yield

Syntax [ImpSpdOnYld, ImpSpdOnDur, ImpSpdOnCnv] = mbsyield2speed(Yield, Settle, Maturity, IssueDate, GrossRate, PrepayMatrix, CouponRate, Delay)

Arguments

Yield	Mortgage yield, compounded monthly, in decimal.
Settle	Settlement date. A serial date number or date string. Settle must be earlier than or equal to Maturity.
Maturity	Maturity date. A serial date number or date string.
IssueDate	Issue date. A serial date number or date string.
GrossRate	Gross coupon rate (including fees), in decimal.
PrepayMatrix	Customized prepayment matrix. A matrix of size max(TermRemaining)-by-NMBS. Missing values are padded with NaNs. Each column corresponds to a mortgage-backed security, and each row corresponds to each month after settlement.
CouponRate	(Optional) Net coupon rate, in decimal. Default = GrossRate.
Delay	(Optional) Delay (in days) between payment from homeowner and receipt by bondholder. Default = 0 (no delay between payment and receipt).

All inputs (except PrepayMatrix) are number of mortgage-backed securities (NMBS) by 1 vectors.

Description [ImpSpdOnYld, ImpSpdOnDur, ImpSpdOnCnv] = mbsyield2speed(Yield, Settle, Maturity, IssueDate, GrossRate, PrepayMatrix, CouponRate, Delay) computes PSA prepayment speeds implied by pool yields and projected (user-defined)

prepayment vectors. The calculated PSA speed produces the same yield, modified duration, or modified convexity, depending upon the output requested.

`ImpSpd0nPrc` calculates the equivalent PSA benchmark prepayment speed for the passthrough to carry the same price.

`ImpSpd0nDur` calculates the equivalent PSA benchmark prepayment speed for the passthrough to carry the same modified duration.

`ImpSpd0nCnv` calculates the equivalent PSA benchmark prepayment speed for the passthrough to carry the same modified convexity.

All outputs are NMBS-by-1 vectors.

Examples

Calculate the equivalent PSA benchmark prepayment speeds for a security with these characteristics and prepayment matrix.

```
Yield = 0.065;
Settle = datenum('1-Jan-2000');
Maturity = datenum('1-Jan-2030');
IssueDate = datenum('1-Jan-2000');
GrossRate = 0.08125;
PrepayMatrix = 0.005*ones(360,1);
CouponRate = 0.075;
Delay = 14;

[ImpSpd0nYld, ImpSpd0nDur, ImpSpd0nCnv] = ...
mbsyield2speed(Yield, Settle, Maturity, IssueDate, GrossRate, ...
PrepayMatrix, CouponRate, Delay)

ImpSpd0nYld =

    117.7644

ImpSpd0nDur =

    116.7436
```

mbsyield2speed

ImpSpdOnCnv =

108.3309

References [1] *PSA Uniform Practices*, SF-49

See Also mbsyield, mbsprice2speed

Purpose Benchmark default

Syntax [ADRPSA, MDRPSA] = psaspeed2default(DefaultSpeed)

Arguments

DefaultSpeed	Annual speed relative to the benchmark. PSA benchmark = 100.
--------------	--

Description [ADRPSA, MDRPSA] = psaspeed2default(DefaultSpeed) computes the benchmark default on the performing balance of mortgage-backed securities per PSA benchmark speed.

ADRPSA is the PSA default rate, in decimal (360-by-1).

MDRPSA is the PSA monthly default rate, in decimal (360-by-1).

Examples Given a mortgage-backed security with annual speed set at the PSA default benchmark, compute the default rates.

```
DefaultSpeed = 100;
```

```
[ADRPSA, MDRPSA] = psaspeed2default(DefaultSpeed);
```

See Also psaspeed2rate

psaspeed2rate

Purpose Single monthly mortality rate given PSA speed

Syntax [CPRPSA, SMMPSA]= psaspeed2rate(PSASpeed)

Arguments PSASpeed Any value > 0 representing the annual speed relative to the benchmark. PSA benchmark = 100.

Description [CPRPSA, SMMPSA]= psaspeed2rate(PSASpeed) calculates vectors of PSA prepayments, each containing 360 prepayment elements, to represent the 360 months in a 30-year mortgage pool.
CPRPSA is the PSA conditional prepayment rate, in decimal [360-by-1].
SMMPSA is the PSA single monthly mortality rate, in decimal [360-by-1].

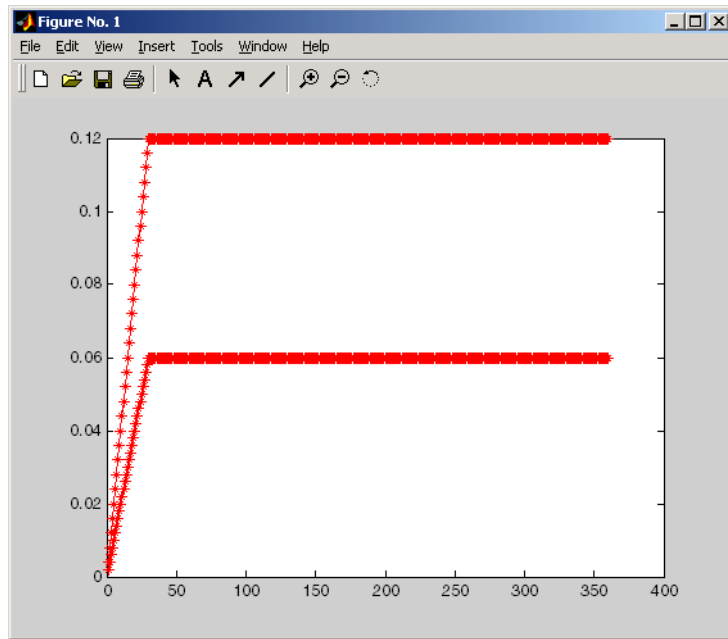
Examples Given a mortgage-backed security with annual speed set at the PSA default benchmark, compute the prepayment and mortality rates.

```
PSASpeed = [100 200];
```

```
[CPRPSA, SMMPSA]= psaspeed2rate(PSASpeed);
```

View a plot of the output.

```
psaspeed2rate(PSASpeed)
```



See Also [psaspeed2default](#)

stepcpncfamounts

Purpose Cash flow amounts and times for bonds and stepped coupons

Syntax [CFlows, CDates, CTimes] = stepcpncfamounts(Settle, Maturity, ConvDates, CouponRates, Period, Basis, EndMonthRule, Face)

Arguments

Settle	Settlement date. A scalar or vector of serial date numbers. Settle must be earlier than or equal to Maturity.
Maturity	Maturity date. A scalar or vector of serial date numbers.
ConvDates	Matrix of serial date numbers representing conversion dates after Settle. Size = number of instruments by maximum number of conversions. Fill unspecified entries with NaN.
CouponRates	Matrix indicating the coupon rates for each bond in decimal form. Size = number of instruments by maximum number of conversions + 1. First column of this matrix contains rates applicable between Settle and the first conversion date (date in the first column of ConvDates). Fill unspecified entries with NaN. See Note below.
Period	(Optional) Coupons per year of the bond. A vector of integers. Allowed values are 0, 1, 2, 3, 4, 6, and 12. Default = 2.

Basis	<p>(Optional) Day-count basis of the instrument. A vector of integers.</p> <ul style="list-style-type: none">• 0 = actual/actual (default)• 1 = 30/360 (SIA)• 2 = actual/360• 3 = actual/365• 4 = 30/360 (PSA)• 5 = 30/360 (ISDA)• 6 = 30/360 (European)• 7 = actual/365 (Japanese)• 8 = actual/actual (ISMA)• 9 = actual/360 (ISMA)• 10 = actual/365 (ISMA)
EndMonthRule	<p>(Optional) End-of-month rule. A vector. This rule applies only when Maturity is an end-of-month date for a month having 30 or fewer days. 0 = ignore rule, meaning that a bond's coupon payment date is always the same numerical day of the month. 1 = set rule on (default), meaning that a bond's coupon payment date is always the last actual day of the month.</p>
Face	<p>(Optional) Face value of each bond in the portfolio. Default = 100.</p>

All arguments must be scalars or number of bonds (NUMBONDS) by 1 vectors, except for ConvDates and CouponRates.

stepcpncfamounts

Note ConvDates has the same number of rows as CouponRates to reflect the same number of bonds. However, ConvDates has one less column than CouponRates. This situation is illustrated by

```
Settle-----ConvDate1-----ConvDate2-----Maturity
                                     Rate1           Rate2           Rate3
```

Description

[CFlows, CDates, CTimes] = stepcpncfamounts(Settle, Maturity, ConvDates, CouponRates, Period, Basis, EndMonthRule, Face) returns matrices of cash flow amounts, cash flow dates, and time factors for a portfolio of NUMBONDS stepped-coupon bonds.

CFlows is a matrix of cash flow amounts. The first entry in each row vector is a negative number indicating the accrued interest due at settlement. If no accrued interest is due, the first column is 0.

CDates is a matrix of cash flow dates in serial date number form. At least two columns are always present, one for settlement and one for maturity.

CTimes is a matrix of time factors for the SIA semiannual price/yield conversion.

$$\text{DiscountFactor} = (1 + \text{Yield}/2)^{-\text{TFactor}}$$

Time factors are in units of semiannual coupon periods. In computing time factors, use SIA actual/actual conventions for all time factor calculations.

Note For bonds with fixed coupons, use cfamounts. If you use a fixed-coupon bond with stepcpncfamounts, MATLAB generates an error.

Examples

This example generates stepped cash flows for three different bonds, all paying interest semiannually. Their life span is about 18-19 years each:

- Bond A has two conversions, but the first one occurs on the settlement date and immediately expires.
- Bond B has three conversions, with conversion dates exactly on the coupon dates.
- Bond C has three conversions, with some conversion dates not on the coupon dates. It has the longest maturity. This case illustrates that only cash flows for full periods after conversion dates are affected, as illustrated below.



The following table illustrates the interest rate characteristics of this bond portfolio.

Bond A Dates	Bond A Rates	Bond B Dates	Bond B Rates	Bond C Dates	Bond C Rates
Settle (02-Aug-92)	7.5%	Settle (02-Aug-92)	7.5%	Settle (02-Aug-92)	2.5%
First Conversion (02-Aug-92)	8.875%	First Conversion (15-Jun-97)	8.875%	First Conversion (14-Jun-97)	5.0%
Second Conversion (15-Jun-03)	9.25%	Second Conversion (15-Jun-01)	9.25%	Second Conversion (14-Jun-01)	7.5%

stepcpncfamounts

Bond A Dates	Bond A Rates	Bond B Dates	Bond B Rates	Bond C Dates	Bond C Rates
Maturity (15-Jun-10)	NaN	Third Conversion (15-Jun-05)	10.0%	Third Conversion (14-Jun-05)	10.0%
		Maturity (15-Jun-10)	NaN	Maturity (15-Jun-11)	NaN

```

Settle = datenum('02-Aug-1992');

ConvDates = [datenum('02-Aug-1992'), datenum('15-Jun-2003'),...
             nan;
             datenum('15-Jun-1997'), datenum('15-Jun-2001'),...
             datenum('15-Jun-2005');
             datenum('14-Jun-1997'), datenum('14-Jun-2001'),...
             datenum('14-Jun-2005')];

Maturity = [datenum('15-Jun-2010');
            datenum('15-Jun-2010');
            datenum('15-Jun-2011')];

CouponRates = [0.075 0.08875 0.0925 nan;
               0.075 0.08875 0.0925 0.1;
               0.025 0.05 0.0750 0.1];

Basis = 1;
Period = 2;
EndMonthRule = 1;
Face = 100;

```

Call `stepcpncfamounts` to compute cash flows and timings.

```

[CFflows, CDates, CTimes] = stepcpncfamounts(Settle, Maturity, ...
ConvDates, CouponRates);

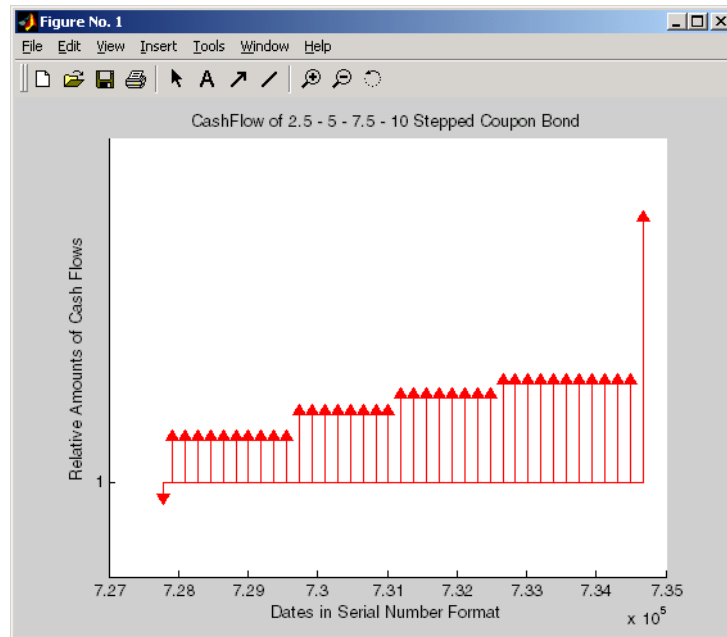
```

Visualize the third bond cash flows (2.5 - 5 - 7.5 - 10).


```

cfplot(CDates(3,:),CFFlows(3,:));
xlabel('Dates in Serial Number Format')
ylabel('Relative Amounts of Cash Flows')
title('CashFlow of 2.5 - 5 - 7.5 - 10 Stepped Coupon Bond')

```



See Also [stepcpnprice](#), [stepcpnyield](#)

stepcpnprice

Purpose Price bond with stepped coupons

Syntax [Price, AccruedInterest] = stepcpnprice(Yield, Settle, Maturity, ConvDates, CouponRates, Period, Basis, EndMonthRule, Face)

Arguments

Yield	Scalar or vector containing yield to maturity of instruments.
Settle	Settlement date. A scalar or vector of serial date numbers. Settle must be earlier than or equal to Maturity.
Maturity	Maturity date. A scalar or vector of serial date numbers.
ConvDates	Matrix of serial date numbers representing conversion dates after Settle. Size = number of instruments by maximum number of conversions. Fill unspecified entries with NaN.
CouponRates	Matrix indicating the coupon rates for each bond in decimal form. Size = number of instruments by maximum number of conversions + 1. First column of this matrix contains rates applicable between Settle and the first conversion date (date in the first column of ConvDates). Fill unspecified entries with NaN. See Note below.
Period	(Optional) Coupons per year of the bond. A vector of integers. Allowed values are 0, 1, 2, 3, 4, 6, and 12. Default = 2.

Basis	(Optional) Day-count basis of the instrument. A vector of integers. <ul style="list-style-type: none">• 0 = actual/actual (default)• 1 = 30/360 (SIA)• 2 = actual/360• 3 = actual/365• 4 = 30/360 (PSA)• 5 = 30/360 (ISDA)• 6 = 30/360 (European)• 7 = actual/365 (Japanese)• 8 = actual/actual (ISMA)• 9 = actual/360 (ISMA)• 10 = actual/365 (ISMA)
EndMonthRule	(Optional) End-of-month rule. A vector. This rule applies only when Maturity is an end-of-month date for a month having 30 or fewer days. 0 = ignore rule, meaning that a bond's coupon payment date is always the same numerical day of the month. 1 = set rule on (default), meaning that a bond's coupon payment date is always the last actual day of the month.
Face	(Optional) Face value of each bond in the portfolio. Default = 100.

All arguments must be scalars or number of bonds (NUMBONDS) by 1 vectors, except for ConvDates and CouponRates.

stepcpnprice

Note ConvDates has the same number of rows as CouponRate to reflect the same number of bonds. However, ConvDates has one less column than CouponRate. This situation is illustrated by

```
Settle-----ConvDate1-----ConvDate2-----Maturity
                                     Rate1           Rate2           Rate3
```

Description

[Price, AccruedInterest] = stepcpnprice(Yield, Settle, Maturity, ConvDates, CouponRates, Period, Basis, EndMonthRule, Face) computes the price of bonds with stepped coupons given the yield to maturity. The function supports any number of conversion dates.

Price is a NUMBONDS-by-1 vector of clean prices.

AccruedInterest is a NUMBONDS-by-1 vector of accrued interest payable at settlement dates.

Note For bonds with fixed coupons, use bndprice. If you use a fixed-coupon bond with stepcpnprice, you will receive the error: incorrect number of inputs .

Examples

Compute the price and accrued interest due on a portfolio of stepped-coupon bonds having a yield of 7.221%, given three conversion scenarios:

- Bond A has two conversions, the first one falling on the settle date and immediately expiring.
- Bond B has three conversions, with conversion dates exactly on the coupon dates.

- Bond C has three conversions, with one or more conversion dates not on coupon dates. This case illustrates that only cash flows for full periods after conversion dates are affected, as illustrated below.



The following table illustrates the interest rate characteristics of this bond portfolio.

Bond A Dates	Bond A Rates	Bond B Dates	Bond B Rates	Bond C Dates	Bond C Rates
Settle (02-Aug-92)	7.5%	Settle (02-Aug-92)	7.5%	Settle (02-Aug-92)	7.5%
First Conversion (02-Aug-92)	8.875%	First Conversion (15-Jun-97)	8.875%	First Conversion (14-Jun-97)	8.875%
Second Conversion (15-Jun-03)	9.25%	Second Conversion (15-Jun-01)	9.25%	Second Conversion (14-Jun-01)	9.25%
Maturity (15-Jun-10)	NaN	Third Conversion (15-Jun-05)	10.0%	Third Conversion (14-Jun-05)	10.0%
		Maturity (15-Jun-10)	NaN	Maturity (15-Jun-10)	NaN

```

Yield = 0.07221;
Settle = datenum('02-Aug-1992');
ConvDates = [datenum('02-Aug-1992'), datenum('15-Jun-2003'),...
             nan;
             datenum('15-Jun-1997'), datenum('15-Jun-2001'),...
             datenum('15-Jun-2005');
             datenum('14-Jun-1997'), datenum('14-Jun-2001'),...

```

stepcpnprice

```
        datenum('14-Jun-2005'));
Maturity = datenum('15-Jun-2010');

CouponRates = [0.075 0.08875 0.0925 nan;
               0.075 0.08875 0.0925 0.1;
               0.075 0.08875 0.0925 0.1];

Basis = 1;
Period = 2;
EndMonthRule = 1;
Face = 100;

[Price, AccruedInterest] = ...
stepcpnprice(Yield, Settle, Maturity, ConvDates, CouponRates, ...
Period, Basis, EndMonthRule, Face)

Price =

    117.3824
    113.4339
    113.4339

AccruedInterest =

    1.1587
    0.9792
    0.9792
```

References

This function adheres to *SIA Fixed Income Securities Formulas for Price, Yield, and Accrued Interest*, Volume 1, 3rd edition, pp. 120 - 123, on zero-coupon instruments pricing.

See Also

bndprice, cdprice, stepcpncfamounts, stepcpnyield, tbillprice, zeroprice

Purpose

Yield to maturity of bond with stepped coupons

Syntax

Yield = stepcpnyield(Price, Settle, Maturity, ConvDates, CouponRate, Period, Basis, EndMonthRule, Face)

Arguments

Price	Vector containing price of the bonds.
Settle	Settlement date. A vector of serial date numbers. Settle must be earlier than or equal to Maturity.
Maturity	Maturity date. A vector of serial date numbers.
ConvDates	Matrix of serial date numbers representing conversion dates after Settle. Size = number of instruments by maximum number of conversions. Fill unspecified entries with NaN.
CouponRates	Matrix indicating the coupon rates for each bond in decimal form. Size = number of instruments by maximum number of conversions + 1. First column of this matrix contains rates applicable between Settle and the first conversion date (date in the first column of ConvDates). Fill unspecified entries with NaN. See Note below.
Period	(Optional) Coupons per year of the bond. A vector of integers. Allowed values are 0, 1, 2, 3, 4, 6, and 12. Default = 2.

Basis	(Optional) Day-count basis of the instrument. A vector of integers. <ul style="list-style-type: none">• 0 = actual/actual (default)• 1 = 30/360 (SIA)• 2 = actual/360• 3 = actual/365• 4 = 30/360 (PSA)• 5 = 30/360 (ISDA)• 6 = 30/360 (European)• 7 = actual/365 (Japanese)• 8 = actual/actual (ISMA)• 9 = actual/360 (ISMA)• 10 = actual/365 (ISMA)
EndMonthRule	(Optional) End-of-month rule. A vector. This rule applies only when Maturity is an end-of-month date for a month having 30 or fewer days. 0 = ignore rule, meaning that a bond's coupon payment date is always the same numerical day of the month. 1 = set rule on (default), meaning that a bond's coupon payment date is always the last actual day of the month.
Face	(Optional) Face value of each bond in the portfolio. Default = 100.

All arguments must be number of bonds (NUMBONDS) by 1 vectors, except for ConvDates and CouponRate.

Note ConvDates has the same number of rows as CouponRate to reflect the same number of bonds. However, ConvDates has one less column than CouponRate. This situation is illustrated by

Settle-----	ConvDate1-----	ConvDate2-----	Maturity
Rate1	Rate2	Rate3	

Description

Yield = stepcpnyield(Price, Settle, Maturity, ConvDates, CouponRate, Period, Basis, EndMonthRule, Face) computes the yield to maturity of bonds with stepped coupons given the price. The function supports any number of conversion dates.

Yield is a NUMBONDS-by-1 vector of yields to maturity in decimal form.

Note For bonds with fixed coupons, use bndyield. You will receive the error incorrect number of inputs if you use a fixed-coupon bond with stepcpnyield.

Examples

Find the yield to maturity of three stepped-coupon bonds of known price, given three conversion scenarios:

- Bond A has two conversions, the first one falling on the settle date and immediately expiring.
- Bond B has three conversions, with conversion dates exactly on the coupon dates.
- Bond C has three conversions, with one or more conversion dates not on coupon dates. This case illustrates that only cash flows for full periods after conversion dates are affected, as illustrated below.

stepcpnyield



The following table illustrates the interest rate characteristics of this bond portfolio.

Bond A Dates	Bond A Rates	Bond B Dates	Bond B Rates	Bond C Dates	Bond C Rates
Settle (02-Aug-92)	7.5%	Settle (02-Aug-92)	7.5%	Settle (02-Aug-92)	7.5%
First Conversion (02-Aug-92)	8.875%	First Conversion (15-Jun-97)	8.875%	First Conversion (14-Jun-97)	8.875%
Second Conversion (15-Jun-03)	9.25%	Second Conversion (15-Jun-01)	9.25%	Second Conversion (14-Jun-01)	9.25%
Maturity (15-Jun-10)	NaN	Third Conversion (15-Jun-05)	10.0%	Third Conversion (14-Jun-05)	10.0%
		Maturity (15-Jun-10)	NaN	Maturity (15-Jun-10)	NaN

```
format long
```

```
Price = [117.3824; 113.4339; 113.4339];
```

```
Settle = datenum('02-Aug-1992');
```

```
ConvDates = [datenum('02-Aug-1992'), datenum('15-Jun-2003'), nan;
```

```
datenum('15-Jun-1997'), datenum('15-Jun-2001'), datenum('15-Jun-2005');
```

```
datenum('14-Jun-1997'), datenum('14-Jun-2001'), datenum('14-Jun-2005')];
```

```
Maturity = datenum('15-Jun-2010');
```

```
CouponRates = [0.075 0.08875 0.0925 nan;
```

```
0.075 0.08875 0.0925 0.1;  
0.075 0.08875 0.0925 0.1];  
Basis = 1;  
Period = 2;  
EndMonthRule = 1;  
Face = 100;  
  
Yield = stepcpnyield(Price, Settle, Maturity, ConvDates, ...  
CouponRates, Period, Basis, EndMonthRule, Face)  
  
Yield =  
  
0.07221440204915  
0.07221426780036  
0.07221426780036
```

References

This function adheres to *SIA Fixed Income Securities Formulas for Price, Yield, and Accrued Interest*, Volume 1, 3rd edition, pp. 120 - 123, on zero-coupon instruments pricing.

See Also

bndprice, cdprice, stepcpncfamoumts, stepcpnprice, tbillprice, zeroprice

tbilldisc2yield

Purpose Convert Treasury bill discount to equivalent yield

Syntax [BEYield MMYield] = tbilldisc2yield(Discount, Settle, Maturity)

Arguments

Discount	Discount rate of Treasury bills in decimal. The discount rate basis is actual/360.
Settle	Settlement date. Settle must be earlier than or equal to Maturity.
Maturity	Maturity date.

Inputs must either be a scalar or a vector of size equal to the number of Treasury bills (NTBILLS) by 1 or 1-by-NTBILLS.

Description

[BEYield MMYield] = tbilldisc2yield(Yield, Settle, Maturity) converts the discount rate on Treasury bills into their respective money-market or bond-equivalent yields.

BEYield is an NTBILLS-by-1 vector of bond-equivalent yields. The bond-equivalent yield basis is actual/365.

MMYield is an NTBILLS-by-1 vector of money-market yields. The money-market yield basis is actual/360.

Examples

Given a Treasury bill with these characteristics, compute the bond-equivalent and money-market yields.

```
Discount = 0.0497;  
Settle = '01-Oct-02';  
Maturity = '31-Mar-03';
```

```
[BEYield MMYield] = tbilldisc2yield(Discount, Settle, Maturity)
```

```
BEYield =
```

0.0517

MMYield =

0.0510

References

This function adheres to *SIA Fixed Income Securities Formulas for Price, Yield, and Accrued Interest*, Volume 1, 3rd edition, pp. 44 - 45 (on Treasury bills), and *Money Market and Bond Calculation* by Stigum and Robinson.

See Also

tbillyield2disc, zeroyield

tbillprice

Purpose Price Treasury bill

Syntax Price = tbillprice(Rate, Settle, Maturity, Type)

Arguments

Rate	Bond-equivalent yield, money-market yield, or discount rate in decimal.
Settle	Settlement date. Settle must be earlier than or equal to Maturity.
Maturity	Maturity date.
Type	(Optional) Rate type. Determines how to interpret values entered in Rate. 1 = money market (default). 2 = bond-equivalent. 3 = discount rate.

All arguments must be a scalar or some Treasury bills (NTBILLS) by 1 or 1-by-NTBILLS vector.

Note The bond-equivalent yield basis is actual/365. The money-market yield basis is actual/360. The discount rate basis is actual/360.

Description Price = tbillprice(Rate, Settle, Maturity, Type) computes the price of a Treasury bill given a yield or discount rate.

Price is an NTBILLS-by-1 vector of T-bill prices for every \$100 face.

Examples Example 1. Given a Treasury bill with these characteristics, compute the price of the Treasury bill using the bond-equivalent yield as input.

```
Rate = 0.045;  
Settle = '01-Oct-02';
```

```

Maturity = '31-Mar-03';

Type = 2;

Price = tbillprice(Rate, Settle, Maturity, Type)

Price =

    97.8172

```

Example 2. Use `tbillprice` to price a portfolio of Treasury bills.

```

Rate = [0.045; 0.046];
Settle = {'02-Jan-02'; '01-Mar-02'};
Maturity = {'30-June-02'; '30-June-02'};
Type = [2 3];

Price = tbillprice(Rate, Settle, Maturity, Type)

Price =

    97.8408
    98.4539

```

References

This function adheres to *SIA Fixed Income Securities Formulas for Price, Yield, and Accrued Interest*, Volume 1, 3rd edition, pp. 44 - 45 (on Treasury bills), and *Money Market and Bond Calculation* by Stigum and Robinson.

See Also

`tbillyield`, `zeroprice`

Purpose Break-even discount of repurchase agreement

Syntax `TBEDiscount = tbillrepo(RepoRate, InitialDiscount, PurchaseDate, SaleDate, Maturity)`

Arguments

RepoRate	The annualized, 360-day based repurchase rate, in decimal.
InitialDiscount	Discount on the Treasury bill on the day of purchase, in decimal.
PurchaseDate	Date the Treasury bill is purchased.
SaleDate	Date the Treasury bill repurchase term is due.
Maturity	Treasury bill maturity date.

All arguments must be a scalar or some Treasury bills (NTBILLS) by 1 or a 1-by-NTBILLS vector.

All dates must be in serial date number format.

Description `TBEDiscount = tbillrepo(RepoRate, InitialDiscount, PurchaseDate, SaleDate, Maturity)` computes the true break-even discount of a repurchase agreement. `TBEDiscount` can be a scalar or vector of size `NTBills-by-1`.

Examples Compute the true break-even discount on a Treasury bill repurchase agreement.

```
RepoRate = [0.045; 0.0475];  
InitialDiscount = 0.0475;  
PurchaseDate = '3-Jan-2002';  
SaleDate = '3-Feb-2002';  
Maturity = '3-Apr-2002';
```



```
TBEDiscount = tbillrepo(RepoRate, InitialDiscount,...  
PurchaseDate, SaleDate, Maturity)
```

```
TBEDiscount =
```

```
0.0491
```

```
0.0478
```

References

This function adheres to *SIA Fixed Income Securities Formulas for Price, Yield, and Accrued Interest*, Volume 1, 3rd edition, pp. 44 - 45 (on Treasury bills), and *Money Market and Bond Calculation* by Stigum and Robinson.

tbillval01

Purpose Value of one basis point

Syntax [Val01Disc, Val01MMY, Val01BEY] = tbillval01(Settle, Maturity)

Arguments

Settle	Settlement date of Treasury bills. Settle must be earlier than or equal to Maturity.
Maturity	Maturity date of Treasury bills.

Description

[Val01Disc, Val01MMY, Val01BEY] = tbillval01(Settle, Maturity) calculates the value of one basis point of \$100 Treasury bill face value on the discount rate, money-market yield, or bond-equivalent yield.

Val01Disc is the value of one basis point of discount rate.

Val01MMY is the value of one basis point of money-market yield.

Val01BEY is the value of one basis point of bond-equivalent yield.

All outputs are of size equal to the number of Treasury bills (NTBILLS) by 1.

Examples

Given a Treasury bill with these settle and maturity dates, compute the value of one basis point.

```
Settle = '01-Mar-03';
Maturity = '30-June-03';
[Val01Disc, Val01MMY, Val01BEY] = tbillval01(Settle, Maturity)

Val01Disc =

    0.0034
```

Val01MMY =

0.0034

Val01BEY =

0.0033

References

This function adheres to *SIA Fixed Income Securities Formulas for Price, Yield, and Accrued Interest*, Volume 1, 3rd edition, pp 108 - 115, on zero coupon instrument pricing.

See Also

tbilldisc2yield, tbillprice, tbillyield, tbillyield2disc

tbillyield

Purpose Yield on Treasury bill

Syntax [MMYield, BEYield, Discount] = tbillyield(Price, Settle, Maturity)

Arguments

Price	Price of Treasury bills for every \$100 face value.
Settle	Settlement date. Settle must be earlier than or equal to Maturity.
Maturity	Maturity date.

All arguments must be a scalar or some Treasury bills (NTBILLS) by 1 or 1-by-NTBILLS vector.

Description

[MMYield, BEYield, Discount] = tbillyield(Price, Settle, Maturity) computes the yield of U.S. Treasury bills given Price, Settle, and Maturity. MMYield is the money-market yields of the Treasury bills. BEYield is the bond equivalent yields of the Treasury bills. Discount is the discount rates of the Treasury bills.

All outputs are NTBILLS-by-1 vectors.

Note The money-market yield basis is actual/360. The bond-equivalent yield basis is actual/365. The discount rate basis is actual/360.

Examples

Given a Treasury bill with these characteristics, compute the money-market and bond-equivalent yields and the discount rate.

```
Price = 98.75;  
Settle = '01-Oct-02';  
Maturity = '31-Mar-03';
```

```
[MMYield, BEYield, Discount] = tbillyield(Price, Settle,...  
Maturity)
```

```
MMYield =
```

```
0.0252
```

```
BEYield =
```

```
0.0255
```

```
Discount =
```

```
0.0249
```

References

This function adheres to *SIA Fixed Income Securities Formulas for Price, Yield, and Accrued Interest*, Volume 1, 3rd edition, pp. 44 - 45 (on Treasury bills), and *Money Market and Bond Calculation* by Stigum and Robinson.

See Also

tbilldisc2yield, tbillprice, tbillyield2disc, zeroyield

tbillyield2disc

Purpose Convert Treasury bill yield to equivalent discount

Syntax `Discount = tbillyield2disc(Yield, Settle, Maturity, Type)`

Arguments

Yield	Yield of Treasury bills in decimal.
Settle	Settlement date. Settle must be earlier than or equal to Maturity.
Maturity	Maturity date.
Type	(Optional) Yield type. Determines how to interpret values entered in Yield. 1 = money market (default). 2 = bond-equivalent.

Inputs must either be a scalar or a vector of size equal to the number of Treasury bills (NTBILLS) by 1 or 1-by-NTBILLS.

Note The money-market yield basis is actual/360. The bond-equivalent yield basis is actual/365. The discount rate basis is actual/360.

Description

`Discount = tbillyield2disc(Yield, Settle, Maturity, Type)` converts the yield on some Treasury bills into their respective discount rates.

Discount is a NTBILLS-by-1 vector of T-bill discount rates.

Examples

Given a Treasury bill with these characteristics, compute the discount rate on a money-market basis.

```
Yield = 0.0497;  
Settle = '01-Oct-02';  
Maturity = '31-Mar-03';
```

```
Discount = tbillyield2disc(Yield, Settle, Maturity)
```

```
Discount =
```

```
0.0485
```

Now recompute the discount on a bond-equivalent basis.

```
Discount = tbillyield2disc(Yield, Settle, Maturity, 2)
```

```
Discount =
```

```
0.0478
```

References

This function adheres to *SIA Fixed Income Securities Formulas for Price, Yield, and Accrued Interest*, Volume 1, 3rd edition, pp. 44 - 45 (on Treasury bills), and *Money Market and Bond Calculation* by Stigum and Robinson.

See Also

tbilldisc2yield

tfutbyprice

Purpose Future prices of Treasury bonds given spot price

Syntax `QtdFutPrice = tfutbyprice(SpotCurve, Price, SettleFut, MatFut, ConvFactor, CouponRate, Maturity, Interpolation)`

Arguments

SpotCurve	Treasury spot curve; a number of futures (NFUT) by 3 matrix in the form of [SpotDates SpotRates Compounding]. Allowed compounding values are -1, 1, 2 (default), 3, 4, and 12.
Price	Scalar or vector containing prices of Treasury bonds or notes per \$100 notional. Use <code>bndprice</code> for theoretical value of bond.
SettleFut	Scalar or vector of identical elements containing settlement date of futures contract.
MatFut	Scalar or vector containing maturity dates (or anticipated delivery dates) of futures contract.
ConvFactor	Conversion factor. See <code>convfactor</code> .
CouponRate	Scalar or vector containing underlying bond annual coupon in decimal.
Maturity	Scalar or vector containing underlying bond maturity.
Interpolation	(Optional) Interpolation method. Available methods are (0) nearest, (1) linear, and (2) cubic. Default = 1. See <code>interp1</code> for more information.

Inputs (except `SpotCurve`) must either be a scalar or a vector of size equal to the number of Treasury futures (NFUT) by 1 or 1-by-NFUT.

Description

QtdFutPrice = tfutbyprice(SpotCurve, Price, SettleFut, MatFut, ConvFactor, CouponRate, Maturity, Interpolation) computes future prices of Treasury notes and bonds given the spot price.

Examples

Determine the future price of two Treasury bonds based upon a spot rate curve constructed from data for November 14, 2002.

```
% Constructing spot curve from Nov 14, data
Bonds = [datenum('02/13/2003'),      0;
         datenum('05/15/2003'),      0;
         datenum('10/31/2004'),    0.02125;
         datenum('11/15/2007'),     0.03;
         datenum('11/15/2012'),     0.04;
         datenum('02/15/2031'),    0.05375];

Yields = [1.20; 1.25; 1.86; 2.99; 4.02; 4.93]/100;

Settle = datenum('11/15/2002');

[ZeroRates, CurveDates] = ...
zbtyield(Bonds, Yields, Settle);

SpotCurve = [CurveDates, ZeroRates];

% Calculating a particular bond's future quoted price
RefDate    = [datenum('1-Dec-2002'); datenum('1-Mar-2003')];
MatFut     = [datenum('15-Dec-2002'); datenum('15-Mar-2003')];
Maturity   = [datenum('15-Aug-2009'); datenum('15-Aug-2010')];
CouponRate = [0.06;0.0575];
ConvFactor = convfactor(RefDate, Maturity, CouponRate);
Price      = [114.416; 113.171];
Interpolation = 1;

QtdFutPrice = tfutbyprice(SpotCurve, Price, Settle, ...
MatFut, ConvFactor, CouponRate, Maturity, Interpolation)

QtdFutPrice =
```

tfutbyprice

113.8129

112.4986

This compares with closing prices of 113.93 and 112.68. The differences are expected due to the nature of the contract and data that is not directly comparable.

See Also

convfactor, tfutbyyield

Purpose

Future prices of Treasury bonds given current yield

Syntax

QtdFutPrice = tfutbyield(SpotCurve, Yield, SettleFut, MatFut, ConvFactor, CouponRate, Maturity, Interpolation)

Arguments

SpotCurve	Treasury spot curve. A number of futures (NFUT) by 3 matrix in the form of [SpotDates SpotRates Compounding] Allowed compounding values are -1, 1, 2 (default), 3, 4, and 12.
Yield	Scalar or vector containing yield to maturity of bonds. Use bndyield for theoretical value of bond yield.
SettleFut	Scalar or vector of identical elements containing settlement date of futures contract.
MatFut	Scalar or vector containing maturity dates (or anticipated delivery dates) of futures contract.
ConvFactor	Conversion factor. See convfactor.
CouponRate	Scalar or vector containing underlying bond annual coupon in decimal.
Maturity	Scalar or vector containing underlying bond maturity.
Interpolation	(Optional) Interpolation method. Available methods are (0) nearest, (1) linear, and (2) cubic. Default = 1. See interp1 for more information.

Inputs (except SpotCurve) must either be a scalar or a vector of size equal to the number of Treasury futures (NFUT) by 1 or 1-by-NFUT.

Description

QtdFutPrice = tfutbyield(SpotCurve, Yield, SettleFut, MatFut, ConvFactor, CouponRate, Maturity, Interpolation)

computes future prices of Treasury notes and bonds given current yields of Treasury bonds/notes.

Examples

Determine the future price of two Treasury bonds based upon a spot rate curve constructed from data for November 14, 2002.

```
% Constructing spot curve from Nov 14, data
Bonds = [datenum('02/13/2003'),      0;
         datenum('05/15/2003'),      0;
         datenum('10/31/2004'), 0.02125;
         datenum('11/15/2007'),   0.03;
         datenum('11/15/2012'),   0.04;
         datenum('02/15/2031'), 0.05375];

Yields = [1.20; 1.25; 1.86; 2.99; 4.02; 4.93]/100;

Settle = datenum('11/15/2002');

[ZeroRates, CurveDates] = ...
zbtyield(Bonds, Yields, Settle);

SpotCurve = [CurveDates, ZeroRates];

% Calculating a particular bond's future quoted price
RefDate    = [datenum('1-Dec-2002'); datenum('1-Mar-2003')];
MatFut     = [datenum('15-Dec-2002'); datenum('15-Mar-2003')];
Maturity   = [datenum('15-Aug-2009'); datenum('15-Aug-2010')];
CouponRate = [0.06; 0.0575];
ConvFactor = convfactor(RefDate, Maturity, CouponRate);
Yield      = [0.03576; 0.03773];
Interpolation = 1;

QtdFutPrice = tfutbyyield(SpotCurve, Yield, Settle, ...
MatFut, ConvFactor, CouponRate, Maturity, Interpolation)

QtdFutPrice =
```

113.8136

112.4991

This compares with closing prices of 113.93 and 112.68. The differences are expected because of the nature of the contract and data that are not directly comparable.

See Also

convfactor, tfutbyprice

tfutimrepo

Purpose Implied simple annual repurchase rate to prevent arbitrage

Syntax `ImpliedRepo = tfutimrepo(ReinvestData, Price, QtdFutPrice, Settle, MatFut, ConvFactor, CouponRate, Maturity)`

Arguments

<code>ReinvestData</code>	Number of futures (NFUT) by 2 matrix of rates and bases for the reinvestment of intervening coupons in the form of [ReinvestRate ReinvestBasis]. ReinvestRate is the simple reinvestment rate, in decimal. Specify ReinvestBasis as 0 = not reinvested, 2 = actual/360, or 3 = actual/365.
<code>Price</code>	Current bond price per \$100 notional.
<code>QtdFutPrice</code>	Quoted bond futures price per \$100 notional.
<code>Settle</code>	Settlement/valuation date of futures contract.
<code>MatFut</code>	Maturity date (or anticipated delivery dates) of futures contract.
<code>ConvFactor</code>	Conversion factor. See convfactor.
<code>CouponRate</code>	Underlying bond annual coupon, in decimal.
<code>Maturity</code>	Underlying bond maturity date.

Inputs (except `ReinvestData`) must either be a scalar or a vector of size equal to the number of Treasury futures (NFUT) by 1 or 1-by-NFUT.

Description `ImpliedRepo = tfutimrepo(ReinvestData, Price, QtdFutPrice, Settle, MatFut, ConvFactor, CouponRate, Maturity)` computes the implied repo rate that prevents arbitrage of Treasury bond futures, given the clean price at the settlement and delivery dates.

ImpliedRepo is the implied annual repo rate, in decimal, with an actual/360 basis.

Examples

Compute the implied repo rate given the following set of data.

```
ReinvestData = [0.018 3];
Price = [114.4160; 113.1710];
QtdFutPrice = [114.1201; 113.7090];
Settle = datenum('11/15/2002');
MatFut = [datenum('15-Dec-2002'); datenum('15-Mar-2003')];
ConvFactor = [1; 0.9854];
CouponRate = [0.06; 0.0575];
Maturity = [datenum('15-Aug-2009'); datenum('15-Aug-2010')];

ImpliedRepo = tfutimprepo(ReinvestData, Price, QtdFutPrice, ...
Settle, MatFut, ConvFactor, CouponRate, Maturity)

ImpliedRepo =

    0.0200
    0.0200
```

See Also

tfutpricebyrepo, tfutyieldbyrepo

tfutpricebyrepo

Purpose Theoretical futures bond price

Syntax [QtdFutPrice AccrInt] = tfutpricebyrepo(RepoData, ReinvestData, Price, Settle, MatFut, ConvFactor, CouponRate, Maturity)

Arguments

RepoData	Number of futures (NFUT) by 2 matrix of simple term repo/funding rates in decimal and their bases in the form of [RepoRate RepoBasis]. Specify RepoBasis as 2 = actual/360 or 3 = actual/365.
ReinvestData	Number of futures (NFUT) by 2 matrix of rates and bases for the reinvestment of intervening coupons in the form of [ReinvestRate ReinvestBasis]. ReinvestRate is the simple reinvestment rate, in decimal. Specify ReinvestBasis as 0 = not reinvested, 2 = actual/360, or 3 = actual/365.
Price	Quoted clean prices of Treasury bonds per \$100 notional at Settle.
Settle	Settlement/valuation date of futures contract.
MatFut	Maturity date (or anticipated delivery dates) of futures contract.
ConvFactor	Conversion factor. See convfactor.
CouponRate	Underlying bond annual coupon, in decimal.
Maturity	Underlying bond maturity date.

Inputs (except RepoData and ReinvestData) must either be a scalar or a vector of size equal to the number of Treasury futures (NFUT) by 1 or 1-by-NFUT.

Description

[QtdFutPrice AccrInt] = tfutpricebyrepo(RepoData, ReinvestData, Price, Settle, MatFut, ConvFactor, CouponRate, Maturity) computes the theoretical futures bond price given the settlement price, the repo/funding rates, and the reinvestment rate.

QtdFutPrice is the quoted futures price, per \$100 notional.

AccrInt is the accrued interest due at the delivery date, per \$100 notional.

Examples

Compute the quoted futures price and accrued interest due on the target delivery date, given the following data.

```
RepoData      = [0.020  2];
ReinvestData  = [0.018  3];
Price         = [114.416; 113.171];
Settle        = datenum('11/15/2002');
MatFut        = [datenum('15-Dec-2002'); datenum('15-Mar-2003')];
ConvFactor    = [1 ; 0.9854];
CouponRate    = [0.06;0.0575];
Maturity      = [datenum('15-Aug-2009'); datenum('15-Aug-2010')];
```

```
[QtdFutPrice AccrInt] = tfutpricebyrepo(RepoData, ...
ReinvestData, Price, Settle, MatFut, ConvFactor, CouponRate, ...
Maturity)
```

```
QtdFutPrice =
```

```
114.1201
```

```
113.7090
```

```
AccrInt =
```

```
1.9891
```

```
0.4448
```

See Also

tfutimprepo, tfutyieldbyrepo

tfutyieldbyrepo

Purpose Theoretical futures bond yield

Syntax `FwdYield = tfutyieldbyrepo(RepoData, ReinvestData, Yield, Settle, MatFut, ConvFactor, CouponRate, Maturity)`

Arguments

RepoData	Number of futures (NFUT) by 2 matrix of simple term repo/funding rates in decimal and their bases in the form of [RepoRate RepoBasis]. Specify RepoBasis as 2 = actual/360 or 3 = actual/365.
ReinvestData	Number of futures (NFUT) by 2 matrix of rates and bases for the reinvestment of intervening coupons in the form of [ReinvestRate ReinvestBasis]. ReinvestRate is the simple reinvestment rate, in decimal. Specify ReinvestBasis as 0 = not reinvested, 2 = actual/360, or 3 = actual/365.
Yield	Yield to maturity of Treasury bonds per \$100 notional at Settle.
Settle	Settlement/valuation date of futures contract.
MatFut	Maturity date (or anticipated delivery dates) of futures contract.
ConvFactor	Conversion factor. See convfactor.
CouponRate	Underlying bond annual coupon, in decimal.
Maturity	Underlying bond maturity date.

Inputs (except RepoData and ReinvestData) must either be a scalar or a vector of size equal to the number of Treasury futures (NFUT) by 1 or 1-by-NFUT.

Description

FwdYield = tfutyieldbyrepo(RepoData, ReinvestData, Yield, Settle, MatFut, ConvFactor, CouponRate, Maturity) computes the theoretical futures bond yield given the settlement yield, the repo/funding rate, and the reinvestment rate.

FwdYield is the forward yield to maturity, in decimal, compounded semiannually.

Examples

Compute the quoted futures bond yield, given the following data:

```
RepoData      = [0.020  2];
ReinvestData  = [0.018  3];
Yield         = [0.0215; 0.0257];
Settle        = datenum('11/15/2002');
MatFut        = [datenum('15-Dec-2002'); datenum('15-Mar-2003')];
ConvFactor    = [1; 0.9854];
CouponRate    = [0.06; 0.0575];
Maturity      = [datenum('15-Aug-2009'); datenum('15-Aug-2010')];
```

```
FwdYield = tfutyieldbyrepo(RepoData, ReinvestData, Yield,...
Settle, MatFut, ConvFactor, CouponRate, Maturity)
```

```
FwdYield =
```

```
    0.0221
    0.0282
```

See Also

tfutimprepo, tfutpricebyrepo

zeroprice

Purpose Price zero-coupon instruments given yield

Syntax Price = zeroprice(Yield, Settle, Maturity, Period, Basis, EndMonthRule)

Arguments

Yield	Scalar or vector containing yield to maturity of instruments.
Settle	Settlement date. A vector of serial date numbers or date strings. Settle must be earlier than or equal to Maturity.
Maturity	Maturity date. A vector of serial date numbers or date strings.
Period	(Optional) Scalar or vector specifying number of quasi-coupons per year. Default = 2.
Basis	(Optional) Day-count basis of the bond. A vector of integers. <ul style="list-style-type: none">• 0 = actual/actual (default)• 1 = 30/360 (SIA)• 2 = actual/360• 3 = actual/365• 4 = 30/360 (PSA)• 5 = 30/360 (ISDA)• 6 = 30/360 (European)• 7 = actual/365 (Japanese)• 8 = actual/actual (ISMA)• 9 = actual/360 (ISMA)

- 10 = actual/365 (ISMA)

EndMonthRule (Optional) End-of-month rule. A vector. This rule applies only when **Maturity** is an end-of-month date for a month having 30 or fewer days. 0 = ignore rule, meaning that a bond's coupon payment date is always the same numerical day of the month. 1 = set rule on (default), meaning that a bond's coupon payment date is always the last actual day of the month.

Description

$\text{Price} = \text{zeroprice}(\text{Yield}, \text{Settle}, \text{Maturity}, \text{Period}, \text{Basis}, \text{EndMonthRule})$ calculates the prices for a portfolio of general short and long term zero-coupon instruments given the yield of the instruments. **Price** is a column vector containing a price for each zero-coupon instrument.

When there is less than one quasi-coupon, the function uses a simple yield based upon "Period times Number of Days in quasi coupon period" day-year. The default period is 2 and the default number of days is 180, which makes the user-supplied yield a simple yield on a 360-day year.

For longer term computations (more than one quasi-coupon), use the bond equivalent yield based upon present value (or compounding).

Formulas

To compute the price when there is one or zero quasi-coupon periods to redemption, **zeroprice** uses the formula

$$\text{Price} = \frac{RV}{1 + \left(\frac{DSR}{E} \cdot \frac{Y}{M} \right)}$$

Quasi-coupon periods are the coupon periods that would exist if the bond were paying interest at a rate other than zero.

When there is more than one quasi-coupon period to the redemption date, **zeroprice** uses the formula

zeroprice

$$Price = \frac{RV}{\left(1 + \frac{Y}{M}\right)^{Nq - 1 + \frac{DSC}{E}}}$$

The elements of the equations are defined as follows.

Variable	Definition
<i>DSC</i>	Number of days from settlement date to next quasi-coupon date as if the security paid periodic interest.
<i>DSR</i>	Number of days from settlement date to the redemption date (call date, put date, and so on).
<i>E</i>	Number of days in quasi-coupon period.
<i>M</i>	Number of quasi-coupon periods per year (standard for the particular security involved).
<i>Nq</i>	Number of quasi-coupon periods between settlement date and redemption date. If this number contains a fractional part, raise it to the next whole number.
<i>Price</i>	Dollar price per \$100 par value.
<i>RV</i>	Redemption value.
<i>Y</i>	Annual yield (decimal) when held to redemption.

Examples

Example 1. Compute the price of a short-term zero-coupon instrument.

```
Settle = '24-Jun-1993';  
Maturity = '1-Nov-1993';  
Period = 2;  
Basis = 0;  
Yield = 0.04;
```

```
Price = zeroprice(Yield, Settle, Maturity, Period, Basis)
```

```
Price =
```

98.6066

Example 2. Compute the prices of a portfolio of two zero-coupon instruments, one short term, and the other long term.

```
Settle = '24-Jun-1993';
Maturity = ['01-Nov-1993'; '15-Jan-2024'];
Basis = [0; 1];
Yield = [0.04; 0.1];

Price = zeroprice(Yield, Settle, Maturity, [], Basis)

Price =

    98.6066
     5.0697
```

References

[1] Mayle, Jan. *Standard Securities Calculation Methods*. New York: Securities Industry Association, Inc. Vol. 1, 3rd ed., 1993, ISBN 1-882936-01-9. Vol. 2, 1994, ISBN 1-882936-02-7.

See Also

bndprice, cdprice, tbillprice, zeroyield

zeroyield

Purpose Yield of zero-coupon instruments given price

Syntax Yield = zeroyield(Price, Settle, Maturity, Period, Basis, EndMonthRule)

Arguments

Price	Scalar or vector containing prices of instruments.
Settle	Settlement date. A vector of serial date numbers or date strings. Settle must be earlier than or equal to Maturity.
Maturity	Maturity date. A vector of serial date numbers or date strings.
Period	(Optional) Scalar or vector specifying number of quasi-coupons per year. Default = 2.
Basis	(Optional) Day-count basis of the bond. A vector of integers. <ul style="list-style-type: none">• 0 = actual/actual (default)• 1 = 30/360 (SIA)• 2 = actual/360• 3 = actual/365• 4 = 30/360 (PSA)• 5 = 30/360 (ISDA)• 6 = 30/360 (European)• 7 = actual/365 (Japanese)• 8 = actual/actual (ISMA)• 9 = actual/360 (ISMA)

- 10 = actual/365 (ISMA)

EndMonthRule (Optional) End-of-month rule. A vector. This rule applies only when **Maturity** is an end-of-month date for a month having 30 or fewer days. 0 = ignore rule, meaning that a bond's coupon payment date is always the same numerical day of the month. 1 = set rule on (default), meaning that a bond's coupon payment date is always the last actual day of the month.

Description

$\text{Yield} = \text{zeroyield}(\text{Price}, \text{Settle}, \text{Maturity}, \text{Period}, \text{Basis}, \text{EndMonthRule})$ calculates the bond-equivalent yield for a portfolio of general short and long term zero-coupon instruments given the price of the instruments. **Yield** is a column vector containing a yield for each zero-coupon instrument.

When the maturity date is fewer than 182 days away and the basis is actual/365, the function uses a simple-interest algorithm. If maturity is more than 182 days away, the function uses present value calculations.

When the basis is actual/360, the simple interest algorithm gives the money-market yield for short (one to six months to maturity) Treasury bills.

The present value algorithm always gives the bond equivalent yield of the zero-coupon instrument. The algorithm is equivalent to calling **bdyield** with the zero-coupon information within one basis point.

Formulas

To compute the yield when there is zero or one quasi-coupon periods to redemption, **zeroyield** uses the formula

$$\text{Yield} = \left(\frac{RV - P}{P} \right) \cdot \left(\frac{M \cdot E}{DSR} \right)$$

Quasi-coupon periods are the coupon periods which would exist if the bond was paying interest at a rate other than zero. The first term

zeroyield

calculates the yield on invested dollars. The second term converts this yield to a per annum basis.

When there is more than one quasi-coupon period to the redemption date, zeroyield uses the formula

$$Yield = \left(\left(\frac{RV}{P} \right)^{\frac{1}{Nq - 1 + \frac{DSC}{E}}} - 1 \right) \cdot M$$

The elements of the equations are defined as follows.

Variable Definition	
<i>DSC</i>	Number of days from settlement date to next quasi-coupon date as if the security paid periodic interest.
<i>DSR</i>	Number of days from settlement date to redemption date (call date, put date, and so on).
<i>E</i>	Number of days in quasi-coupon period.
<i>M</i>	Number of quasi-coupon periods per year (standard for the particular security involved).
<i>Nq</i>	Number of quasi-coupon periods between settlement date and redemption date. If this number contains a fractional part, raise it to the next whole number.
<i>P</i>	Dollar price per \$100 par value.
<i>RV</i>	Redemption value.
<i>Yield</i>	Annual yield (decimal) when held to redemption.

Examples

Example 1. Compute the yield of a short-term zero-coupon instrument.

```
Settle = '24-Jun-1993';  
Maturity = '1-Nov-1993';  
Basis = 0;
```

```
Price      = 95;

Yield = zeroyield(Price, Settle, Maturity, [], Basis)

Yield =

    0.1490
```

Example 2. Recompute the yield of the same instrument using a different day-count basis.

```
Settle     = '24-Jun-1993';
Maturity   = '1-Nov-1993';
Basis      = 1;
Price      = 95;

Yield = zeroyield(Price, Settle, Maturity, [], Basis)

Yield =

    0.1492
```

Example 3. Compute the yield of a long-term zero-coupon instrument.

```
Settle     = '24-Jun-1993';
Maturity   = '15-Jan-2024';
Basis      = 0;
Price      = 9;

Yield = zeroyield(Price, Settle, Maturity, [], Basis)

Yield =

    0.0804
```

zeroyield

References

[1] Mayle, Jan. *Standard Securities Calculation Methods*. New York: Securities Industry Association, Inc. Vol. 1, 3rd ed., 1993, ISBN 1-882936-01-9. Vol. 2, 1994, ISBN 1-882936-02-7.

See Also

bndyield, cdyield, tbillyield, zeroprice

Examples

Use this list to find examples in the documentation.

Treasury Bills

“Treasury Bill Repurchase Agreements” on page 3-3

“Treasury Bill Yields” on page 3-5

Using Zero-Coupon Bonds

“Pricing Treasury Notes” on page 3-8

“Pricing Corporate Bonds” on page 3-10

Stepped-Coupon Bonds

“Cash Flows from Stepped-Coupon Bonds” on page 3-12

“Price and Yield of Stepped-Coupon Bonds” on page 3-13

Pricing and Hedging

“Swap Pricing Example” on page 4-3

Treasury Bond Futures

“Theoretical Prices” on page 4-12

“Implied Repo” on page 4-15

American option

An option that can be exercised any time until its expiration date. Contrast with European option.

amortization

Reduction in value of an asset over some period for accounting purposes. Generally used with intangible assets. Depreciation is the term used with fixed or tangible assets.

annuity

A series of payments over a period of time. The payments are usually in equal amounts and usually at regular intervals such as quarterly, semiannually, or annually.

arbitrage

The purchase of securities on one market for immediate resale on another market in order to profit from a price or currency discrepancy.

basis point

One hundredth of one percentage point, or 0.0001.

beta

The price volatility of a financial instrument relative to the price volatility of a market or index as a whole. Beta is most commonly used with respect to equities. A high-beta instrument is riskier than a low-beta instrument.

binomial model

A method of pricing options or other equity derivatives in which the probability over time of each possible price follows a binomial distribution. The basic assumption is that prices can move to only two values (one higher and one lower) over any short time period.

Black-Scholes model

The first complete mathematical model for pricing options, developed by Fischer Black and Myron Scholes. It examines market price, strike price, volatility, time to expiration, and interest rates. It is limited to only certain kinds of options.

Bollinger band chart

A financial chart that plots actual asset data along with three other bands of data: the upper band is two standard deviations above a user-specified moving average; the lower band is two standard deviations below that moving average; and the middle band is the moving average itself.

bootstrapping, bootstrap method

An arithmetic method for backing an implied zero curve out of the par yield curve.

building a binomial tree

For a binomial option model: plotting the two possible short-term price-changes values, and then the subsequent two values each, and then the subsequent two values each, and so on, over time, is known as “building a binomial tree.” See also **binomial model** on page Glossary-1.

call

a. An option to buy a certain quantity of a stock or commodity for a specified price within a specified time. See **put** on page Glossary-9. **b.** A demand to submit bonds to the issuer for redemption before the maturity date. **c.** A demand for payment of a debt. **d.** A demand for payment due on stock bought on margin.

callable bond

A bond that allows the issuer to buy back the bond at a predetermined price at specified future dates. The bond contains an embedded call option; that is, the holder has sold a call option to the issuer. See also **puttable bond** on page Glossary-10.

cap

Interest-rate option that guarantees that the rate on a floating-rate loan will not exceed a certain level.

caplet

A cap that is guaranteed for one particular date.

cash flow

Cash received and paid over time.

cheapest to deliver

Cheapest to deliver represents the least expensive underlying product that can be delivered upon expiry to satisfy the requirements of a derivative contract.

collar

Interest-rate option that guarantees that the rate on a floating-rate loan will not exceed a certain upper level nor fall below a lower level. It is designed to protect an investor against wide fluctuations in interest rates.

conditional prepayment rate (CPR)

The fraction of mortgage principal that had not prepaid at the beginning of any year but does prepay during the year. CPR is an annualization of the single monthly mortality rate. See also **single monthly mortality (SMM)** on page Glossary-11.

conversion factor

The rate used to adjust differences in bond values for delivery on U.S. Treasury bond futures contracts.

convexity

A measure of the rate of change in duration; measured in time. The greater the rate of change, the more the duration changes as yield changes.

correlation

The simultaneous change in value of two random numeric variables.

correlation coefficient

A statistic in which the covariance is scaled to a value between minus one (perfect negative correlation) and plus one (perfect positive correlation).

coupon

Detachable certificate attached to a bond that shows the amount of interest payable at regular intervals, usually semiannually. Originally coupons were actually attached to the bonds and had to be cut off or "clipped" to redeem them and receive the interest payment.

coupon dates

The dates when the coupons are paid. Typically a bond pays coupons annually or semiannually.

coupon rate

The nominal interest rate that the issuer promises to pay the buyer of a bond.

covariance

A measure of the degree to which returns on two assets move in tandem. A positive covariance means that asset returns move together; a negative covariance means they vary inversely.

delta

The rate of change of the price of a derivative security relative to the price of the underlying asset; that is, the first derivative of the curve that relates the price of the derivative to the price of the underlying security.

depreciation

Reduction in value of fixed or tangible assets over some period for accounting purposes. See also **amortization** on page Glossary-1.

derivative

A financial instrument that is based on some underlying asset. For example, an option is a derivative instrument based on the right to buy or sell an underlying instrument.

discount curve

The curve of discount rates vs. maturity dates for bonds.

duration

The expected life of a fixed-income security considering its coupon yield, interest payments, maturity, and call features. As market interest rates rise, the duration of a financial instrument decreases. See also **Macaulay duration** on page Glossary-7.

efficient frontier

A graph representing a set of portfolios that maximizes expected return at each level of portfolio risk. See also **Markowitz model** on page Glossary-7.

elasticity

See **lambda** on page Glossary-6.

Eurodollar

U.S. dollar-denominated deposits at foreign banks or foreign branches of American banks.

European option

An option that can be exercised only on its expiration date. Contrast with American option.

exercise price

The price set for buying an asset (call) or selling an asset (put). The strike price.

face value

The maturity value of a security. Also known as par value, principal value, or redemption value.

fixed-income security

A security that pays a specified cash flow over a specific period. Bonds are typical fixed-income securities.

floor

Interest-rate option that guarantees that the rate on a floating-rate loan will not fall below a certain level.

forward curve

The curve of forward interest rates vs. maturity dates for bonds.

forward rate

The future interest rate of a bond inferred from the term structure, especially from the yield curve of zero-coupon bonds, calculated from the growth factor of an investment in a zero held until maturity.

forward rate agreement (FRA)

A forward contract that determines an interest rate to be paid or received on an obligation beginning at a start date sometime in the future.

future value

The value that a sum of money (the present value) earning compound interest will have in the future.

gamma

The rate of change of delta for a derivative security relative to the price of the underlying asset; that is, the second derivative of the option price relative to the security price.

Greeks

Collectively, "greeks" refer to the financial measures delta, gamma, lambda, rho, theta, and vega, which are sensitivity measures used in evaluating derivatives.

hedge

A securities transaction that reduces or offsets the risk on an existing investment position.

implied volatility

For an option, the variance that makes a call option price equal to the market price. Given the option price, strike price, and other factors, the Black-Scholes model computes implied volatility.

internal rate of return

a. The average annual yield earned by an investment during the period held. **b.** The effective rate of interest on a loan. **c.** The discount rate in discounted cash flow analysis. **d.** The rate that adjusts the value of future cash receipts earned by an investment so that interest earned equals the original cost. See also **yield to maturity** on page Glossary-13.

issue date

The date a security is first offered for sale. That date usually determines when interest payments, known as coupons, are made.

lambda

The percentage change in the price of an option relative to a 1% change in the price of the underlying security. Also known as elasticity.

LIBOR

Abbreviation for London Interbank Offered Rate, an interest rate set daily in London. Applies to loans among large international banks.

long position

Outright ownership of a security or financial instrument. The owner expects the price to rise to make a profit on some future sale.

long rate

The yield on a zero-coupon Treasury bond.

Macaulay duration

A widely used measure of price sensitivity to yield changes developed by Frederick Macaulay in 1938. It is measured in years and is a weighted average-time-to-maturity of an instrument. The Macaulay duration of an income stream, such as a coupon bond, measures how long, on average, the owner waits before receiving a payment. It is the weighted average of the times payments are made, with the weights at time T equal to the present value of the money received at time T .

Markowitz model

A model for selecting an optimum investment portfolio, devised by H. M. Markowitz. It uses a discrete-time, continuous-outcome approach for modeling investment problems, often called the mean-variance paradigm. See also **efficient frontier** on page Glossary-4.

maturity date

The date when the issuer returns the final face value of a bond to the buyer.

mean

a. A number that typifies a set of numbers, such as a geometric mean or an arithmetic mean. **b.** The average value of a set of numbers.

modified duration

The Macaulay duration discounted by the per-period interest rate; that is, divided by $(1 + \text{rate}/\text{frequency})$.

Monte-Carlo simulation

A mathematical modeling process. For a model that has several parameters with statistical properties, pick a set of random values for the parameters and run a simulation. Then pick another set of values, and run it again. Run it many times (often 10,000 times) and build up a statistical distribution of outcomes of the simulation. This distribution of outcomes is then used to answer whatever question you are asking.

moving average

A price average that is adjusted by adding other parametrically determined prices over some time period.

moving-averages chart

A financial chart that plots leading and lagging moving averages for prices or values of an asset.

normal (bell-shaped) distribution

In statistics, a theoretical frequency distribution for a set of variable data, usually represented by a bell-shaped curve symmetrical about the mean.

notional

The nominal value used to calculate swap payments.

odd first or last period

Fixed-income securities may be purchased on dates that do not coincide with coupon or payment dates. The length of the first and last periods may differ from the regular period between coupons, and thus the bond owner is not entitled to the full value of the coupon for that period. Instead, the coupon is prorated according to how long the bond is held during that period.

off-the-run

All Treasury bonds and notes issued before the most recently issued bond or note of a particular maturity. These are the opposite of on-the-run treasuries.

on-the-run

The most recently issued U.S. Treasury bond or note of a particular maturity. These are the opposite of off-the-run treasuries.

option

A right to buy or sell specific securities or commodities at a stated price (exercise or strike price) within a specified time. An option is a type of derivative.

option-adjusted spread

A yield spread that is not directly attributable to the characteristics of a fixed income security.

passthrough

A type of mortgage-backed security in which the interest and principal payments on the underlying mortgages "pass through" to the holders, pro rata, minus a servicing fee.

par value

The maturity or face value of a security or other financial instrument.

par yield curve

The yield curve of bonds selling at par, or face, value.

present value

Today's value of an investment that yields some future value when invested to earn compounded interest at a known interest rate; that is, the future value at a known period in time discounted by the interest rate over that time period.

principal value

See **par value** on page Glossary-9.

purchase price

Price paid for a security. Typically the purchase price of a bond is not the same as the redemption value.

put

An option to sell a stipulated amount of stock or securities within a specified time and at a fixed exercise price. See also **call** on page Glossary-2.

puttable bond

A bond that allows the holder to redeem the bond at a predetermined price at specified future dates. The bond contains an embedded put option; that is, the holder has bought a put option. See also **callable bond** on page Glossary-2.

redemption value

See **par value** on page Glossary-9.

regression analysis

Statistical analysis techniques that quantify the relationship between two or more variables. The intent is quantitative prediction or forecasting, particularly using a small population to forecast the behavior of a large population.

rho

The rate of change in a derivative's price relative to the underlying security's risk-free interest rate.

sensitivity

The "what if" relationship between variables; the degree to which changes in one variable cause changes in another variable. A specific synonym is volatility.

settlement date

The date when money first changes hands; that is, when a buyer actually pays for a security. It need not coincide with the issue date.

short rate

The annualized one-period interest rate.

short sale, short position

The sale of a security or financial instrument not owned, in anticipation of a price decline and making a profit by purchasing the instrument later at a lower price, and then delivering the instrument to complete the sale. See **long position** on page Glossary-7.

single monthly mortality (SMM)

The fraction of mortgage principal that had not prepaid at the beginning of a given month but does prepay during the month. See also **conditional prepayment rate (CPR)** on page Glossary-3.

spot curve, spot yield curve

See **zero curve, zero-coupon yield curve** on page Glossary-13.

spot rate

The current interest rate appropriate for discounting a cash flow of some given maturity.

spread

For options, a combination of call or put options on the same stock with differing exercise prices or maturity dates.

standard deviation

A measure of the variation in a distribution, equal to the square root of the arithmetic mean of the squares of the deviations from the arithmetic mean; the square root of the variance.

stochastic

Involving or containing a random variable or variables; involving chance or probability.

straddle

A strategy used in trading options or futures. It involves simultaneously purchasing put and call options with the same exercise price and expiration date, and it is most profitable when the price of the underlying security is volatile.

strike

Exercise a put or call option.

strike price

See **exercise price** on page Glossary-5.

swap

A contract between two parties to exchange cash flows in the future according to some formula.

swap option

A swap option; an option on an interest-rate swap. The option gives the holder the right to enter into a contracted interest-rate swap at a specified future date. See also **swap** on page Glossary-11.

tenor

Life of a swap.

term structure

The relationship between the yields on fixed-interest securities and their maturity dates. Expectation of changes in interest rates affects term structure, as do liquidity preferences and hedging pressure. A yield curve is one representation in the term structure.

theta

The rate of change in the price of a derivative security relative to time. Theta is usually small or negative since the value of an option tends to drop as it approaches maturity.

Treasury bill

Short-term U.S. Government security issued at a discount from the face value and paying the face value at maturity.

Treasury bond

Long-term debt obligation of the U.S. Government that makes coupon payments semiannually and is sold at or near par value in \$1000 denominations or higher. Face value is paid at maturity.

variance

The dispersion of a variable. The square of the standard deviation.

vega

The rate of change in the price of a derivative security relative to the volatility of the underlying security. When vega is large the security is sensitive to small changes in volatility.

volatility

a. Another general term for sensitivity. **b.** The standard deviation of the annualized continuously compounded rate of return of an asset. **c.** A measure of uncertainty or risk.

yield

a. Measure of return on an investment, stated as a percentage of price. Yield can be computed by dividing return by purchase price, current market value, or other measure of value. **b.** Income from a bond expressed as an annualized percentage rate. **c.** The nominal annual interest rate that gives a future value of the purchase price equal to the redemption value of the security. Any coupon payments determine part of that yield.

yield curve

Graph of yields (vertical axis) of a particular type of security versus the time to maturity (horizontal axis). This curve usually slopes upward, indicating that investors usually expect to receive a premium for securities that have a longer time to maturity. The benchmark yield curve is for U.S. Treasury securities with maturities ranging from three months to 30 years. See **term structure** on page Glossary-12.

yield to maturity

A measure of the average rate of return that will be earned on a bond if held to maturity.

zero curve, zero-coupon yield curve

A yield curve for zero-coupon bonds; zero rates versus maturity dates. Since the maturity and duration (Macaulay duration) are identical for zeros, the zero curve is a pure depiction of supply/demand conditions for loanable funds across a continuum of durations and maturities. Also known as spot curve or spot yield curve.

zero-coupon bond, or zero

A bond that, instead of carrying a coupon, is sold at a discount from its face value, pays no interest during its life, and pays the principal only at maturity.

A

actual/360 3-2

B

bkcall 6-2
bkcaplet 6-8
bkfloorlet 6-11
bkput 6-14
bond equivalent yield 6-86
break-even discount rate 3-3

C

cbprice 6-20
cdai 6-25
cdprice 6-27
cdyield 6-29
cfamounts 6-31
cheapest to deliver (CTD) 4-15
conditional prepayment rate (CPR) 2-4
convertible bond 4-10
convfactor 6-37
coupon bond functions 3-7
CPR
 (conditional payment rate) 2-4
CTD
 (cheapest to deliver) 4-15

D

discount security 3-2
duration
 modified 2-8
DV01 4-16

E

effective duration 2-10
 defined mathematically 2-10

F

forward rate agreement 6-41
 defined 6-45

I

implied repo 4-15

L

liborduration 6-39
liborfloat2fixed 6-41
liborprice 6-45

M

mbscfamounts 6-48
mbsconvp 6-51
mbsconvy 6-53
mbsdurp 6-55
mbsdury 6-58
mbsnoprepay 6-61
mbsoas2price 6-63
mbsoas2yield 6-67
mbspassthrough 6-71
mbsprice 6-73
mbsprice2oas 6-76
mbsprice2speed 6-80
mbswal 6-83
mbsyield 6-85
mbsyield2oas 6-88
mbsyield2speed 6-92
modified duration 2-8
mortgage-backed securities 2-2
mortgage yield 6-86

O

OAS
 (option-adjusted spread) 2-9
off-the-run 3-15

on-the-run 3-15
option-adjusted spread
 defined 2-10
option-adjusted spread (OAS) 2-9
 effect on pool pricing 2-9

P

passthrough certificate 2-2
prepayment 2-3
prepayment summary 2-16
psaspeed2default 6-95
psaspeed2rate 6-96
Public Securities Association (PSA) 2-3

Q

quasi-coupon periods
 zeroprice 6-139
 zeroyield 6-143

S

seasoned prepayment vector 2-13
single monthly mortality (SMM) rate 2-4
SMM
 single monthly mortality rate 2-4
spread 3-15
 term structure of 3-15
stepcpncfamounts 6-98

stepcpnprice 6-104
stepcpnyield 6-109

T

tbilldisc2yield 6-114
tbillprice 6-116
tbillrepo 6-118
tbillval01 6-120
tbillyield 6-122
tbillyield2disc 6-124
tenor 6-39
tfutbyprice 6-126
tfutbyyield 6-129
tfutimprepo 6-132
tfutpricebyrepo 6-134
time factor 6-34
Treasury bills
 defined 3-2
Treasury bonds 3-2
Treasury notes 3-2

Z

zero-coupon bond
 defined 3-7
 quality of measurement 3-7
zeroprice 6-138
zeroyield 6-142